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Rational design of metal nitride redox materials for solar-driven ammonia synthesis

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Abstract

Fixed nitrogen is an essential chemical building block for plant and animal protein, which makes ammonia (NH₃) a central component of synthetic fertilizer for the global production of food and biofuels. A global project on artificial photosynthesis may foster the development of production technologies for renewable NH₃ fertilizer, hydrogen carrier and combustion fuel. This article presents an alternative path for the production of NH₃ from nitrogen, water, and solar energy. The process is based on a thermochemical redox cycle driven by concentrated solar process heat at 700-1200°C that yields NH₃ via the oxidation of a metal nitride with water. The metal nitride is recycled via solar-driven reduction of the oxidized redox material with nitrogen at atmospheric pressure. We employ electronic structure theory for the rational high-throughput design of novel metal nitride redox materials and to show how transition-metal doping controls the formation and consumption of nitrogen vacancies in metal nitrides. We confirm experimentally that iron doping of manganese nitride increases the concentration of nitrogen vacancies compared to no doping. The experiments are rationalized through the average energy of the dopant d-states, a descriptor for the theory-based design of advanced metal nitride redox materials to produce sustainable solar thermochemical ammonia.

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Keywords

Concentrated solar energy, Thermochemical redox cycle, Metal nitride, Hydrogen storage, Haber Bosch, Density functional theory
1. Introduction

Renewable chemical fuels, such as hydrocarbons, methanol, hydrogen and ammonia may be synthesized from CO₂, H₂O and N₂ by solar-driven photochemical, [1],[2] electrocatalytic, [3],[4] or thermochemical processes [5]. The latter approach utilizes the entire spectrum of concentrated solar energy as the source of high-temperature process heat, and as such provides a thermodynamically favorable path to solar fuels and materials production with high energy conversion efficiencies. A promising example is the production of syngas by thermochemically splitting CO₂ and H₂O via a metal oxide redox cycle [6] (and references cited therein).

Natural photosynthesis relies on structures – proteins – that are built with fixed nitrogen, such as ammonia (NH₃). Both, sugar, a major product of natural photosynthesis, and protein are the central components of the global food and biofuel production. In turn, synthetic ammonia is one of the major products of the chemical industry [7] that is mainly used as a fertilizer [8]. Additionally, NH₃ is an energy carrier formed via reduction of N₂, analogously to the products of photosynthesis, such as CO and hydrocarbon fuels via reduction of CO₂ and splitting of H₂O. Thus, NH₃ may find application as hydrogen carrier [9],[10] and as a fuel for alkaline fuel cells [11],[12] and in internal combustion engines [13],[14],[15]. Currently, NH₃ is produced industrially from N₂ and H₂ via the catalytic Haber-Bosch process at up to 300 bar and 400-500°C [7],[16],[17],[18],[19]. The overall process is characterized by the high energy consumption associated with the production of the reactants. Usually, H₂ is obtained by steam-reforming of natural gas, while N₂ is obtained by cryogenic separation from air. Both of these processes require a major input of energy, either in the form of heat or electricity, and consequently cause a significant concomitant pollution derived from the combustion of fossil fuels for heat and electricity generation. The total energy requirement is in the range 28-166 GJ/t NH₃ [7],[16]. Furthermore, the severe process conditions require sophisticated high-pressure and high-temperature machinery that is operated in large-scale centralized plants producing typically 1,000-3,000 t NH₃ day⁻¹ [7],[18].

To convert the nearly inert N₂ molecule into a reactive chemical, Haber’s early studies [20] examined the formation of NH₃ from H₂ and various metal nitrides. These studies were motivated by the temporary formation of NH₃ at low pressures from an iron nitride contamination of the catalyst that Ostwald used [21]. The NH₃ formation ceased quickly since the spent iron nitride could not be regenerated with N₂ at low pressure and the work spurred the development of the
Haber-Bosch process, in which NH$_3$ is formed at high pressure to shift the thermodynamic equilibrium [20]. Current metal nitrides for the production of complex nitrogen-containing molecules cannot be regenerated with 1 bar N$_2$ [22]. Examples are Ni$_3$N, Cu$_3$N, Zn$_3$N$_2$ and Ta$_3$N$_5$, which liberate 30, 25, 23, and 13 mol% of their lattice nitrogen in form of NH$_3$ when reacted with H$_2$ at 250, 250, 400, and 700°C, respectively [23]. Certain metal nitrides have been studied as low-pressure NH$_3$ synthesis catalyst [24],[25] and some ternary metal nitrides have been found to reversibly reduce N$_2$ at low pressure and to liberate the fixed nitrogen in form of NH$_3$ in a second step, when reacted with H$_2$ [26],[27],[28]. A typical example of such a material is Co$_3$Mo$_3$N that yields Co$_6$Mo$_6$N and up to 8 mol% of its lattice nitrogen in form of NH$_3$ when reacted for 60 min with H$_2$ at 400°C [28]. To increase the NH$_3$ yield, current materials development focuses on increasing the amount of nitrogen stored in the metal nitride and on increasing the fraction of the lattice nitrogen that yields NH$_3$ [22].

This paper focuses on materials development for a solar-driven ammonia synthesis from N$_2$ and H$_2$O (instead of H$_2$) that – in contrast to the Haber-Bosch process – does not require fossil fuels, electricity, or high-pressure operations [29],[30],[31]. In a first step, NH$_3$ is formed at 1 bar and below 200-500°C via the oxidation of a solid metal nitride redox material with steam [32],[33]. The oxidized redox material is subsequently regenerated in an endothermic step driven by concentrated solar process heat at up to 1200°C with a stream of N$_2$ with or without a gaseous chemical reducing agent [29],[30],[31]. The reaction stoichiometry of this redox cycle is given with Supporting Information (SI). While this process has been demonstrated successfully with Al-based redox materials, [34],[35],[36] the fixation of N$_2$ with Al$_2$O$_3$ requires a carbonaceous reducing agent and technically-challenging temperatures above 1700°C. [30],[36],[37]. Certain transition-metal redox materials such as Cr-based nitrides have been shown to circumvent the need for a solid reducing agent and allow to regenerate the nitride below 1500°C, but at the expense of lower extents of the nitrogen fixation and ammonia evolution [29],[30],[31].

Only few metals accomplish the trade-off between thermodynamically stable formation of a metal nitride from N$_2$ that gives NH$_3$ upon hydrolysis [30],[32],[33] and formation of only intermediately stable metal oxides that can be recycled at moderate process conditions [29],[30]. This is in analogy to the Sabatier principle in heterogeneous catalysis [38] that describes the ideal catalytic activity of a material as function of an intermediately strong bond formed between the catalyst surface and key reaction-intermediates [19],[25]. As a starting point, we have chosen Mo and Mn as primary metals for the development of advanced metal nitride redox materials.
However, while both metals exhibit promising characteristics, Mo binds nitrogen slightly too weak leading to relatively low nitride and NH$_3$ yields [30],[32] and Mn binds nitrogen somewhat too strong leading to the formation of relatively stable metal oxides due to the correlated stability of metal nitrides and metal oxides [39].

Here, we employ electronic structure computations to show how the bonding of nitrogen in the solid state can be controlled via doping with transition metals. Such novel theory-assisted design is analogous to the rational design of metal oxide redox materials [40],[41],[42], where reactivity is controlled by the oxygen vacancy formation energy [40],[41]. To verify the concept, we experimentally demonstrate controlling nitrogen vacancy formation in manganese based redox materials. Finally, we rationalize the trends in the Gibbs free energy of the nitrogen vacancy formation with the charge density distribution in the ternary metal nitrides and the d-band center, a quantitative descriptor for the theory-based design of advanced metal nitride redox materials for sustainable solar-derived ammonia.

