# /COMPUTER PROGRAM FOR SIZING AND ANALYZING FIXED SHADING DEVICES (SHADE)/ 

by

VINOD S. CHATURVEDI
B. Arch., Bombay University, India, 1985

A Master's Thesis
submitted in partial fulfillment of the
requirements for the degree
MASTER OF ARCHITECTURE

Department of Architecture College of Architecture and Design

KANSAS STATE UNIVERSITY
Manhattan, Kansas
1990


Prof. Gary Coates

# Computer Program for Sizing and Analyzing Fixed SHAding DEvices 

SHADE


## Acknowledgements

I am very grateful to Professor Dale Bryant without whose advice and able guidance this thesis would not have even been undertaken. I whole heartedly thank him for the time that he spent with me on this project.

Thanks also to Professor Gary Coates and Professor Claude Keithly for the help that they gave me in all possible ways through out this project.

At the end, I would like to thank my parents and family for their endless efforts in achieving my educational goals, and all others who helped me directly or indirectly in successful completion of this thesis.

## Table of Contents

Preface ..... 1
Introduction ..... 3
Program Overview ..... 8
Tutorial ..... 11
System Overview ..... 28
List of User-Defined Variables ..... 30
Future Improvements and Additions ..... 33
Conclusion ..... 36
Appendix
A. Heliodon Test Results ..... 39
B. Solar Position Charts ..... 41
C. U.S. and World Maps ..... 51
D. Sizing Overhang ..... 54
E. Sizing Wing Wall ..... 56
F. User Response ..... 58
G. Program Listing ..... 61
Bibliography ..... 63
Abstract

## Preface

Passive solar design has now become a significant part of the process of architectural design. In order to design efficient passive solar building it is necessary to provide appropriately sized shading devices that allow sun to strike the window when it is needed and block the sun when it is too hot for comfort. By enhancing the designer's ability to design shading devices, the computer program SHADE contributes to the development of the field of passive solar design.

SHADE allows architects working in the preliminary design phase to size and evaluate the performance of fixed horizontal overhangs and/or vertical wing walls. It is also a useful tool for lay persons and students of architecture who are interested in learning more about Environmental Systems in Architecture. Now, with SHADE it is easier not only to size the fixed shading devices but also to evaluate the shading performance of these devices at any time of year, without using the cumbersome process of constructing sun path diagrams or making models to be tested under simulated solar conditions.

A basic knowledge of solar design is still required to use this program - such as having an ability to visualize the solar positions at different times of day and for different seasons. The 'beginner' is strongly advised to read "Designing with the LOF Sun Angle Calculator" distributed by Libbey-Owens-Ford Company, Toledo, Ohio, 1975 before operating SHADE.

Phase-I of SHADE is developed to allow the user to size and locate fixed horizontal overhangs. The limitation for sizing horizontal overhangs is that they only can be sized correctly and practically for windows facing within 10 degrees east or west of due south.

The vertical wing walls can be sized in Phase-ll for all window orientations. However, it will work most accurately for windows
facing + or -30 degrees of due south. For all other window orientations, the sizing would still be accurate, but due to certain assumptions regarding the appropriateness and location of wing walls explained later in the text (pg. 20), the output may not be reliable.

The edge effect of the overhang can be addressed by suitably sizing the overhang extension beyond the left or right edge of the window in Phase-III.

The strongest and perhaps the most useful feature of SHADE is the shadow pattern simulation of shading devices in Phase-IV. The performance of a horizontal overhang or a combination of horizontal overhang and vertical wing walls can be evaluated by viewing the shadow pattern for the design under consideration at one hour intervals for the entire year, even at diferent window orientations. The size of overhang or wing walls can be the one derived through the program in Phase-I and II or the user can choose to evaluate any other design of his or her choice. The only limitaton is that, in order to be able to view a shadow pattern for a combination of horizontal overhang and vertical wing walls, the sizes of both the projections will have to be the same. This requirement of the program is the result of the need to simplify the shadow patterns.

A user can study various permutations and combinations of fixed shading device designs and carefully evaluate them all before selecting the one (or ones) that are most appropriate for the design under consideration. To facilitate the use of SHADE generated results outside the computer work station, a hard copy of any desired graphics or text output can be easily printed at the stroke of a key anytime during the entire execution of the program.

## Introduction

${ }^{1}$ A south facing window in a passive solar building designed to gather as much sun as possible in winter, while reducing the winter space heating demands may also lead to overheating the interior if left exposed during the summer months. Controlling this cycle throughout the year is an important aspect of energy conserving passive solar design. A horizontal overhang that is properly located above the window is one simple way to shade the collector during summer months while leaving it unshaded during winter.


Fig. 1 This and fig. 2, $3 \& 6$ are reproduced from "Sizing Fixed Overhangs for Solar Collectors", a handout distributed by the Technical Energy Information Services of the KSU Cooperative Extension Service, 1983.

