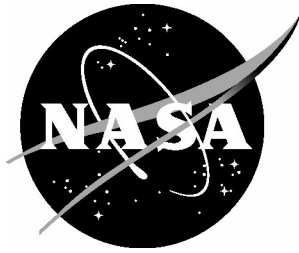


NASA/TP-2015-218980



# Solar Proton Transport within an ICRU Sphere Surrounded by a Complex Shield: Combinatorial Geometry

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November 2015

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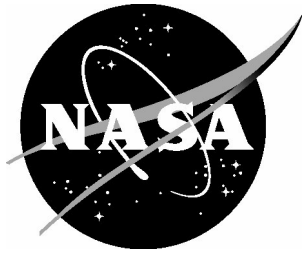
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## Abstract

*The 3DHZETRN code, with improved neutron and light ion ( $Z \leq 2$ ) transport procedures, was recently developed and compared to Monte Carlo (MC) simulations using simplified spherical geometries. It was shown that 3DHZETRN agrees with the MC codes to the extent they agree with each other. In the present report, the 3DHZETRN code is extended to enable analysis in general combinatorial geometry. A more complex shielding structure with internal parts surrounding a tissue sphere is considered and compared against MC simulations. It is shown that even in the more complex geometry, 3DHZETRN agrees well with the MC codes and maintains a high degree of computational efficiency.*

## Introduction

A 3D version of HZETRN has recently been developed and tested in simple geometries and compared to available Monte Carlo (MC) codes [Wilson et al. 2014a-c, 2015]. In the first study [Wilson et al. 2014a,b], an aluminum sphere with a radial thickness of 20 g/cm<sup>2</sup> was examined, and comparisons were made between 3DHZETRN results and MC simulations at locations within the sphere exposed to solar particle event (SPE) and galactic cosmic ray (GCR) boundary conditions. Well defined convergence tests were performed that spanned the transport formalism, covering the straight ahead approximation ( $N = 1$ ), bi-directional approximation ( $N = 2$ ), and more detailed 3D treatment ( $N > 2$ ) for neutrons and light ions. Note that in the formalism of Wilson et al. [2014a-c, 2015],  $N$  denotes the number of transport directions used to describe the assumed isotropic neutron and light ion fluxes at lower energies. The convergence tests and comparison to MC results established improved description of the neutron and light ion solutions within the 3D formalism. It was also shown that although there are still noticeable differences associated with the nuclear production models used in the codes, 3DHZETRN agreed with the MC models to the extent they agree with each other in finite geometry. The main difference between the transport codes was found to be in the computational costs. While 3DHZETRN results were generated in several seconds on a single CPU, the MC code run times were several orders of magnitude larger ( $\sim 10^8$  seconds) and required high performance computing clusters.

In the next study [Wilson et al. 2014c, 2015], a tissue sphere with a radial thickness of 15 g/cm<sup>2</sup>, defined by the International Commission on Radiation Units and Measurements (ICRU) [ICRU 1993], was surrounded by an aluminum spherical shell with thickness 20 g/cm<sup>2</sup>, and similar convergence tests and comparisons to MC were provided. Improvements in the low energy neutron and light ion spectra as a result of 3D corrections were again clearly established. Despite the added geometric complexity of the two material sphere configuration, agreement between all the codes was actually improved compared to the previous single material aluminum sphere. The improved agreement was attributed to the hydrogen content of the ICRU tissue sphere. For energies below  $\sim 100$  MeV, elastic collisions between neutrons and hydrogen dominate the neutron transport processes. These elastic collisions, on average, transfer half the neutron energy to the target hydrogen, which in turn, very rapidly attenuates the neutron energy spectrum. Although neutron production cross sections show significant variation amongst the codes for aluminum targets, as seen in the first study [Wilson et al. 2014a,b], neutron-hydrogen elastic cross sections are more precisely and accurately represented in the codes either through evaluated nuclear data files or detailed parameterizations [Wilson et al. 1991]. Again, it was found that 3DHZETRN was in good agreement with the MC simulation results, and the primary difference between the codes lay in the associated computational costs, where 3DHZETRN is several orders of magnitude faster.

Herein, a more complex and realistic shielding geometry with multiple parts is considered. An ICRU tissue sphere is surrounded by a cylindrical aluminum shell containing two additional internal aluminum boxes. The sizes and locations of the internal parts are chosen to provide partial shielding of the ICRU sphere, thereby emphasizing 3D effects in the transport process. The chosen geometry is sufficiently complex to further test 3DHZETRN while still allowing engagement of various MC codes to verify the solution methods.

