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TIME SERIES STOCHASTIC PROCESS
AND FORECASTING

by

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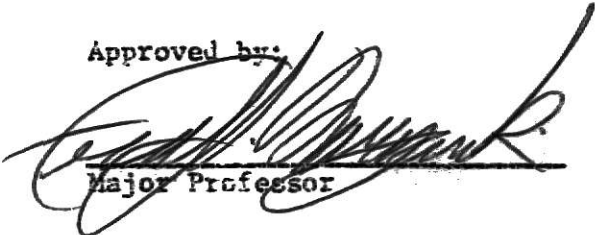
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To my parents and my wife Nancy
for
their love and patience

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