Latitude, window size and orientation all affect the design of an effective sun shading device. The earth's axis is not perpendicular but is tilted at a constant angle of 23027 ' to the plane in which it orbits the sun. Because of this fact, at one point in the orbit, i.e. during winter, the axis tilts away from the sun, resulting in the sun appearing low in the sky. At the opposite point, half a year later during summer, the axis is tilted toward the sun, causing the sun to appear higher in the sky (Fig. 1). Thus a building located between the

[^0]tropics will actually have sunlight on the north side in June and the south side in December.

The time of year is equally important. The figure below illustrates the seasonal variation in sun path. In summer, the sun rises and sets north of the east-west line while in winter it rises and sets south of that line.


Fig. 2
Also, note how the elevation of the sun at its highest point, or solar noon, changes with the season. (Fig. 3)

Fig. 3


For the window to be fully sunlit in the winter, there must be a gap between it and the overhang. The gap is the space between the bottom of the overhang and the top of the window. The overhang projection and gap are usually expressed as ratios with respect to the window height. The relative projection is the required projection
divided by the window height. Similarly, the required gap divided by the window height gives the relative gap. (Fig. 4)


Fig. 4: Section
The equation to find the relative projection and gap are as follows ${ }^{1}$ :
Relative gap $=\tan (L$ - Ds $) /(\tan (L-D w)-\tan (L-D s))$
Relative Projection $=1 /(\cot (\mathrm{L}-\mathrm{Ds})-\cot (\mathrm{L}-\mathrm{Dw})$
Where, $\mathrm{Ns}=$ (Number of desired shade days in summer) $\times 1 / 2$
$\mathrm{Nw}=($ Number of desired sun days in winter) $\times 1 / 2$
L = Latitude
Ds $=$ Summer Declination $=23.45 \sin ((360 / 365)(N s+456))$
$\mathrm{Dw}=$ Winter Declination $=23.45 \sin ((360 / 365)(\mathrm{Nw}+639))$
The correct length of an overhang must also be considered to avoid the edge effect. The edge effect occurs when the overhang does not extend horizontally along the wall far enough to prevent the sun from slipping past on either side and striking the window. For all practical purposes, there will not be any edge effect if the following relation is true (Fig. 5) :
(relative extension) $+[3 / 25 \times$ (relative width) $]$ is $>2.7$
Where, relative extension $=$ horizontal overhang extension along the wall beyond the window / window height
relative width $=$ window width $/$ window height

[^1]

Relative Extension $=\mathrm{e} / \mathrm{h}$ Relative Width $=w / h$

Fig. 5 : Elevation
An overhang can be designed to provide a specific number of days of full sun striking the window in winter and complete shade in summer. The rest of the time the window will be partly shaded and partly exposed.

Ideally, windows should be shaded during the entire cooling season (i.e. summer) and sunlit during the entire heating season (i.e. winter). But this usually is not practical unless moveable devices are built. In general, the more full-sun or full-shade days desired, the larger the overhang has to be.

Another problem is that while the days of full shade and full sun are symmetrical around the summer and winter solstices, the maximum heating and cooling loads normally occur 30 to 45 days after the respective solstices. (Fig. 6). This symmetry of the shading about the solar cycle rather than the heating and cooling cycle means, for instance, that a window shaded during the summer will likely be shaded during the latter part of winter, too.


Fig. 6

Thus, to design an effective overhang for a given window using the computer program SHADE the site latitude, and preferred number of shade and sunlit days should_be known (Refer to "List of UserDefined Variables" on pages $30-32$, to determine the number of full shade days and full sun days). The number of full-shade days does not have to be the same as the full sun-sun days.

## Program Overview

SHADE is developed to size and locate fixed shading devices, such as horizontal overhangs in Phase-I and vertical wing walls in Phase-II, for any window at any latitude. The edge effect of the overhang can be addressed by suitably sizing the overhang extension beyond the left or right edge of the window in Phase-III. The performance of a shading device can be evaluated for the entire year, at different window orientations, in Phase-IV. The description of each phase is as follows :

## PHASE-I. SUZUNG OVERMANG

This segment of the program works only for windows facing + or 10 degrees of due south. For all other window orientations, the sun is so low in the sky that for any overhang to be effective, it will have to be unusually large, which in turn may not be practical.

Input : Height and width of window under investigation, the site latitude, desired number of full shade days and full sun days. (Refer to "List of User-Defined Variables" on pages $30-32$, to determine the number of full shade days and full sun days.)

Output : The size of overhang projection and the gap from the top of the window.

## PHASE-II. SUZUNG WING WALL

For most of the windows facing between east or west of due south, an overhang alone on top of the window may not be enough to shade the window entirely and effectively especially during the hottest period of the day. An appropriately sized wing wall on one or both sides of the window (depending on window orientation) may be designed to counter this problem.