In this report, transport code development efforts will be briefly reviewed with an emphasis on the most recent extensions leading to a generalized version of 3DHZETRN applicable in combinatorial geometry. As in the previous studies [Wilson et al. 2014a-c, 2015], convergence tests are performed and comparison to MC simulations are provided. The next step in 3DHZETRN development will allow the use of more complex and realistic geometric models, including human phantoms, so that simple mapping of the present methodology into more realistic applications can be studied. Although a final solution to engineering design problems is not yet at hand, the current status of deterministic methods agrees with MC codes to the degree that various MC codes agree among themselves



in many cases. The main limitation within 3DZHETRAN remains in the nuclear databases and requires additional experimental measurements and nuclear model development.

### 3DZHETRAN

The 3DZHETRAN theoretical formalism has been provided in prior reports [Wilson et al. 2014a-c, 2015] and will not be repeated in detail here. However, an overview is given here to provide clarity in the notation and terminology used later in this paper. Additional discussion is given in this section regarding extensions of the present code to general combinatorial geometry.

#### *Theoretical Formalism Overview*

The linear Boltzmann transport equation within the continuous slowing down approximation for the flux (or fluence) density,  $\phi_j(\mathbf{x}, \boldsymbol{\Omega}, E)$ , of a  $j$  type particle is given by [Wilson et al. 1991, 2005]

$$\mathbf{B}[\phi_j(\mathbf{x}, \boldsymbol{\Omega}, E)] = \sum_k \int_E^\infty \int_{4\pi} \sigma_{jk}(E, E', \boldsymbol{\Omega}, \boldsymbol{\Omega}') \phi_k(\mathbf{x}, \boldsymbol{\Omega}', E') d\boldsymbol{\Omega}' dE', \quad (1)$$

where the differential operator on the left hand side is defined as

$$\mathbf{B}[\phi_j(\mathbf{x}, \boldsymbol{\Omega}, E)] \equiv \boldsymbol{\Omega} \cdot \nabla \phi_j(\mathbf{x}, \boldsymbol{\Omega}, E) - \frac{1}{A_j} \frac{\partial}{\partial E} [S_j(E) \phi_j(\mathbf{x}, \boldsymbol{\Omega}, E)] + \sigma_j(E) \phi_j(\mathbf{x}, \boldsymbol{\Omega}, E). \quad (2)$$

In equations (1) and (2),  $A_j$  is the atomic mass of a type  $j$  particle,  $S_j(E)$  is the stopping power of a type  $j$  ion with kinetic energy  $E$  (vanishes for neutrons),  $\sigma_j(E)$  is the total macroscopic cross section for a type  $j$  particle with kinetic energy  $E$ , and  $\sigma_{jk}(E, E', \boldsymbol{\Omega}, \boldsymbol{\Omega}')$  is the double differential macroscopic production cross section for interactions in which a type  $k$  particle with kinetic energy  $E'$  and direction  $\boldsymbol{\Omega}'$  produce a type  $j$  particle with kinetic energy  $E$  and direction  $\boldsymbol{\Omega}$ .

Solution methods are developed by separating the double differential cross section for neutron ( $j = n$ ) production and the particle fluxes into forward and isotropic components. The forward components are associated mainly with higher energy direct quasi-elastic events and projectile fragmentation products [Wilson 1977, Wilson et al. 1988], and the isotropic components are associated with lower energy secondary particles, including target fragments.

The forward component is first solved within the straight ahead approximation, wherein all particles are assumed to travel along a common axis ( $\boldsymbol{\Omega} \approx \boldsymbol{\Omega}'$ ). This allows previously developed and highly efficient numerical solution techniques to be utilized [Wilson et al. 1991, Slaba et al. 2010a]. The forward solution then gives rise to a source of isotropically produced neutrons, given as

$$\xi_{n,iso}(\mathbf{x}, \boldsymbol{\Omega}, \boldsymbol{\Omega}_0, E) = \sum_k \int_E^\infty \sigma_{nk,iso}(E, E', \boldsymbol{\Omega}, \boldsymbol{\Omega}_0) \phi_{k,for}(\mathbf{x}, \boldsymbol{\Omega}_0, E') dE', \quad (3)$$

where  $\sigma_{nk,iso}(E, E', \boldsymbol{\Omega}, \boldsymbol{\Omega}')$  is the isotropic component of the neutron production cross section, and  $\phi_{k,for}(\mathbf{x}, \boldsymbol{\Omega}, E)$  is the forward component of the flux. The symbol  $\boldsymbol{\Omega}_0$  denotes the direction of the inbound forward flux arriving at location  $\mathbf{x}$ , and  $\boldsymbol{\Omega}$  denotes the transport direction within the geometry along which the isotropic flux is being computed, as in Fig. 1. The transport equation for the isotropic neutron flux is given by

$$[\boldsymbol{\Omega} \cdot \nabla + \sigma_n(E)] \phi_{n,iso}(\mathbf{x}, \boldsymbol{\Omega}, E) = \int_E^\infty \int_{4\pi} \sigma_{nn}(E, E', \boldsymbol{\Omega}, \boldsymbol{\Omega}') \phi_{n,iso}(\mathbf{x}, \boldsymbol{\Omega}', E') d\boldsymbol{\Omega}' dE' + \xi_{n,iso}(\mathbf{x}, \boldsymbol{\Omega}, \boldsymbol{\Omega}_0, E). \quad (4)$$