This work is at the interface of fundamental physical science of redox materials on one hand, and chemical engineering to store solar energy as ammonia. The ultimate vision of this work is a device that converts nitrogen from air, water and sunlight, at ambient pressure and without electricity, into ammonia and oxygen. Such a device would facilitate the production of NH$_3$ fuel, as an alternative to carbon-based fuels derived from solar-driven CO$_2$ and H$_2$O splitting. Ammonia fertilizer for food and biofuels could be produced without the infrastructure for supplying natural gas or coal and the know-how and technology for the high-pressure operations employed globally for the production of synthetic NH$_3$. A global project on artificial photosynthesis, as it is contemplated in this themed issue, [43],[44] could raise the public profile of this field and may assist in funding the development of solar-derived NH$_3$ through governmental, private, and corporate contributions. Although solar-derived NH$_3$ may be economically more attractive in certain geographically, economically, or politically isolated regions than NH$_3$ from large-scale Haber-Bosch plants, accounting for ethical implications, such as diminished environmental impacts when avoiding the dependence on fossil fuel feedstock, may make solar-derived NH$_3$ economically competitive with NH$_3$ from Haber-Bosch plants. In this sense, solar-driven N$_2$ reduction is equivalent to solar-driven CO$_2$ reduction and H$_2$O splitting, the central reactions of “synthetic photosynthesis” for an efficient production of solar fuel and food as well as acquisition of knowledge: Ethically, they are common heritage of humanity and should not be fully owned by profit-focused private interests. The mild process
conditions of solar-derived ammonia will allow implementation in parts of the world that may lack the infrastructure for a highly complex high pressure catalytic process like the Haber-Bosch based approach to ammonia. Ideally, global synthetic photosynthesis should be held on trust for humanity and its ecosystems and should be employed through a politically and economically neutral agency [44]. As verbalized at the Royal Society’s meeting discussing a global artificial photosynthesis project at Chicheley Hall in 2014: “Our goal is to work cooperatively and with respect for basic ethical principles to produce the scientific breakthroughs that allow development and deployment of an affordable, equitably accessed, economically and environmentally sustainable, non-polluting global energy and food system that also contributes positively to our biosphere.”

2. Methods and Materials

2.1 Thermochemical equilibrium calculations

To quantify the potential of binary transition-metal nitride redox materials for a solar-driven ammonia synthesis, the thermochemical equilibrium of the redox cycle was analyzed for Mo- and Mn-based bulk metal nitrides at 1 bar and as a function of temperature from tabulated free energy data [39]. We note negative free energy differences mark exergonic reactions.

2.2 Electronic structure calculations

To quantify the effect of doping on the nitrogen vacancy formation energetics in transition-metal nitrides, cubic γ-Mo2N and hexagonal ζ-Mn2N were modeled via density functional theory (DFT), performed with the Grid-based projector-augmented wave (GPAW) code [45],[46]. Exchange-correlation interactions were treated by the revised Perdew-Burke-Ernzerhof (RPBE) functional of Hammer, Hansen, and Nørskov [47] and atomic configurations were handled in the Atomic Simulation Environment (ASE) [48],[49]. Mo2N and Mn2N were modeled with four and eight metal atoms, respectively, and the stoichiometric amount of nitrogen occupying half of the octahedral interstitial sites. The bulk structures had periodic boundary conditions in all directions and were modeled with a k-point sampling of 4x4x4. The corresponding D0.5Mo1.5N and D0.25Mn1.75N ternary metal nitride models were created via replacing one of the parent metal atoms in each model with a dopant, D = Sc, Ti, V, Cr, Mo, Mn, Fe, Co, Ni, Cu or Zn, where all compositions containing Mn, Fe, Co, or Ni were modeled with spin-polarized calculations. The free energy of forming nitrogen vacancies in the bulk was determined as the difference in the total electronic energy of the metal nitride with nitrogen vacancies (50% and 25% relative to the
stoichiometric composition of Mo$_2$N and Mn$_2$N, respectively) and the stoichiometric metal nitride plus the chemical potential of N$_2$ in the gas phase. The value was converted to free energy at 25°C and 1 bar using standard statistical mechanical equations evaluated through ASE. The partial charge density was determined for all metal nitride models via Bader decomposition [50]. Computational details are given with SI.

2.3 N$_2$ reduction

The effect of doping Mo- and Mn-based redox materials with Cr and Fe on the stability of the metal nitrides formed by Mo and Mn, respectively, was studied by reacting approximately 0.75-2.00 g Cr, Mn, Fe, Mo, or equimolar Mo/Cr and Mn/Fe metal powder mixtures with N$_2$. The metal powder was placed into a quartz boat and heated with a tube furnace (HTF55347C furnace, CC58434C temperature controller, Lindberg/Blue) for 0.5, 5, 10, 30, and 120 min (all samples) and 60, 90, and 240 min (samples containing Mn) at 750°C in 1.86 L(STP) N$_2$ min$^{-1}$ (all samples) and 1.86 L(STP) N$_2$ min$^{-1}$ diluted with 0.47 L(STP) H$_2$ min$^{-1}$ (samples containing Mo or Cr). All metals (99.8% pure Cr, 99.9% Mn, 99.9% Fe, and 99.95% Mo, from Noah Technologies, minor impurity levels are specified with SI) were -325 mesh and had comparable average particle diameters and specific BET surface areas, as shown with SI. All gases were of UHP Zero grade (Linweld). This article discusses the data for the N$_2$ reduction with Mn, Fe, and Mn/Fe, while the data for Mo, Cr, and Mo/Cr is given with SI.

2.4 Solid-state analysis

The composition of the solids was quantified via powder X-ray diffraction (XRD) using a MiniFlex II diffractometer (5-80 °2θ range, Cu-target X-ray tube, 30 kV / 15 mA output, diffracted beam monochromator, Rigaku). Scanning electron microscopy (SEM) was used (S-3500N Scanning Electron Microscope, Hitachi, 20 kV) to determine the average particle diameter and energy-dispersive X-ray spectroscopy (EDS, Nova NanoSEM 430, FEI Company, 5-15 kV, beam deceleration, high stability Schottky field emission gun, and Oxford X-Max Large Area Analytical silicon drift detector) was used to map the distribution of metal dopant and nitrogen at the surface. All reactants and products were weighed (AE260 DeltaRange balance, Mettler) and the specific BET surface area was analyzed by NanoScale Inc., Manhattan, KS.
3. Results and Discussion

3.1 Controlling the nitrogen vacancy formation in transition-metal nitrides

To drive a two-step ammonia synthesis with concentrated solar energy and to facilitate the use of water as hydrogen source for the NH₃ evolution, this section outlines the process conditions of a solar-thermochemical ammonia synthesis with metal nitride redox materials. We start our analysis with thermochemical equilibrium calculations for Mn₅N₂ and Mo₂N, metal nitrides that facilitate the trade-off between high NH₃ yields on one side and high N₂ reduction yields on the other side. Thereafter we establish a rationale for how to further improve this trade-off via doping metal nitrides with transition metals.

Figure 1A shows the thermodynamic equilibrium for the oxidation of Mn₅N₂ with water at 1 bar yielding MnO, NH₃ and the balance H₂. As indicated with the shaded area, the reaction is exergonic – that is thermodynamically favoring the formation of the reaction products – over the entire examined temperature range. We note forming NH₃ at elevated temperatures and 1 bar requires the need to quickly remove NH₃ from the reactor to thereby avoid its decomposition into N₂ and H₂ above 180°C at thermodynamic equilibrium [20],[30]. The oxygen can be abstracted from the formed MnO in a second step above 1230°C (below the melting point of Mn) using by-produced H₂ as reducing agent and ensuring that the partial pressure of water, pH₂O, is below 1.5 × 10⁻⁴ bar. This endothermic reaction can be driven with concentrated solar radiation and stores the chemical potential in the redox material that is employed for the subsequent reduction of N₂ at 1 bar yielding Mn₅N₂ below 1060°C. Figure 1B shows that the composition of the metal nitride allows to alter these reaction conditions: with Mo₂N the NH₃ evolution and the N₂ reduction are both limited at 1 bar to temperatures below 640°C and 700°C, respectively. However, the reduction of the formed MoO₂ can be achieved more facile with CO as reducing agent (e.g., from gasified biomass) at above 730°C and below 4.0 × 10⁻¹ bar pCO₂. We note the ideal temperature for the reduction of MoO₂ with CO depends also on the vapor pressure of the molybdenum oxides that are formed during the NH₃ evolution and the tendency for undesirable carbon deposition in the reactor.