Input : Height and width of window, site latitude, orientation of window, desired month, day, and beginning hour (Time -1) and ending hour (Time - 2) between which $100 \%$ shade is required; and desired month, day, and beginning hour (Time - 3) and ending hour (Time - 4) between which $100 \%$ sun is required.


Fig. 7 : Plan
Output : The size of the right and left wing wall projections and their respective gaps from the edge of the window.

## PHASE-III. OVERMANG EXTENSION

An alternative to placing wing walls on one or both sides of the window is to have an overhang extending beyond the sides of window to such a length that it will nullify the edge effect. (See explanation in Introduction).

Input : Size of window, site latitude, orientation of window, desired month, day of month, and beginning and ending hours of day for $100 \%$ shade.

Output : The length of the overhang extension on one both sides of the window. (fig. 8)


Fig. 8 : Elevation

## PHASE-IV. SHADOW PATTERN

There are two parts to this section. Part One is the shadow pattern simulation for a window with only a horizontal overhang. Part two is for a window with both a horizontal overhang and a wing wall on one or both sides of the window.

Input : height and width of window, orientation of window, desired month of year, and day of month for viewing shadow casting pattern.

Output : Shadow pattern simulation for the entire year at one hour intervals, beginning from the first hour after sunrise to an hour before sunset for each day. Also, the percentage area of the window in sun and shade is shown for each hour.

## Tutorial

The Program Overview outlines the input requirements of different program phases and the output that can be produced. This section is designed as a tour of the various phases for the first time user.

## Program Setup :



Fig. 9 : The boxes indicate the key to be pressed to get into or out of various phases.

The operation of the program is fairly simple. The program is presented in a phased manner, and most of the steps follow a definite sequence. Upon choosing any phase from the Main Menu,there is first a brief explanation of various input requirements relevant to that phase. After reading through the text the user may proceed with that phase by pressing any key on the keyboard (except ESC). It is possible to return to the Main Menu by pressing "ESC".

For some of the steps in this program, the user is advised to follow a certain sequence. For example, a user may not get into the shadow pattern simulation phase of program if the overhang or wing wall sizes are not defined. This sizing may be done first by entering the appropriate phase. It is also possible to use some pre-determined size for the horizontal overhang or wing walls. In such case, the
user is not required to enter the sizing phase of overhang or wing walls.

## Default Setup :

All the inputs, including the main menu, have a default value which is defined in the first run of the program. All subsequent changes of this value by the user become the default value for the next run of the program until the user exits SHADE.

## Input Setup :

To get error-free results, the user has three opportunities to correct any incorrect input value :

1. The back space key can be used to make any immediate change whenever desired.
2. An error message is displayed with a beep and the same input line is re-displayed if the input is out of range or of a different kind (e.g. a real number in place of an integer), or if there are unrelated characters in the numeric input.
3. After completion of all related inputs in one section, a message is displayed to confirm all of the input values. The user can, at this stage, change one or all input values or proceed to confirm.

## Scaling:

The program is designed to automatically scale the graphic output according to the size of the window, or the resultant size of overhang and wing walls. The default scaling factor is 10 raster units to 1 foot.

## Unit :

The program uses feet and inches in decimal format as its input/output parameter.

In this example the following operations will be demonstrated -

1. Size the overhang in Phase-I for a 3' x 5' south facing window situated in Manhattan, KS at 390 north latitude. (For error checking purpose, use $40^{\circ}$ )
2. Use the same window above to size the wing walls in Phase-II.
3. Use the same window to determine the length of the overhang extension in Phase-III with its resulting shadow pattern.
4. View the shadow pattern for the above window in Phase-IV -
A. With only the horizontal overhang sized in Phase-I.
B. With a combination of horizontal overhang and vertical wing walls sized in Phase-II.

The first thing that is displayed on the screen after entering SHADE is the title page followed by Main Menu.

Select an Option

|  | (Item) | (Explanation Field) |
| :--- | :--- | :--- |
| P1 | PHASE-I | Sizing Overhang |
| P2 | PHASE-II | Sizing Wing Wall |
| P3 | PHASE-III | Sizing Overhang Extension |
| P4 | PHASE-IV | Shadow Pattern |
| P5 | EXIT | From SHADE to DOS |

Fig. 10 : Main Menu
The items in the Main Menu are scrolled through by using the "Up" and "Dn" arrow keys. When either of the keys is pressed, the selected item is highlighted and the explanation field is displayed. Press <Return> to select the highlighted item. An item from the menu list can also be selected by pressing the letter " P " and the number associated with that menu item followed by pressing <Return>. The default item is always PHASE-I.

Select PHASE-I and press <Return>

## PHASE-I :

A brief note about this phase and its Input specifications is displayed.