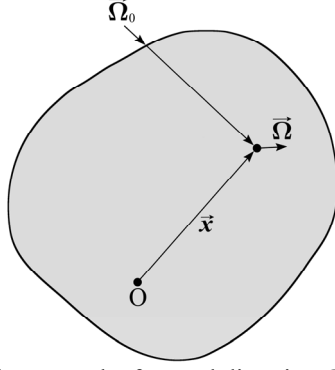


Fig. 1. Geometry depicting relationship between the forward direction  $\Omega_0$  and transport direction  $\Omega$  at location  $x$ .

Equation (4) is solved along the transport direction  $\Omega$  within the bi-directional approximation discussed in detail elsewhere [Slaba et al. 2010b]. A final step in the solution methodology is to compute the source of light ions produced from the lower energy isotropic neutrons. Once this source is computed, the isotropic component of the light ion flux is solved under the assumption that no further nuclear collisions occur, giving partial 3D treatment to low energy charged particles.

A remaining detail in the transport formalism is to define a discrete number,  $N$ , of transport directions,  $\Omega$ , over which the isotropic flux is evaluated. In connecting to historical code development, the  $N = 1$  solution corresponds to the usual straight ahead approximation wherein all particles are assumed to follow a common axis. In this case, there is only one transport direction  $\Omega$ , and  $\Omega = \Omega_0$ . The  $N = 2$  solution corresponds to the bi-directional transport approximation, wherein particles are allowed to propagate either straight forward or straight backward. In this case, there are two transport directions ( $\Omega_1 = \Omega_0$  and  $\Omega_2 = -\Omega_0$ ). Values of  $N > 2$ , correspond to a more detailed three dimensional (3D) description of the isotropic flux component and are the emphasis of recent advances in code development [Wilson et al 2014a-c, 2015]. In those previous studies, values of  $N = 1, 2, 6, 10, 14, 18, 22$  were considered, as shown in Fig. 2.

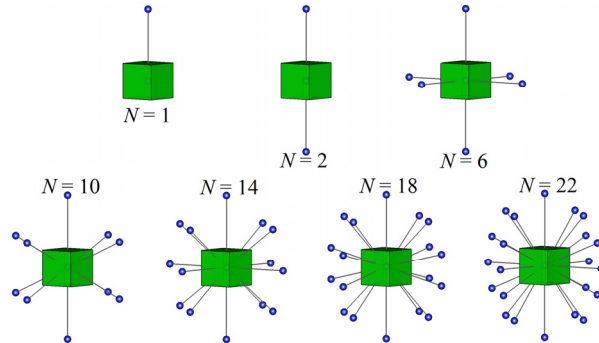


Fig. 2. Transport directions used to describe isotropic component of flux.

These distributions were developed by prescribing a number of latitudinal ( $N_\alpha$ ) and longitudinal ( $N_\beta$ ) directions along with the two polar directions. For the present study, a generalized algorithm for computing the transport direction vectors,  $\Omega$ , was implemented into the code to enable more comprehensive testing in complex geometry, as will be shown in the next section.

The algorithm is described as follows. The number of latitudinal ( $N_\alpha$ ) and longitudinal ( $N_\beta$ ) directions is chosen. This gives the total number of directions

$$N = N_\alpha N_\beta + 2, \quad (5)$$

where the two additional polar directions (forward/backward) have been added. The longitudinal angles ( $\beta_i$ ) and latitudinal angles ( $\alpha_i$ ) are computed as

$$\beta_i = 2\pi \frac{i-1}{N_\beta}, \quad (6)$$

$$\alpha_i = \arccos \left[ a + \frac{\Delta}{2} (2i-1) \right], \quad (7)$$

where  $a = -1 + 2 / N$ ,  $b = 1 - 2 / N$ , and  $\Delta = (b - a) / N_\alpha$ . The directional components are then computed using the typical spherical coordinate transformations

$$\mathbf{\Omega}_i = \begin{pmatrix} \cos(\beta_i) \sin(\alpha_i) \\ \sin(\beta_i) \sin(\alpha_i) \\ \cos(\alpha_i) \end{pmatrix}. \quad (8)$$

In the following section, convergence in the induced radiation field within the ICRU tissue sphere is examined as a function of  $N$ , and transport direction distributions as large as  $N = 86$  are considered.