The ideal metal nitride composition would confer thermochemical properties to the redox material for a solar-driven NH₃ synthesis that lie between those of Mn₅N₂ and Mo₂N. Ideally, the metal nitride should be slightly more stable than Mo₂N – to fix more nitrogen above 700°C – while the metal oxide should be less stable than MnO – to avoid the need for temperatures above
1200°C and the means to establish low partial pressures of H₂ or CO₂, respectively. Similar to the possibility to control the adsorption energy of adsorbates at surfaces by altering the surface composition, [19],[19],[25],[38] doping bulk metal nitrides with transition metals may diminish or augment the formation of the metal nitride [51]. However, no rationale exists yet that describes how to compose metal nitrides to control the stability of the lattice nitrogen.

To establish trends in the effect of doping transition-metal nitrides on the bonding of the lattice nitrogen, we compute the free energy of the nitrogen vacancy formation across 22 metal nitride compositions. We hypothesize, negative free energies of the nitrogen vacancy formation correlate with metal nitride compositions that spontaneously liberate lattice nitrogen (in from of NH₃ if a hydrogen source such as H₂ or H₂O is present) and that less readily form lattice nitrogen from N₂, and vice versa. Figure 2 plots the free energy of the nitrogen vacancy formation in Mn₂N bulk (i.e., the ζ-phase manganese nitride with a broad stoichiometry that includes Mn₅N₂ and Mn₆N₂.58) [52] doped with a 3d transition metal or Mo vs. the number of d-electrons in the ground state of the dopant. The figure shows that all tested dopants decrease the stability of the lattice nitrogen, relative to the value for un-doped Mn₂N, which is shown with a solid line. As a general trend, a high occupancy of the dopant d-states correlates with a high un-stability of the lattice nitrogen. In other words, filling the metal d-states of the metal nitride decreases the bonding strength of the lattice nitrogen. We note Zn₀.25Mn₁.75N shows the largest deviation from this trend, which is discussed in Section 3.3. Figure 3 shows the equivalent analysis for Mo₂N. The steeper slope of the linear correlation for Mo₂N, i.e., -0.162 eV for Mo₂N vs. -0.072 eV for Mn₂N, suggests that the stability of the lattice nitrogen in doped Mo₂N is significantly more sensitive to the occupancy of the d-states than the stability of the lattice nitrogen in doped Mn₂N.

In summary, the formation and consumption of nitrogen vacancies in transition-metal nitrides can be controlled with the occupancy of the metal d-states. Aiming at the design of metal nitride redox materials, we suggest the relative strong binding of nitrogen in Mn₂N may be diminished via doping with metals such as Fe while the relative weak binding of nitrogen in Mo₂N may be augmented via doping with metals such as Cr.

**3.2 N₂ reduction with Fe-doped Mn**

The test the predicted weakening of the nitrogen bonding in manganese nitride when doping with late transition metals, this section evaluates trends in the formation of manganese nitrides and iron nitrides from manganese, iron, an equimolar mixture of both metals and N₂ at 1 bar and
Figure 4A shows the formation of ε-Mn₄N and ζ-Mn₆N₂.₅₈ (which is equivalent to Mn₅N₂ and Mn₂N discussed in Section 3.1) [52] as a function of time. Mn fixes N₂ quickly, yielding about 85 mol% Mn₄N after 30 min. Thereafter, the yield of Mn₄N decreases while the yield of the additional Mn₆N₂.₅₈ phase increases to 85 mol% Mn₆N₂.₅₈ after 240 min, indicating that the nitride with increased nitrogen content is formed via nitridation of the nitride with lower nitrogen content. We note the formation of these two manganese nitride phases is as predicted by the Mn-N phase diagram, [53] while the η and θ phases with higher nitrogen content [52] are unstable at 750°C [53]. Furthermore, the transformation of the ε phase via nitridation into the ζ phase is expected [53] and analogous to the formation of related interstitial nitrides, such as CrN from Cr₂N [29]. Details on the crystal phases and physical characteristics of the redox materials are given with Table S1 (SI). In the presence of Fe, as shown with Figure 4B, the quick formation of Mn₄N levels after 30 min at approximately 64 mol% and the subsequent formation of Mn₆N₂.₅₈ reaches only 29 mol% after 240 min. That is, Mn fixes about 0.24-0.28 mol nitrogen per mol Mn after 60-240 min in the presence of Fe, which is about 66-74% of 0.32-0.40 mol nitrogen fixed per mol Mn in the absence of Fe. This indicates that Fe destabilizes the lattice nitrogen in manganese nitrides. Assessing whether or not the dopant affects the diffusion kinetics of the nitrogen vacancies as well requires further studies.

While Fe appears to destabilize the bond that is formed between Mn and the lattice nitrogen, Mn stabilizes the formation iron nitrides that are thermodynamically unstable in the absence of Mn, as shown with Figure 5. As expected, [39] Fe does not reduce N₂ at 1 bar and 750°C. However, in the presence of Mn some nitrogen appears to intercalate into the Fe lattice yielding up to 54 mol% of a cubic FeN₀.₀₃₂₄ phase after 240 min. In conclusion, iron appears to diminish the formation of manganese nitrides – as predicted with Figure 2 – while manganese augments the formation of iron nitrides – in agreement with the lower occupancy of the d-states in Mn vs. Fe, as discussed in Section 3.1.

We note while the preparation and cycling of ternary metal nitrides [26],[27],[28] or nanocomposites would provide the possibility to quantify the effect of the dopant on the bond energy of the lattice nitrogen, the discussed data for metal powders and metal powder mixtures confirms the trends in the stability of transition-metal nitrides predicted via electronic structure theory. To visualize the morphology of the metal nitrides employed in this work, Figure 6 shows SEM images of cubic Mn₄N (up to 84.6 mol%), mostly cubic Mo and tetragonal Mo₂N (up to 21.1
mol%) and a powder mixture of mostly trigonal Cr$_2$N, cubic Mo and some cubic CrN and tetragonal Mo$_2$N. Details are given with SI. The X-ray emission map of the metal powder mixture shows that the parent metal, Mo, and the metal dopant, Cr, are closely located in some regions. We suggest that these are the domains where the bonding of the lattice nitrogen is affected by both metals, while in other domains of the metal mixture the bonding of nitrogen is dominated by the presence of one metal only. We note while Cr increases the fraction of nitrogen fixed by Mo, as shown with Figure S2 (SI), the amount of nitrogen fixed by Mo is still below that fixed by Cr, as shown in Figure 6C by the inhomogeneous distribution of nitrogen mostly located with Cr. The Cr dopant appears to support the nitridation of Mo with N$_2$ into Mo$_2$N, presumably due to reduction of molybdenum oxides at the surface (discussed with SI) and due to stronger binding of the lattice nitrogen (such as discussed above for the formation of iron nitrides).

From a practical perspective, an optimized metal nitride redox material should provide a high specific surface area for the formation and consumption of nitrogen vacancies, either via a porous structure [54], similar to the structure of advanced metal oxide redox materials [55], or in form of a porous particle bed [56]. As a starting point we have computed the apparent nitrogen diffusion constants at 750°C (see details in the SI) with $7.77 \times 10^{-9}$ cm$^2$ s$^{-1}$ for the formation of Mn$_6$N$_{2.58}$ and $3.07 \times 10^{-11}$ cm$^2$ s$^{-1}$ for the formation of Mo$_2$N. These values compare well with those reported previously, i.e., $3.07 \times 10^{-9}$ cm$^2$ s$^{-1}$ for the ζ-manganese nitride phase at 890°C [57] and $5 \times 10^{-9}$ to $3 \times 10^{-14}$ cm$^2$ s$^{-1}$ for Mo$_2$N at 600-750°C [58],[59]. Comparing these values for a presumably interstitial nitrogen diffusion process [58] to the diffusion constants for nitrogen vacancy diffusion in good anion conductors, such as $2 \times 10^{-11}$ cm$^2$ s$^{-1}$ at 700°C in nitrogen-doped yttria-stabilized zirconia, [60] indicates that transition-metal nitrides are promising materials for the fixation of N$_2$ [58]. Due to the higher fraction of fixed nitrogen per metal and the higher diffusion constant, manganese nitrides might be ideal starting materials for the development of advanced metal nitride redox materials for a solar-driven low-pressure ammonia synthesis.