Press any key to continue
Now, begins the input section of Phase-I. Enter the following values at their respective prompts :

SITE LATITUDE : 40
WINDOW WIDTH : 3
WINDOW HEIGHT : 5
NO. OF DESIRED SHADE DAYS IN SUMMER : 60
NO. OF DESIRED SUN DAYS IN WINTER : 90
After the 'END INPUT' signal, the prompt reads -
DO YOU WANT TO CHANGE ANYTHING, Y OR N :
Check to see at this point that all the values entered are numerically correct. Then -

Enter < $\mathrm{N}>$ for no change and
Press <Return>
The resultant output is the plan, elevation, and section of the window as shown below (Fig.11). The size of overhang projection and gap is also displayed -


Fig. 11

Note: 1. The overhang extension on both sides of the window is assumed to be 1 foot for simplicity.
2. See Appendix-D for the size of overhang obtained manually using the graph developed by Energy Extension Center, Kansas State University.

## Press any key for summary of results

The summary is given as shown below :
Latitude : 40
Window width : 3
Window height : 5
Number of full shade days in summer : 60
Number of full sun days in winter: 90
Overhang projection : 2.30 ft .
Gap from top of window : 1.52 ft .
To take a look at the shadow pattern for the overhang we just sized Press any key to continue

## PHASE-IV :

This phase begins with a brief explanation, and lists the keyboard commands to be used for viewing the shadow pattern for any day of the month at one hour intervals. This list of keyboard commands can also be accessed by pressing the "F3" key, while viewing the shadow pattern.

Press any key to continue
An important note follows. The horizontal overhang or vertical wing walls must have been sized in either Phase-I or Phase-Il for this part of the program to work. Otherwise, the user must enter a predetermined size to proceed. In this example, the overhang was just sized in Phase-I. Thus -

Press any key to continue
At this stage, the user can view the shadow pattern for a combination of overhang and wing walls (choice 2), but we are interested in viewing the shadow pattern only for the overhang at this time, so -

Enter <1> at the MAKE SELECTION prompt and
Press <Return>

Another important note follows including a display of the current set of input values. The user can use any other pre-determined size of overhang at this stage, but we will use the size of the overhang just determined in Phase-I, so -

Enter <1> at the MAKE SELECTION prompt and Press <Return>
Now we are in the input section of this phase. Enter the following values at their respective prompts -

WINDOW ORIENTATION : 0
MONTH OF YEAR FOR SHADOW CASTING : 6
DAY OF MONTH FOR SHADOW CASTING : 21
Note : 1. The shadow pattern always begins with the first hour after sunrise and ends at the hour before sunset for the day chosen. This eliminates the need for entering time of day.
2. The Solar Position Charts listing altitude and azimuth angles for 0 to 64 degrees north latitudes at an interval of 8 degrees are included in Appendix-B for reference.
3. All the times used here are actual 'solar time'. Solar time is measured relative to local solar noon - the instant when the sun is exactly south (or north) of the observer. Local solar noon is usually different than local standard time which can be as much as one hour. But this can be ignored, because the length of the shaded time is the same.

After the 'END INPUT' signal -
Enter < $\mathrm{N}>$ for no change and
Press <Return>
Now, the user can see the shadow pattern for the window under investigation, with its overhang as sized in Phase-I. Since, the first hour after sunrise on June 21 for 40 degrees north latitude is 5 a.m. the values that are displayed on the screen are -

TIME OF DAY : 5
DATE : 6/21
ORIENTATION : 0.00
ALTITUDE : 4
AZIMUTH : 117

Any time of the day when the sun is not shining directly onto the wall which houses the window, the following messages are displayed :

NO SHADOW ON WALL (if the sun is still beyond the wall face after the sunrise hour)
NO SHADOW ON WALL TILL SUNSET (if the sun has gone beyond the wall face)
The other self explanatory messages are -
NO SUNRISE YET
SUNRISE HOUR - GO TO NEXT HOUR
SUNSET HOUR - TRY THE HOUR BEFORE
THE SUN IS DOWN
In this example, the sunrise hour for June 21 is 5.00 a.m.. So the first output that is displayed on the screen shows 'NO SHADOW ON WALL'. This is because the azimuth is 117 degrees east of due south, while the window is facing due south. Anytime during the day the azimuth is greater than 90 degrees there will be no shadow on the wall face. The first shadow pattern that appears on the screen is for 9.00 a.m. when the azimuth is 80 degrees and the altitude is 49 degrees (Fig. 12). The corresponding percentages of window area in shade is $28.80 \%$ and the area in sun is $71.20 \%$.

Similarly, the message 'NO SHADOW ON WALL TILL SUNSET' is displayed at 16 hours ( 4.00 p.m.), because the azimuth now is 91 degrees west of due south.


Fig. 12

Note:- $\overline{1}$. For this program all azimuth angles east of due south are considered positive, while those west of due south are negative.
2. See Appendix-A for the Heliodon test photographs to compare the shadow patterns for the same size of window at same latitude as used in this example.