### *Combinatorial Geometry*

The present work required extensions to 3DZHETRAN to enable general combinatorial geometry to be studied. As a result, an efficient computational ray-tracer was developed and integrated into the code. Fundamentally, the ray-tracer provides the thickness and type of each material traversed in moving from any location in space along an arbitrary direction through the geometry. Such information is required in two places within the 3DZHETRAN formalism (see Fig. 1). First, to evaluate the forward flux along the direction  $\mathbf{\Omega}_0$ , the ray-tracer provides the ordering, material types, and thicknesses traversed in passing from the outermost geometric boundary to the point of interest,  $\mathbf{x}$ . Second, to evaluate the isotropic flux along the transport direction  $\mathbf{\Omega}$  passing through  $\mathbf{x}$ , the ray-tracer is called again to provide similar information.

Solid spheres, boxes, cylinders, and ellipsoids can be easily ray-traced since the equations describing intersection between any ray in space and one of the solids have a closed form analytic solution. Additional geometric and computational complexity is introduced when these simple solids are nested inside each other but must be included as a capability.

The currently implemented ray-tracer allows any number of the simple solids to be nested inside each other, allowing relatively complex geometries to be defined. Partially nested solids (i.e. solids that are not entirely contained by another solid) are not currently supported. Nesting geometric solids is achieved computationally by requiring simple containment (mother-daughter) relationships to be explicitly defined prior to execution. In particular, the definition of each object prior to execution includes a field identifying its immediate mother volume (i.e. the solid that contains it). From this basic information, a complete mother-daughter tree is generated within the code for the ray-tracer upon execution.

The overall procedure of the ray-tracer is described as follows. For a given point and ray-trace direction, intersection distances between the point and the boundaries of each solid in the geometry are computed. If no intersection with a given solid occurs, the evaluated distance is set as a negative number. Next, the list of intersection distances is sorted from smallest to largest. This sets the ordering of objects and materials traversed along the ray. Negative numbers in the list, corresponding to solids that were not intersected, are discarded. The remaining list of intersection distances uniquely defines the ordering, material types, and lengths traversed by the ray and is then passed from the ray-tracer to the transport procedure.

The present status of the ray-tracer allows relatively complex shielding geometries to be efficiently studied within the 3DZHETRAN transport code. Future work will describe implementation of detailed human phantom models into the code. Also, extensions to the ray-tracer to enable compatibility with shielding thickness distributions, as generated in the computer aided design vehicle optimization analyses, are forthcoming. Both of these advancements will provide the final connections between the computationally efficient 3DZHETRAN code to engineering design and radiation risk studies for space applications.





Also of interest is the dose and dose equivalent at locations within the tissue sphere. Dosimetric quantities are evaluated at depths in the tissue sphere at  $z = \{0, 0.007, 0.3, 1, 5, 25, 29, 29.7, 29.993, 30\}$  g/cm<sup>2</sup> with results in Tables 1 and 2 for  $N = 1, 2, 6, 10, 26, 38, 58, 86$ . The doses near the top and bottom of the tissue sphere are seen to converge rapidly with increasing  $N$ . The local fields in these locations are dominated by transport through the aluminum shield giving improved convergence behavior over the case concerning the surface of a homogeneous aluminum shield [Wilson et al. 2014a,b]. The rate of convergence of dose equivalent is somewhat slower, since the details on the penetration of charged particles produced by neutrons are more dependent on angular factors. Still, the rate of convergence is quite rapid in the complex geometry with adequate results in only 20 or more transport directions (see Fig. 5), similar to the spherical shell shield studied in earlier papers [Wilson et al. 2014c,2015].

The solution methodology appears to be nearly converged for  $N > 20$ . This is supported in Tables 1 and 2 by comparing exposure values for different  $N$  at a fixed depth. The relative difference, compared to the  $N = 86$  solution, is found to be less than 1% for dose and less than 2% for dose equivalent for  $N > 10$  at all depths. The induced particle fluence is shown in Fig. 6 at the near ( $z = 0$ ) and distal ( $z = 30$ ) interfaces. Also shown are the lowest order  $N = 1$  and  $N = 2$  solutions, corresponding to the straight ahead and bi-directional approximations, respectively. The  $N = 1$  solution has no contributions from the backward leaking neutrons that have been moderated within the tissue sphere. This can be seen in the incorrect neutron spectral shape below 20 MeV at  $z = 0$ . This error is largely corrected by the  $N = 2$  bi-directional approximation. All solutions are nearly converged for  $N > 10$  (i.e. within fractions of a percent of the  $N = 86$  result).

Table 1. Webber SPE dose as a function of number of transport directions,  $N$ , at various depths in the tissue sphere including those defined by ICRU.