3.3 Electronic structure descriptors

To understand how doping controls the formation and consumption of nitrogen vacancies in transition-metal nitrides, this section discusses trends in the electronic structure of doped Mn$_2$N and doped Mo$_2$N. We find that the stability of the lattice nitrogen in these materials can be predicted with the average energy of the metal d-states of the dopant and the quantity and
geometry of partially localized electronic charge. Employing these trends for the computational screening [3],[61] of advanced metal nitride redox materials is outlined.

**Figure 7A** decomposes the electronic interaction of the metal dopant, as an example for doped Mo$_2$N, into the metal-projected s-, p-, and d-orbitals. The figure identifies continuous filling of the d-states and emptying of s- and p-states when moving the dopant from the left to the right in the periodic table. These trends correlate with a decreasing stability of the lattice nitrogen, as shown with **Figure 7B** and **7C**. Figure 7B employs the b-band center – that is the central moment of the dopant d-band – as a descriptor for the electronic structure trends in transition-metal doped metal nitrides. This metric has been used successfully for describing adsorption energy trends at transition-metal surfaces which, in turn, has revolutionized the high-throughput screening of advanced catalysts [62]. As a general trend, the positive slope of the correlation shown with Figure 7B identifies the anti-bonding character of the dopant d-states, while the negative slope of the two correlations shown with Figure 7C identifies the bonding contribution of the dopant s- and p-states to the bonding of the lattice nitrogen. However, while the d-band center yields a linear correlation with predictive value, the correlation of the p- and, in particular, the s-band center is rather qualitative. Essentially, only the values for the Zn dopant deviate from the d-band center correlation which can be understood due to the stable configuration of the completely filled Zn d-states, as discussed with SI.

To understand the difference in the sensitivity of the scaling between the free energy of the nitrogen vacancy formation and the number of electrons in the dopant d-states, which is shown with Figure 2 and 3, we compute the partial charge localized at the metals and nitrogen in the metal nitride models. **Figure 8A** and **8B** show the correlation of the free energy of the nitrogen vacancy formation with the partial charge localized at the dopant and the partial charge localized in average at the lattice nitrogen, respectively. Generally, a high amount of net-positive charge localized at the dopant and a high amount of net-negative charge localized at the lattice nitrogen correlate with stable lattice nitrogen. The steeper slope of scaling of the free energy of the nitrogen vacancy formation with the partial dopant charge for D$_{0.5}$Mo$_{1.5}$N vs. D$_{0.25}$Mn$_{1.75}$N suggests that the dopant donates nearly the same amount of charge in both materials which, however, has a stronger effect on the bonding of the lattice nitrogen in D$_{0.5}$Mo$_{1.5}$N relative to D$_{0.25}$Mn$_{1.75}$N. The larger increase or decrease of charge density at the lattice nitrogen when doping D$_{0.5}$Mo$_{1.5}$N vs. D$_{0.25}$Mn$_{1.75}$N, shown with Figure 8B, can therefore be understood due to the dopant concentration in the metal nitride. Doping Mo$_2$N with twice the amount of metal,
compared to Mn$_2$N, yields nearly twice the amount of charge density change in average at the lattice nitrogen, relative to the un-doped metal nitride. Previous studies have suggested that the bonding of nitrogen in metal nitrides can be controlled via metal doping [51]. The trends discussed here indicate that the stability of the lattice nitrogen in transition-metal nitrides can be controlled with the type and the amount of a metal dopant due to the anti-bonding character of the dopant d-states as well as due to the amount of charge density transferred to the lattice nitrogen.

Comparable to the trends in the quantity of the charge density transfer, forming nitrogen vacancies in ternary metal nitrides shows also trends in the geometry of the charge distribution. **Figure 9A** analyzes changes in the charge density due to the formation of nitrogen vacancies in Mo$_2$N. Darker shaded areas mark regions with accumulated charge (charge sinks) while lighter areas mark regions from which charge is withdrawn (charge sources). As shown schematically with **Figure 9B**, the stability trends of the lattice nitrogen can be understood due to attractive and repulsive electronic interactions between charge density sinks and sources.

In detail, doping Mo$_2$N with Sc or Ti results in stronger binding of the lattice nitrogen compared to no doping, as shown with Figure 3. For these dopants, the charge density difference near the dopant exhibits four 3d lobes that are nearly equally pronounced. For the V, Cr and Mo dopants, the binding of the lattice nitrogen decreases while the charge density starts to accumulate at the dopant, next to the lattice nitrogen. When doping with Mn, Fe, Co, and Ni the binding of the lattice nitrogen decreases further while charge density also accumulates at the lattice nitrogen. This suggests that the weaker binding of the lattice nitrogen is due electronic repulsion between two charge sinks. This also explains why the binding of the lattice nitrogen does not decrease further when further increasing the occupancy of the dopant d-states, i.e., when doping with Cu and Zn. For the Cu dopant the spatial polarization of the charge density difference at the dopant weakens while it nearly changes its polarization for the Zn dopant, which appears to cancel the repulsion between two charge sinks. This correlates with an increase in the stability of the lattice nitrogen in Mo$_2$N when doping with Zn. Further details of this analysis are given with SI that is showing the charge density differences due to doping in Mn$_2$N.

### 4. Conclusions

Complementing the production of solar fuels and chemicals via synthetic photosynthesis, NH$_3$ fertilizer from solar-driven N$_2$ and H$_2$O splitting could aid in the global and decentralized production of solar-derived food and biofuels. Renewable NH$_3$ fuel might be an attractive
alternative to carbon-based fuels derived from solar-powered CO\textsubscript{2} and H\textsubscript{2}O splitting, the central reactions of synthetic photosynthesis. In this sense, this work contributes with novel design principles for metal nitride redox materials to the development of a global project on artificial photosynthesis which, in turn, could raise the public profile of this field and may assist in funding the development of solar ammonia production.

Here we have outlined the process conditions required to produce NH\textsubscript{3} from H\textsubscript{2}O and N\textsubscript{2} with a metal nitride redox material and concentrated solar radiation at ambient pressure. This can be achieved with Mo\textsubscript{2}N that is oxidized with H\textsubscript{2}O at approximately 500\degree C and recycled from the formed MoO\textsubscript{2} with N\textsubscript{2}/CO at 750\degree C and below 4.0 x 10\textsuperscript{-1} bar pCO\textsubscript{2}. As an alternative, NH\textsubscript{3} can be formed with Mn\textsubscript{5}N\textsubscript{2} that is oxidized with H\textsubscript{2}O at or above 500\degree C and recycled from the formed MnO with N\textsubscript{2}/H\textsubscript{2} at 1000-1230\degree C and below 1.5 x 10\textsuperscript{-4} bar pH\textsubscript{2}O. Due to the intermediate thermochemical stability of Mn\textsubscript{5}N\textsubscript{2} and MnO, the fast formation kinetics of Mn\textsubscript{4}N, and relative fast apparent solid-state diffusion of nitrogen in Mn\textsubscript{6}N\textsubscript{2.58}, manganese nitride was identified as an ideal candidate for the development of ternary metal nitride redox materials. To further decrease the correlated stability of the metal oxide, the design of ternary manganese-based metal nitrides focuses on destabilizing the lattice nitrogen. We have employed electronic structure theory to show that the stability of the lattice nitrogen in transition metal nitrides can be increased or decreased to a desirable process- and redox material-dependent value via doping with transition metals. This was verified experimentally for manganese nitride doped with iron. The electronic structure trends of transition-metal nitrides suggest that the nitrogen bonding is destabilized with an increasing occupancy of the anti-bonding dopant d-states. The d-band center has been identified as a quantitative descriptor that can be computed from first principles and utilized for the high-throughput screening of advanced metal nitrides for a solar-driven NH\textsubscript{3} synthesis at moderate process conditions.

Acknowledgments

We gratefully acknowledge the financial support by the European Research Council under the European Union’s ERC Advanced Grant (SUNFUELS — No. 320541), the Swiss Competence Center Energy & Mobility, the US National Science Foundation Grant # 0903701 (Integrating the Socioeconomic, Technical, and Agricultural Aspects of Renewable and Sustainable Biorefining Program), and the Center for Sustainable Energy at Kansas State University. We thank Alexandru M. Avram, Daniel L. Boyle, Kent E. Hampton, and James R. Hodgson for their technical
assistance. Experimentation was carried out at Kansas State University. The theoretical calculations and analyses were conducted at the High-Performance Computation cluster of ETH Zürich.