The user is in complete control during this shadow simulation phase of the program. Use the following keys as indicated to analyze the effect of the overhang on the window -

| <-- | : TO PREVIOUS HOUR |
| :--- | :--- |
| --> | TO NEXT HOUR |
| ARROW UP : TO NEXT MONTH |  |
| ARROW DN | TO PREVIOUS MONTH |
| HOME | :TO FIRST HOUR AFTER SUNRISE |
| END | :TO HOUR BEFORE SUNSET |
| PG UP | :TO DECEMBER 21 |
| PG DN | : TO JUNE 21 |
| + | : ADD 5 DEG. TO ORIENTATION |
| - | :SUBTRACT 5 DEG. FROM ORIENTATION |
| F3 | : HELP |
| F7 | :TO EXIT |

The "F3" key functions as a help feature. When it is depressed it lists all the above commands for easy reference.

Pressing the "F7" key will return the user to the Main Menu.
Note : To print any screen image during this shadow simulation phase, refer to the System Overview section (pp. 28-29) of this manual.

To size the wing walls for the given window, we need to go to Phase-II of this program.

## PHASE-II:

Note : For any window facing south to have wing walls, logically, it must also have an overhang. Therefore, it is advisable to go to Phase-I before entering this phase.

Use the arrow key to go one line down in the menu list. The explanation field for PHASE-II is now highlighted.

Press <Return>
A brief note about this phase and its input requirements will be displayed on the screen. This phase of the program will work most accurately for windows facing within 30 degrees east or west of due south. For all other window orientations it would still be accurate, but the output is based on certain assumptions regarding the appropriateness and location of wing wall as explained on next page.

Press any key to continue
Another important note follows. This phase of program works only for the window values used in Phase-l. So the user must go to Phase-I if he or she has not already done so. Alternatively, it is possible to proceed without going to Phase-I, if the current values listed here are acceptable. For this example, the current values were already defined while in Phase-I. Thus -

Press any key to continue
Now you are in the input section. Enter the following values at their respective prompts :

WINDOW ORIENTATION : 0
MONTH OF YEAR FOR 100\% SHADE : 5
DAY OF MONTH FOR 100\% SHADE : 21
BEGINNING HOUR OF DAY FOR 100\% SHADE : 9
ENDING HOUR OF DAY FOR 100\% SHADE : 15
MONTH OF YEAR FOR 100\% SUN : 11
DAY OF MONTH FOR $100 \%$ SUN : 15
BEGINNING HOUR OF DAY FOR 100\% SUN : 9
ENDING HOUR OF DAY FOR $100 \%$ SUN : 15

Note : 1. If the user is sizing wing walls for a window facing between 300 and 1700 of due south then the prompt to enter the beginning hours for $100 \%$ shade (time-1) and for $100 \%$ sun (time-3) are not displayed. It is assumed that for these orientations the wing wall to the right side of window (as displayed on the screen) will not be appropriate. Similarly, for a window facing between 1900 and $330^{\circ}$ of due south, the prompts to enter the ending hours for $100 \%$ shade (time-2) and for $100 \%$ sun (time-4) are not displayed. It is assumed that the wing wall to the left of window is not appropriate.


Fig. 13 : Plan indicating the valid selection of time when the azimuth is within the range shown.
2. If a user, for a beginning hour or for an ending hour enters a time when actually the sun is behind the wall face or is at a position subtending an obtuse angle with respect to the wall face, then an error message 'INVALID SELECTION OF TIME' is displayed (Fig. 13). The user in such cases is required to change this time suitably in the next cycle of input prompts by entering <Y> after the 'END INPUT' signal.

After the 'END INPUT' signal -
press < $\mathbf{N}>$ for no change, if the values entered are numerically correct.
Press <Return>
The output displayed is the plan of window with the appropriate wing walls as shown below. The numeric wing wall projections and gaps are also shown


Fig. 14

To view the shadow pattern -
Press any key to continue
A note follows. If the user wishes to view the shadow pattern for a combination of horizontal overhang and vertical wing walls, then for reason of simplicity the sizes of both the wing walls and the overhang projections will have to be the same.

Press any key to continue
At this stage, if the right and left wing wall projections sized earlier are different, then the user has the following three options to maintain equal sizes for both wing walls for uniformity in design

1. Select the smaller of the two dimensions
2. Select the average of the two dimensions
3. Select the larger of the two dimensions

In this example, since both wing walls are of the same size, these options are not displayed.
Instead, this time the screen shows the plan, elevation, and section of the given window as shown below with appropriate overhang projection and its gap (from Phase-I), as well as the wing wall projection and its gap.

## Fig. 15



Press any key to continue
The screen shows the section of window with appropriate overhang and wingwall projections. Again, the user has the three options listed above to override the calculated dimensions.