$z$ (g/cm <sup>2</sup> )	Dose (cGy/event)							
	$N = 1$	$N = 2$	$N = 6$	$N = 10$	$N = 26$	$N = 38$	$N = 58$	$N = 86$
0	42.76	42.78	42.76	42.80	42.79	42.79	42.78	42.78
0.007	42.46	42.48	42.47	42.49	42.49	42.48	42.48	42.48
0.3	38.68	38.76	38.74	38.76	38.75	38.75	38.74	38.75
1	32.32	32.40	32.38	32.40	32.39	32.38	32.38	32.38
5	14.56	14.61	14.59	14.61	14.59	14.59	14.59	14.59
25	1.55	1.55	1.54	1.54	1.55	1.54	1.55	1.54
29	1.13	1.13	1.13	1.12	1.13	1.13	1.13	1.13
29.7	1.08	1.07	1.08	1.06	1.07	1.07	1.07	1.07
29.993	1.05	1.05	1.05	1.04	1.05	1.05	1.05	1.05
30	1.05	1.05	1.03	1.03	1.04	1.04	1.04	1.04

Table 2. Webber SPE dose equivalent as a function of number of transport directions,  $N$ , at various depths in the tissue sphere including those defined by the ICRU.

$z$ (g/cm <sup>2</sup> )	Dose Equivalent (cSv/event)							
	$N = 1$	$N = 2$	$N = 6$	$N = 10$	$N = 26$	$N = 38$	$N = 58$	$N = 86$
0	65.90	65.99	65.69	66.08	65.99	65.94	65.86	65.90
0.007	62.51	62.56	62.37	62.62	62.51	62.44	62.41	62.45
0.3	54.92	55.49	55.26	55.47	55.36	55.28	55.26	55.31
1	45.73	46.27	46.06	46.24	46.15	46.06	46.04	46.09
5	20.68	21.03	20.81	20.94	20.81	20.76	20.78	20.82
25	2.64	2.63	2.56	2.47	2.59	2.57	2.58	2.57
29	2.03	2.00	2.04	1.90	2.04	2.02	2.05	2.05
29.7	1.95	1.91	2.00	1.83	1.98	1.96	1.99	1.99
29.993	1.91	1.86	1.99	1.79	1.94	1.91	1.96	1.95
30	1.91	1.84	1.80	1.74	1.85	1.83	1.84	1.84

The fluence spectra in the neighborhood of the near and distal interface are shown in Fig. 7 for  $N = 26$ . A rapid transition occurs in passing from aluminum to tissue in the near interface and in passing from tissue to aluminum in the distal interface. This can be seen in the proton and <sup>4</sup>He spectra in Fig. 7 below 10 MeV/n. The <sup>4</sup>He fluence spectra are shown in the neighborhood of the near and distal interfaces on an expanded scale in Fig. 8. The

$^4\text{He}$  ions produced in the aluminum shield rapidly form a new equilibrium spectrum within the first few millimeters of tissue as observed in the near interface. Similarly, at the distal interface, the leakage of  $^4\text{He}$  from the aluminum into the tissue shield quickly forms a new, less dynamic, approach to an equilibrium spectrum within the first few millimeters of tissue.

One difference for the present complex inhomogeneous geometry compared to the tissue sphere in close contact with the aluminum spherical shell [Wilson et al. 2014c, 2015] is that the aluminum surface in the present case is exposed to the secondary light ions over a restricted solid angle whereas the spherical shell configuration is over the full hemisphere. This results in some differences in behavior in the transition region. This is seen most clearly by comparing the present result in Fig. 8 with the results derived previously for the inhomogeneous sphere [Wilson et al. 2014c, 2015].

It is found that the details of the  $^4\text{He}$  spectra (for example, see Fig. 8) cannot be verified by MC simulations since the computational costs required to control statistical fluctuations at low energies are too large. Even the hope of defining the transition regions for neutrons and protons has not been successful in MC simulations. Biasing techniques could be implemented to resolve these issues in future work. As a result, the larger features generated from MC simulations are used to verify the 3DHZETRAN results. If the trends in the 3DHZETRAN solution over larger distances are verified, then it is reasonably assumed that the interface details revealed by 3DHZETRAN are reasonably correct in the context of the current interaction models. The  $N = 26$  will be used in the MC benchmarks discussed in the next section.