**Electronic supplementary material**

Computational and experimental details, N\textsubscript{2} reduction yields and kinetics with Mo, Cr and Cr-doped Mo at 1 bar, 450-1200°C and 0-120 min, comprehensive summary of the N\textsubscript{2} reduction rate constants, diffusion constants, complete Bader charge analysis and DOS plots for the dopant-projected d-states, Charge density differences due to doping in Mn\textsubscript{2}N, Data repository.

**References**


41. Deml, A. M., Stevanović, V., Holder, A. M., Sanders, M., O'Hayre, R., Musgrave, C. B. 2014 Tunable oxygen vacancy formation energetics in the complex perovskite oxide Sr\textsubscript{x}La\textsubscript{1-x}Mn\textsubscript{y}Al\textsubscript{1-y}O\textsubscript{3}. Chemistry of Materials 26, 6595-6602.


49. Both ASE and GPAW are open-source code available from the Department of Physics at the Technical University of Denmark and are available at https://wiki.fysik.dtu.dk/ase/ and https://wiki.fysik.dtu.dk/gpaw/


Figure captions

Figure 1: Solar-driven low-pressure ammonia synthesis with (A) manganese nitride and (B) molybdenum nitride redox materials, shown schematically with panel (C). Negative values (shaded regions) of the thermodynamic equilibria indicate exergonic reactions; $p\text{H}_2\text{O}$ is fixed at $1.5 \times 10^{-4}$ bar for the reduction of $\text{MnO}$, while $p\text{CO}_2$ is fixed at $4.0 \times 10^{-1}$ bar for the reduction of $\text{MoO}_2$. Online version in colour.

Figure 2: Designing metal nitride redox materials: Free energy of the nitrogen vacancy formation in $D_{0.25}\text{Mn}_{1.75}\text{N}$ metal nitrides doped with a transition metal, D (marked) vs. the number of electrons in the dopant d-states. The solid line marks $\Delta G_v[N]$ for $\text{Mn}_2\text{N}$; the dashed line is a linear regression ($R^2 \sim 0.75$). The filled symbol marks a system that is studied experimentally in this work. Online version in colour.

Figure 3: Designing metal nitride redox materials: Free energy of the nitrogen vacancy formation in $D_{0.5}\text{Mo}_{1.5}\text{N}$ metal nitrides doped with a transition metal, D (marked) vs. the number of electrons in the dopant d-states. The solid line marks $\Delta G_v[N]$ for $\text{Mo}_2\text{N}$; the dashed line is a linear regression ($R^2 \sim 0.93$). The filled symbol marks a system that is studied experimentally in this work. Online version in colour.

Figure 4: Kinetics of the $\text{N}_2$ reduction: Reaction yield in mol% of the indicated metal nitride formed relative to a stoichiometric conversion of Mn at 750°C with (A) Mn and (B) Fe-doped Mn forming $\text{Mn}_4\text{N}$ (light orange symbols) and $\text{Mn}_6\text{N}_{2.58}$ (dark blue symbols). Error propagation within a 95% confidence interval (error bars) yields in average ±17.81%. Solid lines are kinetic models limited by solid-state diffusion that are fitted to the data at 5-30 min for $\text{Mn}_4\text{N}$ and 60-240 min for $\text{Mn}_6\text{N}_{2.58}$. Online version in colour.

Figure 5: Kinetics of the $\text{N}_2$ reduction: Reaction yield in mol% Fe$\text{N}_{0.0324}$ formed relative to a stoichiometric conversion of Fe at 750°C with pure Fe (circles) and Fe-doped Mn (triangles). Error propagation within a 95% confidence interval (error bars) yields in average ±20.83%. The solid line is a kinetic model limited by solid-state diffusion that is fitted to the data at 60-240 min. Online version in colour.
**Figure 6**: Scanning electron micrographs for (A) Mn$_4$N and (B) Mo/Mo$_2$N, and (C) Energy-dispersive X-ray spectroscopy analysis of mostly Cr$_2$N (mixed blue/red domains) and Mo (green domains) formed from an equimolar mixture of Mo (green signal) and Cr (blue signal) powder after nitridation for 2 hrs at 750°C in N$_2$ (red signal). Online version in colour.

**Figure 7**: Electronic structure analysis: (A) Dopant-projected density of states (DOS) of D$_{0.5}$Mo$_{1.5}$N$_{0.5}$ bulk for the marked representative dopants D (occupied states below the Fermi level are shaded and the position of the d-band center is indicated with a dashed line), and correlations of the free energy of the nitrogen vacancy formation with (B) the d-band center and (C) the s- and p-band centers of D$_{0.5}$Mo$_{1.5}$N$_{0.5}$. The complete data is provided with SI. Solid lines are linear regressions to the data shown with filled symbols. Online version in colour.

**Figure 8**: Correlations of the free energy of the nitrogen vacancy formation with the partial average charge of the (A) dopant and (B) lattice nitrogen. Solid lines are linear regressions to the data shown with filled symbols. The data with the highest and lowest partial charges are marked with the dopant. Empty symbols are the un-doped metal nitrides (marked with the metallic constituent) and metal nitrides doped with Zn (marked with Zn). All data is given with SI. Online version in colour.

**Figure 9**: (A) Charge density differences (in units of the elementary charge per Å$^3$) due to the formation of nitrogen vacancies in D$_{0.5}$Mo$_{1.5}$N (shown at the height of the nitrogen nucleus). The first panel in the first row is a schematic of the metal nitride crystal geometry with solid and dashed circles marking atoms in the upper and lower plane of the bulk models, respectively. (B) A schematic of the correlation between the nitrogen binding strength and the charge density and location near the nitrogen vacancy. M, V, and D mark the parent metal, the nitrogen vacancy, and the dopant, while a bold (simple) “+” or “-” mark the strong (weak) accumulation of positive or negative charge, respectively. Online version in colour.
Supporting Information for:

Rational design of metal nitride redox materials for solar-driven ammonia synthesis

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Overview

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1. Stoichiometry of the redox cycle

The reaction stoichiometry of the solar thermochemical ammonia synthesis via a two-step redox cycle can be represented with:

Metal nitride oxidation (Ammonia evolution):

\[
\frac{1}{b} M_a N_b + \frac{ad}{bc} H_2 O \rightarrow \frac{a}{bc} M_c O_d + NH_3 + \left( \frac{ad}{bc} - \frac{3}{2} \right) H_2
\]

Metal oxide reduction (Nitrogen reduction):

\[
\frac{a}{bc} M_c O_d + \frac{1}{2} N_2 \rightarrow \frac{1}{b} M_a N_b + \frac{ad}{2bc} O_2
\]

where M denotes a metal and \(M_a N_b\) and \(M_c O_d\) are the (completely) nitrated and oxidized forms of the metal nitride redox material with generalized stoichiometry. We note the thermochemical equilibrium of the metal oxide reduction can be shifted towards the formation of the reaction products via adjusting the process pressure and temperature and via coupling the reaction to the oxidation of a chemical reducing agent such as \(CO, H_2\), or gasified biomass.

2. Computational details

2.1 Thermochemical equilibrium calculations

Thermochemical data [1] were extrapolated for \(\text{Mn}_4\text{N}\) at \(\geq 700\) K \((R^2 = 1)\), for \(\text{Mn}_5\text{N}_2\) at \(\geq 900\) K \((R^2 = 0.999999)\), and for \(\text{Mo}_2\text{N}\) at \(\geq 1500\) K \((R^2 = 0.999997)\) using third-order polynominal regressions.