Enter <3>, the larger of two dimensions, for this example and press <Return>
The graphic screen this time shows the plan, elevation, and section as before, kut with final projections and gaps of overhang and wing wall combination.

## PRESS ANY KEY FOR SUMMARY OF RESULTS



PLAN
Fig. 17
Press any key for a summary of the results
The final output is given as below :
SIZE OF WINDOW
LATITUDE : 40
ORIENTATION : 0.00
OVERHANG PROJECTION : 2.30'
OVERHANG GAP : $1.52^{\prime}$
WINGWALL PROJECTION : $2.30^{\prime}$
RIGHT WINGWALL GAP : $1.00^{\prime}$
LEFT WINGWALL GAP : 1.00'
To view the shadow pattern for a combination of wing walls and overhang -

Press any key to continue

This leads once more to Phase-IV, which was used to view shadow pattern for the overhang sized in Phase-I. The procedure to follow is similar to the one used before.

Press any key to continue
After reading the important note -
Press any key to continue
Since, the shadow pattern for a combination of horizontal overhang and vertical wing wall is to be viewed -

Enter <2> at the MAKE SELECTION prompt, and
Press <Return>

This is followed by another important note.
Press any key to continue
There is a list of current input values now on screen. At this moment, the user can use any other pre-determined size of wing wall projection (choice 2), but we will use the common size of overhang and wing wall projection just determined in Phase-II. So -

Enter <1> at the MAKE SELECTION prompt and press <return>
This is input section. Enter the following values at their respective prompts -

Orientation : 0 Month of Year for Shadow Casting : 5 Day of Month for Shadow Casting : 21
Again, at the END INPUT signal -
Enter <N> for no change, and Press <Return>
The first output displayed at 5.00 a.m. on June 21 for 40 degrees north latitude on the screen shows 'NO SHADOW ON WALL', because, as explained earlier, the azimuth at the first hour after sunrise is 115 degrees east of south which is greater than the wall face angle of 90 degrees. Use right arrow key to move forward until you see the first shadow pattern on the screen. This is for 8.00 a.m., at which time the azimuth is 87 degrees and the altitude is 35 degrees (Fig. $16)$. The window at this stage is $100 \%$ in shade.

Use the same keys explained before to evaluate the shadow performance for different times of the day, for different months, or for different orientations.

Pressing the "F7" key will return the user to Main Menu.

## Fig. 18



## PHASE-III:

Select Phase-III from the Main Menu. The explanation field will be highlighted.

## Press <Return>

This phase begins with a brief explanation and its input/output requirements. Since in this phase the user can size the overhang extension and view its resultant shadow pattern simultaneously, the procedure to proceed is the same as used in Phase-IV.

Press any key to continue
An important note follows. The size of the overhang must be defined by means of Phase-I for Phase-III of SHADE to work. Otherwise, the program uses the current values listed on the screen to proceed. For this example, the overhang has already been sized. Thus -

Press any key to continue
Now, you are in the input section of this phase. Enter the following values at their respective prompts -

ORIENTATION : 0
MONTH OF YEAR FOR 100\% SHADE : 5
DAY OF MONTH FOR SHADOW CASTING : 21
BEGINNING HOUR OF DAY FOR 100\% SHADE : 10
ENDING HOUR OF DAY FOR 100\% SHADE : 14
After the 'END INPUT' signal -

Enter < $\mathbf{N}>$, if all values entered are numerically -correct, and Press <Return>
As explained earlier, the operation of this section of the program is similar to Phase-IV; the only difference is that, when the user reaches the beginning or ending hour shadow pattern entered in the input section, there is a prompt at the bottom of the screen asking the user that the time before or after which $100 \%$ shade is desired be confirmed. The user at that moment has the option to change the beginning hour or ending hour (whatever is applicable), if he or she foresees that the resultant shadow pattern for the new overhang extension will not cover the window adequately.

In this example, while viewing the shadow pattern for May 21, upon reaching the shadow pattern for 10 a.m., there will be a prompt at the bottom of the screen to confirm the beginning or ending hour for 100\% shade. (Fig.19)


Fig. 19
At this point -
Enter < $\mathbf{Y}>$ to confirm, and
Press <Return>
The overhang extension to the right side of window is adjusted accordingly to be 3.60 ft . long. (Fig. 20)

Fig. 20


Similarly, upon reaching the14 hour (2 p.m.) shadow pattern, confirm the time for $100 \%$ shade, and the left extension is also adjusted to be 3.60 ft .

Note : 1. The user, when prompted to confirm the beginning or the ending hour for $100 \%$ shade, can change the time by entering < $\mathbf{N}>$ and pressing <Return>. Now, the user will be prompted to enter the new time. If the user is satisfied with the percentage of the window area in shade for the existing overhang extension, then he or she can enter a time when there is likely to be no shadow on the wall (e.g. sunrise or sunset time).
2. If the user, when prompted to confirm the beginning or the ending hour for $100 \%$ shade, confirms the time by entering $<\mathrm{Y}>$ when the window already is in $100 \%$ shade or in the optimum shade possible, then a message to that effect is displayed on the screen.