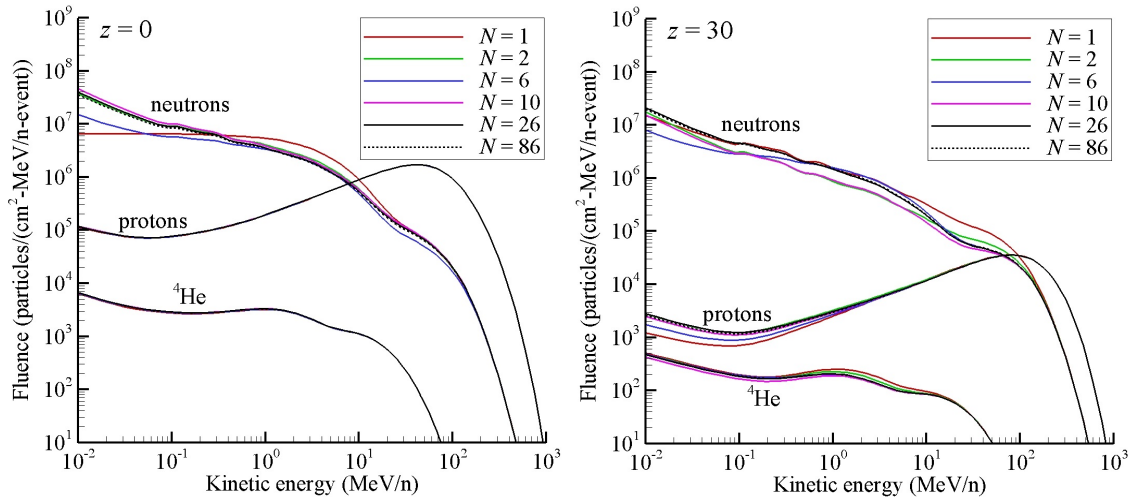


Fig. 6. Webber SPE convergence test at the top (left plot) and bottom (right plot) of a 30 g/cm<sup>2</sup> diameter tissue sphere within a complex shield of aluminum.

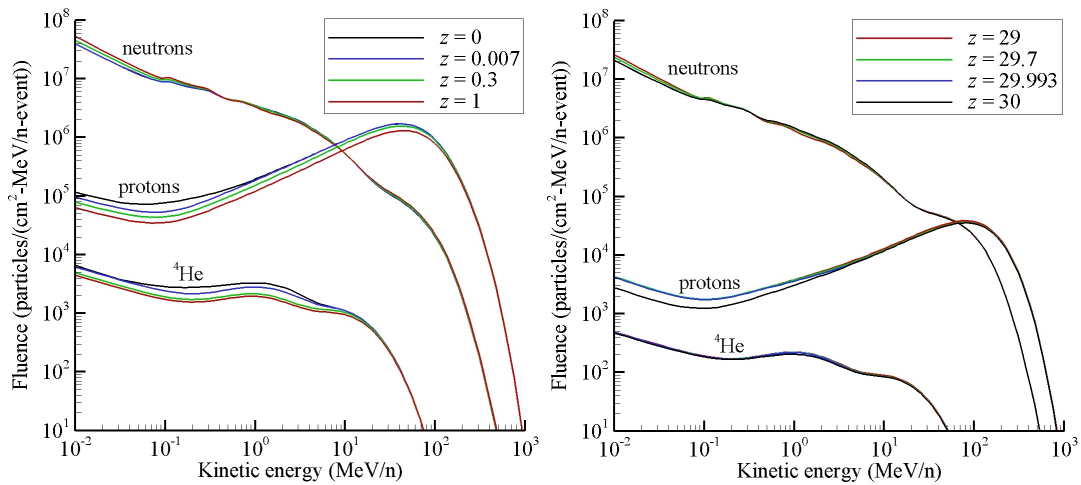


Fig. 7. Webber SPE induced fluence within the ICRU sphere at locations near the top (left plot) and bottom (right plot) tissue/shield interface with  $N = 26$ .