2.2 Local optimization procedures

In all DFT calculations the linesearch BFGS algorithm was employed to optimize the atomic geometries until the maximum force was less than 0.05 eV Å\(^{-1}\). Convergence was achieved with a Fermi-Dirac smearing of 0.1 eV and the structure optimization results were extrapolated to 0 K. The lattice constants of the \(\text{Mo}_2\text{N}\) and \(\text{Mn}_2\text{N}\) bulk metal nitrides were chosen as the DFT-calculated bulk lattice constants to avoid reminiscent stress in the calculations. We note, the DFT-computed lattice constants (i.e., \(a = 4.220\) Å for \(\text{Mo}_2\text{N}\) and \(a = 2.853\) Å and \(c = 4.393\) Å for \(\text{Mn}_2\text{N}\)) compare well with the experimental values (i.e., \(a = 4.163\) Å for \(\text{Mo}_2\text{N}\) [2] and \(a = 2.844\) Å and \(c = 4.509\) Å or \(\text{Mn}_2\text{N}\) [3]), which is a relative difference of 0.32-2.57% that is within the uncertainty of DFT calculations. [4],[5]

2.3 Free energy computations

The free energies of the chemical species \(i\) \((G_i)\) was calculated with: [5]

\[
G_i(T,P) = N_i \mu_i(T,P) = E_i + U_{ZPE,i} - TS_i(T,P)
\]
where T is the absolute temperature (298.15 K), P is the absolute pressure (1.013 bar), N_i is the number of atoms, \( \mu_i \) is the chemical potential, \( E_i \) is the DFT-determined total electronic energy, \( U_{ZPE,i} \) is the zero-point vibrational energy, and \( S_i \) is the entropy. \( N_2 \) was assumed to be an ideal gas, while the liberated lattice nitrogen was computed based on the harmonic approximation where all degrees of freedom are treated as frustrated harmonic vibrations and pressure-volume contributions are neglected. All thermodynamic properties were calculated from vibrational frequencies and standard statistical mechanical equations, evaluated through ASE, and free energy corrections of the solids were neglected. [6]

The free energy of forming nitrogen vacancies (\( \Delta G_v[N] \)) in the bulk was computed with: [7]

\[
\Delta G_v[N] = G_v - (G_s - G_{N_2}^r)
\]

where \( G_v \), \( G_s \) and \( G_{N_2}^r \) are the free energies of the metal nitride model with the nitrogen vacancies, the stoichiometric metal nitride (without nitrogen vacancies) and the reference energy of the lattice nitrogen yielding \( N_2 \) gas. Negative free energies indicate an exergonic evolution of the lattice nitrogen. The reference free energy of nitrogen (\( G_{N_2}^r \)) is computed from stable \( N_2 \) gas, [4],[5] with:

\[
G_{N_2}^r = G[N_2]/2
\]

where \( G[N_2] \) is the free energy of \( N_2 \) molecules in the gas phase.

2.4 Charge density differences

The charge density difference (CDD) for doping a metal nitride is computed as the difference between the volumetric charge density (CD) of a doped bulk metal nitride and the CD of the metal nitride without the dopant. Analogously, the CDD for the formation of nitrogen vacancies is computed as the CD of a metal nitride model with nitrogen vacancies plus the CD of the balance of atomic nitrogen minus the CD of the stoichiometric metal nitride model.

3. Experimental details

3.1 N_2 reduction

The level of impurities of the metal precursors is given by the manufacturer (Noah Technologies) for Mn (99.9% pure) with: 0.0015% Ag, 0.0030% Al, 4.16 ppm As, 3.78 ppm B, < 1 ppm Ba, < 1 ppm Be, < 1 ppm Bi, 0.0099% Ca, < 1 ppm Cd, 2.38 ppm Co, 0.0059% Cr, < 1 ppm Cu, 0.0571% Fe, < 8 ppm K, 3.19 ppm La, < 1 ppm Li, < 4 ppm Mg, < 1 ppm Mo, < 0.001% Na, < 1 ppm Ni, < 4 ppm P, 0.0019% Pb, < 4 ppm Pd, 0.0379% S, 0.0020% Sb, 0.0076% Se, 0.0070% Si, < 4 ppm Sn, < 1 ppm Sr, < 4 ppm Th, < 2 ppm Ti, 0.0177% Tl, < 0.002 % U, < 1 ppm V, 9.73 ppm W, < 1 ppm Y, < 1 ppm Zn, < 2 ppm Zr; for Mo (99.95% pure) with: < 1 ppm Al, < 1 ppm Co, < 1 ppm Cr, < 1 ppm Cu, < 1 ppm Fe, < 1 ppm Mg, < 1 ppm Mn, < 1 ppm Ni, < 0.004% W, < 0.015% O_2, < 0.001% C (total); for Fe (99.9% pure) with: < 3 ppm As, < 2 ppm Hg, < 4 ppm Pb, 0.04% acid insolubles; and for Cr (99.8% pure) with: 0.10% Fe, 0.012% C, 0.68% O, 0.022% S.

Table S1 summarizes the characterization of the metal reactants and the metal nitrides that were formed from pure metal powder and \( N_2 \). We note Table S1 does not list the discussed cubic FeN_{0.0324} since this compound was not obtained with pure Fe powder.
The tube furnace employed in this work was equipped with a quartz tube (60 mm inner diameter, 1 m length) that was purged for 10 min with 0.5-0.9 L(STP) N₂ min⁻¹ before each experiment. The heating rate (rₘ) for N₂ reduction experiments at 750°C was approximately rₘ = At + B, where t is the heating time in min, A = -6.91 °C min⁻² and B = 77.4 °C min⁻¹.

To determine the temperature that results in a minimum formation of surface oxides during the nitridation of Mo, the reaction of Mo powder with N₂ held for 2 hrs: 998 ± 3 mg Mo was placed into a quartz boat, pretreated for 10 min (STP) and B: 998 ± 3 mg Mo was placed into a quartz boat, pretreated for 10 min (STP) and replaced with a flow of 1.86 ± 0.05 L(STP) N₂ min⁻¹ when the maximum reaction temperature was reached. After 2 hrs the furnace was cooled (at about -13.5 to -2.73 °C s⁻¹ within the first 60 s, -3.85 to 0.767 °C s⁻¹ at 60 to 180 s and above -0.767 °C s⁻¹ at above 180 s) to below 75°C. The solid was removed and stored under air at 4°C. To eliminate the possibility of rapid quenching affecting the yield of Mo₂N, the nitridation of Mo for 2 hrs with N₂ at 450 or 750 °C was repeated with a cooling rate of about -6.05 to -1.80 °C min⁻¹. This decrease in the cooling rate did not affect the Mo₂N yield.

3.2 Processing of experimental data

The yield (Xᵢ) of the chemical species j (a metal, metal nitride or metal oxide, respectively) is reported as the molar ratio of a chemical species detected after the experiment (nᵢ in mol) relative to the theoretical amount of that species formed at stoichiometric conversion of the metal reactant (nᵢ* in mol)

\[
X_j = \frac{n_j}{n_j^*} = \frac{\Delta m_{v,j} M_{\text{metal}}}{\Delta m_p X_{\text{metal}} M_j a_j}
\]

where \(\Delta m\) (in g) is the mass difference between the solid reactant and the quartz boat at time \(t\) and before the reaction (subscript 0), \(x\) (in g g⁻¹) is the metal, metal nitride, or metal oxide weight fraction, \(M\) (in g mol⁻¹) is the molar mass, and \(a\) is a dimensionless coefficient that is accounting for the stoichiometric amount of metal atoms contained in the reaction product.

Table S1: Characterization of the metal and binary metal nitride powder beds

| Metal | Mo | Cr | Fe | Mn | Nitride | \(\beta\)-Mo₂N | Cr₂N | \(\varepsilon\)-Mn₄N
\(\text{CrN}\) | (\(\text{MnN}_2\text{N}_{2.58}\)) |
|-------|----|----|----|----|---------|--------------|------|-------------------|
| Space group | \(\text{Im} \bar{3} \text{m}\) | \(\text{Im} \bar{3} \text{m}\) | \(\text{Im} \bar{3} \text{m}\) | \(\text{I}4 \bar{3} \text{m}\) | \(\text{I}4 \bar{3} \text{m}\) | \(\text{P}3\overline{1} \text{m}\) | \(\text{P}3\overline{1} \text{m}\) | \(\text{Pm} \bar{3} \text{m}\)
\(\text{Fm} \bar{3} \text{m}\) | \(\text{P}6\overline{1}22\) |
| \(d_p\) (μm) | 6 ± 4 | 18 ± 13 | 29 ± 21 | 43 ± 22 | 7 ± 4 | 17 ± 11 | 46 ± 19 |
| \(A_{\text{BET}}\) (m² kg⁻¹) | 429 ± 3 | 692 ± 8 | 281 ± 5 | 269 ± 2 | 426 ± 3 | 654 ± 9 | 270 ± 3 |
| \(\Phi\) (m³ m⁻³) | 0.75 | 0.57 | 0.66 | 0.62 | - | - | - |