[^2]This ends the tutorial section.

## System Overview

## LOADING THE PROGRAM :

Turn the computer on and insert the SHADE disk. First, to enable the printer to print graphic output, type the following while in DOS mode, before entering SHADE -

C > GRAPHICS.COM
This file is built-in for the operating system MS-DOS/2.0. Use any other similar procedure relevant to the operating system being used. Now, change the drive from $C$ to $A$ (or $B$ whichever is appropriate) and type SHADE -
$\mathrm{C}>\mathrm{A}$ :
A > SHADE
or, if the program has been loaded on the hard drive, then just type SHADE -
C > SHADE

In a short time the title page will appear. Pressing any key then leads to the Main Menu. Now the user takes control of the program as explained in the Program Overview (pp. 8-10) and Tutorial sections (pp. 11-27) of this reference manual.

## HARDWARE REQUIREMENTS :

SHADE will run on IBM PCs or compatibles with one disk drive and 75 K of memory. It is recommended that a color monitor be used. Also, a graphics printer is necessary if hard copy is desired. The use of a hard disk drive with math co-processor will speed up the operations considerably.

## PRINTING:

A user can get a hard copy at any stage during the entire run of SHADE. Press <prt sc> while pressing the shift key on the keyboard, when the printer is ready. This command is known as 'screen dump',
which when called will print everything on the current- screen onto an attached printer without saving the contents of screen. A dot matrix printer with graphic capabilities such as Epson Fx 100, Brother HR 35, Alps ALQ 200 is necessary to get such a hard copy. The important thing to note is that, the in-built graphics file must be enabled before entering SHADE. Refer "Loading the Program" section on previous page for the procedure.

## List of User-Defined Variables

1. Latitude (L) : Integer :

Indicates the location of the site in northern or southern hemisphere. The value ranges from 00 to 900 for northern latitudes, and 00 to -900 for southern latitudes. (Refer U.S. and world maps included in Appendix-C to locate latitudes for a given place.)
2. Height of Window $(\mathrm{H})$ : Positive non-zero real : The height of the window in feet from sill level.
3. Width of Window (W) : Positive non-zero real : The width of the window in feet.
4. Number of Desired Shade Days in Summer (Ns) : Positive non-zero integer : Indicates the total number of days in summer when the window needs to be in $100 \%$ shade from sun; half of this number is before summer solstice (June 21) and half after.
5. Number of Desired Sun Days in Winter (Nw) : Positive non-zero integer : Indicates the total number of days in winter when the window needs to be in $100 \%$ sunlight; half of this number is before winter solstice (December 21) and half after.

Note: The desired number of full shade and sun days are to be determined by analyzing the regional and site modified climate of the building under consideration. Any period during the year that the temperature goes over the comfort zone ${ }^{1}$, would result in a $100 \%$ shade requirement. When the temperature drops below the comfort zone, there would be a $100 \%$ sun requirement during that period of year. Buildings which generate a significant amount of internal heat due to lights, people and equipments (an internally loaded building)

[^3]will require more days of full shade than a building without such internal loads (a skin loaded building). See "Sun, Wind and Light" by G. Z. Brown (pp. 33-35), MEEB - Seventh edition, by B.Stein et al. (pp. 34-49), and "Upsidedown" by G. Z. Brown et al. (pp. 3-21 to 3-32) for a discussion of how to determine when shade is needed for any given building.
6. Overhang Projection (P) : Positive non-zero real :

Indicates the perpendicular length of overhang projection, in feet, from the face of the wall. Although this value is achieved through the program, it can also be chosen by the user to simulate the shading pattern for any pre-determined overhang. (See fig. 4, pg. 5)
7. Overhang Gap (G): Positive non-zero real :

Indicates, in feet, the position of the bottom of the overhang from the top of window. Although this value can also be determined through the program, it can also be chosen by the user to simulate the shading pattern for any pre-determined overhang. (See fig. 4, pg. 5)
8. Overhang Extension to Right of Window (ER) : Positive non-zero real : Indicates the length of overhang, in feet, beyond the right edge of window. (See fig. 5, pg. 6)
9. Overhang Extension to Left of Window (EL) : Positive non-zero real : Indicates the length of overhang, in feet, beyond the left edge of the window. (See fig. 5, pg. 6)
10. Right Wing Wall Projection (RWWP) : Positive non-zero real : Indicates, in feet, the perpendicular projection of the right wing wall from the face of the wall. Normally derived through the program, it can also be chosen by the user who desires to see the shadow pattern simulation of a pre-determined wing wall. (See fig. 7, pg. 9)
11. Left Wing Wall Projection : (LWWP) : Positive non-zero real : Indicates, in feet, the perpendicular projection of the left wing
wall from the face of the wall. Normally derived through the program, it can also be chosen by the user who desires to see the shadow pattern simulation of a pre-determined user-defined wing wall. (See fig. 7, pg. 9)
12. Right Wing Wall Gap : (RWWG) : Positive non-zero real : Indicates, in feet, the clear gap from the right edge of the window to the right wing wall. Normally derived through the program, it can also be chosen by the user who desires to see the shadow pattern simulation of pre-determined user-defined wing wall. (See fig. 7, pg. 9)
13. Left Wing Wall Gap : (LWWG) : Positive non-zero real :