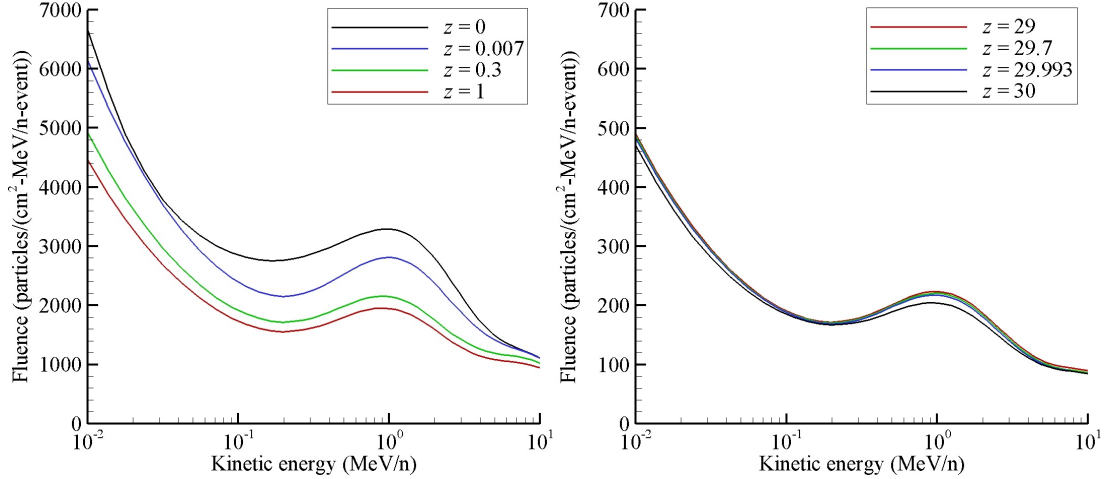


Fig. 8. Webber SPE induced  ${}^4\text{He}$  fluence within the ICRU sphere at locations near the top (left plot) and bottom (right plot) tissue shield interface with  $N = 26$ .

### Monte Carlo Benchmarks

Using the external source and geometry defined in Fig. 3, the induced neutron and proton fluence spectra were evaluated at detector locations within the ICRU sphere by three MC codes (Geant4 [Agostinelli et al. 2003], FLUKA [Fasso et al. 2005, Battistoni et al. 2007], and PHITS [Sato et al. 2006, 2013]) and 3DZHETRAN. Results are shown in Fig 9. The scoring regions (detectors) and physics options used in this set of simulations are identical to what was used in Wilson et al. [2014c, 2015] and will not be repeated here.

The proton fluence predictions among the three codes are in reasonable agreement above 1 MeV with very large statistical uncertainty below 1 MeV (not shown). Some of the differences in proton spectra at  $z = 30$  may be associated with the simplified assumptions of the straight ahead approximation in 3DZHETRAN light ion transport. The larger discrepancy lies with the neutron spectra, where disagreement among the MC results brackets the 3DZHETRAN solution. The FLUKA and 3DZHETRAN results exhibit a similar inflection in the neutron spectrum near 10 to 60 MeV that may be related to the use of an early FLUKA approximation to the secondary neutron spectrum used in HZETRAN [Ranft 1980, Wilson et al. 1988] and carried over into 3DZHETRAN.

To further quantify differences among the codes, the neutron spectra are converted into effective dose using conversion factors for isotropic neutrons evaluated by Pelliccioni [2000] using FLUKA. The effective dose on the top and bottom of the tissue sphere is given in Table 3. The 3DZHETRAN ( $N = 26$ ) compares well with the three MC codes, and is within 5% of the PHITS results. The older HZETRAN ( $N = 1$ ) provides a conservative overestimate as expected. An added measure of degree of agreement is to evaluate the relative root mean square (RMS) differences in the neutron fluence from the four codes as given in Table 4 on the top and the bottom of the ICRU sphere. Again, it is seen that the agreement of 3DZHETRAN with the MC codes is about the same as the agreement of the MC codes among themselves.

A principle difference in the three codes is the computational efficiency. The time required by the three codes to run these benchmarks is given in CPU seconds used and listed in the first column of Table 5. Although it is difficult to favor one code over another on the basis of the veracity of the solutions obtained, there are vast differences in computational time required to evaluate fluence spectra even in this simplest of complex geometries (tissue sphere within a complex shield of a single elemental material). Still, Monte Carlo methods provide an important verification for developing codes capable of meeting operational and especially design requirements. Computational speed has proven to be important in spaceflight validation in low Earth orbit (LEO) where the time structure of the environment can be used to test various environmental components as was done using Liulin instrument measurements onboard the International Space Station (ISS) [Wilson et al. 2007, Slaba et al. 2013]. The main limitation on such studies remain the uncertainty in the environmental models (especially for the trapped environment) and uncertainty in nuclear cross sections.