\(\Lambda\) via X-ray diffraction; \(\beta\) average particle diameter; \(\gamma\) BET surface area; \(\delta\) void space fraction \(\Phi = 1 - \rho_{\text{bulk}}/\rho_{\text{particle}}\), where \(\rho_i\) is the density in kg m⁻³, relative error via error propagation ± 5.98 %; generally, powder bed surface = 33 ± 2 cm², powder bed thickness < 1 mm.
To assess the effect of solid-state diffusion limitations, a diffusion-limited shrinking-core model for spherical particles with constant size [8] was applied to the experimental data:

\[
(S7) \quad kr = 1 - 3 \times (1 - X_j)^{2/3} + 2 \times (1 - X_j)
\]

where \( k \) (in \( s^{-1} \)) is a specific rate constant. We note this model describes the reported kinetic data best (highest \( R^2 \)) when compared to kinetic models that account for limiting gas phase diffusion or available surface area. [8]

4. Supporting results

4.1 \( N_2 \) reduction with Mo, Cr, and Cr-doped Mo

Figure S1 shows the formation of \( Mo_2N \) and \( MoO_2 \) from Mo heated in \( N_2 \). XRD showed formation of tetragonal \( \beta-Mo_2N \) with a homogeneity range of 28.7 to 34.5 mol\% N. Thus, quantitative calculations in this work assume stoichiometric \( Mo_2N \) as-indicated. Given the minimum \( MoO_2 \) yield and maximized \( Mo_2N \) near this temperature, Mo was nitrated at 750°C in this work.

Figure S2 shows the formation of \( Mo_2N \) with pure Mo powder or Cr-doped Mo powder and \( N_2 \) or a mixture of \( H_2 \) and \( N_2 \); the formation of \( Cr_2N \) and \( CrN \) with pure Cr powder and \( N_2 \) or a mixture of \( H_2 \) and \( N_2 \) is shown for reference. The nitridation of Mo at 750°C and 1 bar reaches a 1.2 mol\% yield after 0.5 min, that is increasing thereafter with diminished kinetics to a maximum of 3.3 mol\% after 120 min. Cr fixes \( N_2 \) quickly forming 66 ± 3 mol\% \( Cr_2N \) after 10 min, which converts into up to 15.8 ± 0.5 mol\% \( CrN \) after 120 min. The formation of \( CrN \) is slow and is described well with a diffusion-limited reaction mechanism (\( R^2 > 0.94 \)). Forming the nitrides in presence of \( H_2 \) affects the yield of \( Cr_2N \) and \( CrN \) only slightly but increased the yield of \( Mo_2N \) more than six-fold to 21.1 ± 0.7 mol\% after 120 min. While the formation of the trigonal \( Cr_2O_3 \) phase was in average 34% below the yield of \( Cr_2O_3 \) when reacting the metal with \( N_2 \) only (which yielded 0 to 2.7 mol\% \( Cr_2O_3 \)), \( MoO_2 \) or \( MoO_3 \) were not detected. The yield of \( Mo_2N \) from Mo/Cr powder mixtures reacted with \( N_2 \) or the \( N_2/H_2 \) gas mixture differs only slightly from the results obtained with Mo and the \( N_2/H_2 \) gas mixture; in presence of Cr after 120 min 18 ± 2 and 23 ± 5 mol\% \( Mo_2N \) were formed in absence or presence of \( H_2 \), respectively. The limited yield of \( Mo_2N \) from Mo and \( N_2 \) that is increased by the presence of \( H_2 \) or Cr can be understood due to the reduction of a thin layer \( MoO_2 \) that limits the formation of \( Mo_2N \) at the surface of the Mo reactant, yielding \( H_2O \) or traces of chromium oxides with \( H_2 \) or Cr respectively. The generally slow formation of \( Mo_2N \) in presence of Cr or \( H_2 \) indicates that the hypothesized promotion of the \( N_2 \) reduction yield with Mo by the presence of Cr cannot be assessed due to diffusion limitations that prevent reaching the thermochemical equilibrium at the studied experimental conditions.
Figure S1: Formation of Mo$_2$N (light orange symbols) or MoO$_2$ (dark blue symbols) in mol% of the indicated metal compound formed relative to stoichiometric conversion of Mo after heating at a given temperature for 2 hrs with 1 bar N$_2$. Lines are a guide only. The average relative error of the data within a 95% confidence interval is ± 22.86%.

Figure S2: Reduction of N$_2$ at 750°C with (A) Mo and 1 bar N$_2$ (dark red symbols) or 0.199 bar H$_2$ diluted in 0.801 bar N$_2$ (light orange symbols) forming Mo$_2$N, (B) an equimolar mixture of Mo and Cr and 1 bar N$_2$ (dark red symbols) or 0.199 bar H$_2$ diluted in 0.801 bar N$_2$ (light orange symbols) forming Mo$_2$N, and (C) Cr and 1 bar N$_2$ forming Cr$_2$N (dark red symbols) and CrN (dark blue symbols) or 0.199 bar H$_2$ diluted in 0.801 bar N$_2$ forming Cr$_2$N (light orange symbols) and CrN (light blue symbols). Error bars are via error propagation within a 95% confidence interval. Solid lines are kinetic models limited by solid-state diffusion that are fitted to the data at 0.5-120 min. Dashed lines are the approximate location of the thermodynamic equilibrium for forming the indicated metal nitride with N$_2$.

Figure S3 shows the morphology of Mo as-purchased, after heating in N$_2$, and after heating in H$_2$/N$_2$. The analysis shows while Mo retains its hexoctahedral symmetry after heating with N$_2$ it is apparently covered with a structure that replaces the terrace-like appearance of the pristine Mo surface. Heating Mo in H$_2$/N$_2$ results in the disappearance of the hexoctahedral symmetry of Mo. This in conjunction with the increased yield of Mo$_2$N when heating Mo in H$_2$/N$_2$ confirms the interpretation that MoO$_2$ is formed from traces O$_2$ and H$_2$O at the surface of Mo that is heated in N$_2$. This oxide layer limits the formation of Mo$_2$N. The oxide layer is removed in the presence of H$_2$ which explains the increased yield of Mo$_2$N due to decreased diffusion limitations.
Figure S3: Scanning electron micrographs of Mo samples (A) as-purchased, (B) after heating for 2 hrs at 750°C in N₂, or (C) in 0.199 bar H₂ diluted in 0.801 bar N₂.

Table S2 summarizes the reaction rate constants determined from the experimental data and shrinking-core models that account for solid-state diffusion limitations.

Table S2: Reaction rate constants, k

<table>
<thead>
<tr>
<th>Solid reactant</th>
<th>Solid product</th>
<th>Gas phase</th>
<th>Time range / s</th>
<th>k / s⁻¹</th>
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<tbody>
<tr>
<td>Mn</td>
<td>Mn₄N</td>
<td>N₂</td>
<td>5-30</td>
<td>4.14 × 10⁻⁴</td>
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<tr>
<td>Mn</td>
<td>Mn₆N₂.₅₈</td>
<td>N₂</td>
<td>60-240</td>
<td>3.71 × 10⁻⁵</td>
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<td>Mn/Fe</td>
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<td>N₂</td>
<td>5-30</td>
<td>1.81 × 10⁻⁴</td>
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<tr>
<td>Mn/Fe</td>
<td>Mn₆N₂.₅₈</td>
<td>N₂</td>
<td>60-240</td>
<td>3.89 × 10⁻⁶</td>
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<tr>
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<td>Mo₂N</td>
<td>N₂</td>
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</tr>
<tr>
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<td>Mo₂N</td>
<td>N₂/H₂</td>
<td>5-120</td>
<td>2.57 × 10⁻⁶</td>
</tr>
<tr>
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<td>Mo₂N</td>
<td>N₂</td>
<td>5-120</td>
<td>2.68 × 10⁻⁶</td>
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<td>Mo/Cr</td>
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<td>5-120</td>
<td>2.15 × 10⁻⁶</td>
</tr>
</tbody>
</table>

A) pure or equimolar mixtures; B) 1 bar N₂ or 0.199 bar H₂ diluted in 0.801 bar N₂

From the experimental data an apparent diffusion constant, D, can be estimated with [8]:

\[ D = \frac{\rho_p d_p^2 k}{24 b c_g} \]  

where \( \rho_p \) (in mol m⁻³) is the density of the solid reactant, \( d_p \) (in m) is the average particle diameter, \( b \) is the dimensionless molar ratio of reacted solid per reacted N₂, and \( c_g \) (in mol m⁻³) is the molar concentration of N₂. The computation was limited to the reported kinetic data that is well described with equation S7 (i.e., \( R^2 \) in the range of 0.90 to 0.98 for CrN and Mo₂N respectively, 0.80 to 0.85 for Mn₆N₂.₅₈).