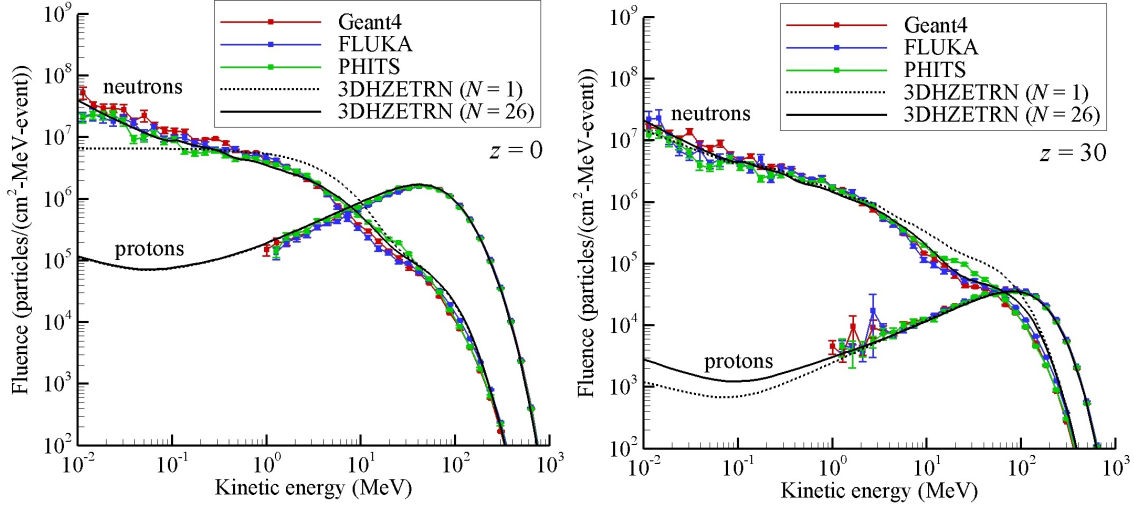


Fig. 9. Webber SPE benchmark with  $N = 26$  compared with Geant4, FLUKA, and PHITS at detector locations near the top (left plot) and bottom (right plot) of the ICRU tissue sphere.

Table 3. Neutron effective dose values (mSv/event) at  $z = 0$  g/cm<sup>2</sup> (top of ICRU sphere) and  $z = 30$  g/cm<sup>2</sup> (bottom of ICRU sphere). Propagated MC statistical errors in neutron effective dose values were all less than 2%.

$z$ (g/cm <sup>2</sup> )	3DZHETRAN ( $N = 1$ )	3DZHETRAN ( $N = 26$ )	Geant4	FLUKA	PHITS
0	10.31	6.98	5.68	5.68	6.92
30	5.44	3.50	2.77	2.96	3.29

Table 4. Neutron fluence root mean square relative differences of 3DZHETRAN ( $N = 26$ ) and MC codes at  $z = 0$  g/cm<sup>2</sup> (top of ICRU tissue sphere) and  $z = 30$  g/cm<sup>2</sup> (bottom of ICRU sphere). Dimensionless units.

$z$ (g/cm <sup>2</sup> )	vs Geant4	vs FLUKA	vs PHITS	MC spread
0	0.468	0.308	0.269	0.676
30	0.433	0.327	0.339	0.674

Table 5. Total CPU seconds required for benchmark calculations. Total number of histories ran in Monte Carlo simulations are shown in parentheses.

	Webber SPE
3DZHETRAN ( $N = 26$ )	59
Geant4	$2.0 \times 10^8$ ( $3.5 \times 10^{11}$ )
FLUKA	$5.1 \times 10^8$ ( $3.9 \times 10^{11}$ )
PHITS	$9.6 \times 10^7$ ( $1.4 \times 10^{11}$ )

## Conclusions

In this work, 3DZHETRAN was extended to enable analysis of general combinatorial geometry. The extensions were tested by considering a cylindrical aluminum shell surrounding internal aluminum boxes and an ICRU tissue sphere. The internal boxes were positioned relative to the external source to provide only partial shielding of the ICRU sphere, thereby emphasizing 3D transport effects. Following the outline of previous studies [Wilson et al. 2014a-c, 2015], convergence tests were performed to determine the solution dependence on the number of transport directions,  $N$ . It was found that  $N = 26$  provided nearly converged results with minimal relative error compared to the  $N = 86$  solution.

Comparisons between 3DZHETRAN and the MC codes, Geant4, FLUKA, and PHITS, were made at points within the geometry exposed to the Webber 1956 SPE. As in the previous studies [Wilson et al. 2014a-c, 2015], it was found that 3DZHETRAN agrees well with MC codes. Most importantly, even within the complex geometry,

3DHZETRN was several orders of magnitude faster than the MC simulations. Future work will provide yet another extension to the 3DHZETRN geometry capabilities by enabling analysis through complex and realistic geometry described by only a single ray-trace thickness distribution. Such geometric descriptions are typically generated in the vehicle design and optimization process [Wilson et al. 2003, Walker et al. 2013], where detailed computer aided design models are maintained and developed [Qualls et al. 2001, Simon et al. 2014]. This extension is the critical step in connecting and integrating 3DHZETRN into shield optimization frameworks.

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**REPORT DOCUMENTATION PAGE**

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<b>14. ABSTRACT</b> The 3DHZETRN code, with improved neutron and light ion ( $Z < 2$ ) transport procedures, was recently developed and compared to Monte Carlo (MC) simulations using simplified spherical geometries. It was shown that 3DHZETRN agrees with the MC codes to the extent they agree with each other. In the present report, the 3DHZETRN code is extended to enable analysis in general combinatorial geometry. A more complex shielding structure with internal parts surrounding a tissue sphere is considered and compared against MC simulations. It is shown that even in the more complex geometry, 3DHZETRN agrees well with the MC codes and maintains a high degree of computational efficiency.					
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