Figure S4 plots \( D \) vs. the theoretical volume fraction, \( f_v \), occupied by atoms or ions:
\[ f_v = \frac{4\pi N_A \rho}{3} \sum \gamma_k r_k^3 \]

where \( N_A \) is Avogadro’s constant, \( \rho \) (in mol m\(^{-3}\)) is the molar density of the formed reaction product, \( \gamma_k \) is the dimensionless fraction of atoms per product phase, and \( r_k \) (in m) is the radius of the nitrogen or the metallic constituent of the metal nitride. Based on the relative low electronegativity of Mn, nominal N\(^3\)- ions were assumed for Mn\(_6\)N\(_{2.58}\) (i.e., Mn in 2+ oxidation state). CrN and Mo\(_2\)N [9],[10] were computed as metallic compounds (i.e., atomic N bonded covalently by 12-coordinated metal atoms). MoO\(_2\) that is presumably present when reacting Mo with N\(_2\) was included as ideal ionic compound.

![Graph](image-url)  

Figure S4: Apparent diffusion coefficients for the diffusion through the marked solid at 750°C vs. the theoretical volume occupied by metal and nitrogen or oxygen atoms. The density of Mn\(_6\)N\(_{2.58}\) was estimated with 6,131 ± 292 kg m\(^{-3}\). The solid line is to guide the eye. Error propagation within a 95% confidence (error bars) yields in average ± 17.81%. The highest present nitride phases are indicated along with the gases present during the nitridation experiments in parenthesis.

4.2 Electronic structure details

Table S3 summarizes the Bader charge analysis of the metal nitrides models.
Table S3: Partial charges, $q_{\text{Atom}} / e$

| Atom | $D$ in $D_0.25Mn_{1.75}N$ | D | $D_{\text{in} D}$ | Sc | Ti | V | Cr | Mo | Mn | Fe | Co | Ni | Cu | Zn |
|------|--------------------------|---|------------------|----|----|---|----|----|----|----|----|----|----|----|----|
| D    | 1.4743                   | 1.4072 | 1.1414 | 0.8612 | 0.8437 | 0.7359 | 0.5704 | 0.3954 | 0.2978 | 0.3484 | 0.5600 |
| Mn   | 0.6244                   | 0.6565 | 0.6959 | 0.7185 | 0.7275 | 0.7359 | 0.7601 | 0.7863 | 0.7972 | 0.7820 | 0.7493 |
| Mn   | 0.7879                   | 0.7587 | 0.7363 | 0.7199 | 0.7750 | 0.7375 | 0.7318 | 0.7187 | 0.7249 | 0.7363 | 0.8200 |
| Mn   | 0.6383                   | 0.6606 | 0.7002 | 0.7384 | 0.7048 | 0.7374 | 0.7509 | 0.7689 | 0.7693 | 0.7628 | 0.7423 |
| Mn   | 0.5855                   | 0.6081 | 0.6727 | 0.7144 | 0.7405 | 0.7375 | 0.7686 | 0.7930 | 0.8037 | 0.7828 | 0.7542 |
| Mn   | 0.6383                   | 0.6606 | 0.7000 | 0.7385 | 0.7049 | 0.7374 | 0.7509 | 0.7689 | 0.7693 | 0.7626 | 0.7423 |
| Mn   | 0.6244                   | 0.6564 | 0.6957 | 0.7189 | 0.7275 | 0.7359 | 0.7603 | 0.7861 | 0.7971 | 0.7818 | 0.7496 |
| Mn   | 0.6319                   | 0.6526 | 0.6914 | 0.7300 | 0.6938 | 0.7359 | 0.7497 | 0.7693 | 0.7808 | 0.7813 | 0.7487 |
| N    | -1.5097                  | -1.5302 | -1.5196 | -1.4896 | -1.4866 | -1.4734 | -1.4562 | -1.4346 | -1.4204 | -1.4186 | -1.4663 |
| N    | -1.5093                  | -1.5279 | -1.5204 | -1.4882 | -1.4850 | -1.4735 | -1.4550 | -1.4358 | -1.4198 | -1.4195 | -1.4644 |
| N    | -1.5093                  | -1.5279 | -1.5194 | -1.4884 | -1.4850 | -1.4734 | -1.4549 | -1.4357 | -1.4198 | -1.4197 | -1.4644 |
| N    | -1.4767                  | -1.4747 | -1.4745 | -1.4738 | -1.4612 | -1.4734 | -1.4766 | -1.4807 | -1.4803 | -1.4805 | -1.4715 |

Figure S5 shows a complete density of states (DOS) analysis of the dopant-projected d-states. The figure shows how the dopant d-states are increasingly occupied when moving the dopant in the periodic table from the left to the right, which is shown in the manuscript representatively for $\text{Ti}_{0.5}\text{Mo}_{1.5}\text{N}$, $\text{Mo}_{2}\text{N}_{0.5}$, and $\text{Cu}_{0.5}\text{Mo}_{1.5}\text{N}_{0.5}$. Furthermore, the figure shows how the deviation of Zn-doped compounds from the correlations discussed in the manuscript can be understood due to the energetically highly stable and essentially fully occupied d-states of the Zn dopant, when compared to the DOS of all other dopants in both Mo$_2$N- and Mn$_2$N-based metal nitrides.
Figure S5: Density of states (DOS) for stoichiometric $D_{0.5}Mo_{1.5}N$ (using a $k$-point sampling of $12 \times 12 \times 12$, except $8 \times 8 \times 8$ for $D = Ni$) and $D_{0.25}Mn_{1.75}N$ (using a $k$-point sampling of $8 \times 8 \times 8$); the dopant, $D$, is marked on each DOS plot and the occupied states below the Fermi level are shaded in blue.

Comparable to the trends in the quantity of the charge density transfer, doping transition-metal nitrides with different metals shows as well trends in the geometry of the charge redistribution. Figure S6 shows the difference in the volumetric charge density between doped $Mn_{2}N$ and undoped $Mn_{2}N$. Darker shaded areas mark regions with accumulated charge (charge sinks) while lighter areas mark regions from which charge is withdrawn (charge sources). Comparing the charge density differences at the height of the dopant nucleus across the tested dopants shows a polarization of the charge density difference near the dopant with a distinct charge source that is opposite to a charge sink for all dopants with fewer or equal valence electrons in d-orbitals, relative to the Mn $3d^5$ occupancy (i.e., Sc to Cr and Mo). In these materials the nitrogen vacancies are formed at the lattice nitrogen that is marked with a solid circle in the schematic of the crystal geometry. With decreasing stability of the lattice nitrogen due to doping with metals...
that have more valence electrons in d-orbitals relative to Mn (i.e., Fe to Zn), this polarization of the charge density difference rotates by about 180°. For the Fe, Co and Ni dopants, this coincides with the formation of the nitrogen vacancies at the lattice nitrogen that is marked with a dashed circle, i.e., along an axis that is rotated by 180° relative to the vacancy formation in the metal nitrides with a reversed polarization of the charge density difference. For the two dopants with nearly or completely filled d-states, i.e., Cu and Zn, the nitrogen vacancies are formed at the lattice nitrogen that is marked with a solid circle.

**Figure S6:** Charge density differences (in units of the elementary charge per Å³) due to doping $D_{0.25}\text{Mn}_{1.75}\text{N}$ bulk with the indicated dopant D (shown at the height of the dopant nucleus). The first panel in the first row is a schematic of the metal nitride crystal geometry with solid and dashed circles marking atoms in the upper and lower plane of the bulk models, respectively.
5. References