Indicates, in feet, the clear gap between the left edge of the window and the left wing wall. Normally derived through the program, it can be chosen by the user who desires to see the shadow pattern simulation of a pre-determined user-defined wing wall. (See fig. 7, pg. 9)
14. Orientation (ORIENT) : Positive real :

Indicates, in degrees, the orientation of the window due east of true south. The value ranges from 00 to 3600 .
15. Beginning Hour (AM_TIME) : Positive non-zero integer : Indicates the beginning hour of the day after which $100 \%$ shade or sun is required. The range varies from 1 to 24.
16. Ending Hour (PM_TIME) : Positive non-zero integer : Indicates the ending hour of the day before which $100 \%$ shade or sun is required. The range varies from 1 to 24.
17. Month of Year (mm) : Positive non-zero integer :

Indicates the month of year when shadow pattern is to be viewed. The range is from 1 to 12.
18. Day of Month (dd) : Positive non-zero integer: Indicates the day of the month when the shadow pattern is to be viewed. The range is from 1 to 31 .

## Future Improvements and Additions

Writing a computer program is a continuing process. No program is ever complete and there is always scope for future additions, alterations or updates. The two suggested future additions for SHADE are as follows :

## 1. HELP MENU

An active help menu can be added to be accessed at every change of screen image. The help screen shall display :
a. Brief information about all four phases.
b. All user-defined variables with brief explanation.
c. All major user-operated keyboard commands.
d. All hardware directives like save, delete, retrieve, print and their use.


Fig. 21

## 2. BALANCE POINT TEMPERATURE CALCULATION-

To get a more accurate and realistic estimate of the number of desired shade days in summer and sun days in winter, the balance point temperature can be found based on the internal heat gain analysis of the building under investigation. This analysis shall include heat generated - in terms of ${ }^{1}$ Btus per hour - by people, lighting, machines (if any), and any other heat generating source. This total heat gain when plotted against the 2 skin/volume ratio of the building gives the resulting balance point temperature. Any day the outdoor temperature goes over this balance point temperature, the building needs to be cooled; subsequently requiring $100 \%$ shade. On the other hand, if the outdoor temperature goes over the balance point temperature, the building needs to be heated; subsequently requiring $100 \%$ direct sunlight. See "Sun, Wind and Light" by G. Z. Brown (pp. 33 to 35 ), "Mechanical and Electrical Equipment for Buildings" - Seventh edition by B. Stein et al. (pp. 34 to 49), and "Upsidedown" by G. Z. Brown et al. (pp 3-21 to 3-32) for a discussion of how to determine when shade is needed for any given building.

The other possible additions to enhance the program could be as follows :
3. The main menu structure using the explanation field format could be implemented to work for all other inputs as well which appear at the beginning of each phase.
4. The ability to save the design of a window can be added for its usefulness in a real design situation. Each window design could be saved as separate file with a file name. Another good feature would be to look at the current directory and display the names of

[^4]all legal databases for selection for reading or writing the computer data files.
5. For the program to be of much use in the analysis stage of design, it would have to be able to print out tables summarizing the performance of the window designed. A table with the percentages of shading and non-shading area for a particular period of time (a day) would allow the user to compute heat gain as part of overall energy analysis of the building. These reports could be made available as a formatted display either on the screen or in a file. An alternative file format (fields separated by commas, with alphanumeric information in double quotes) would make the data available to LOTUS 1-2-3 or a database management system for further analysis.
6. There could also be an option to print the summary of the window design to a file or to a printer. Window designs could be named and dated with the current date.

## Conclusion

"...Analysis methods for solar design allow the designer or researcher to investigate and, in many cases, predict the thermal performance of a particular building or system. These tools provide an alternative to constructing costly working models and often allow an extended forecast of system behavior, under varying loads and inputs, which may not be easily attainable through a physical representation..."
(From "Microcomputer Methods for Solar Design and Analysis", A brochure developed by the Building Applications and Regulatory Support Branch of Solar Energy Research Institute.)

The author while being a teaching assistant for the course Environmental Systems in Architecture I (taught in the Department of Architecture at Kansas State University by Professor Gary Coates) felt the need to write a computer program which would speed up the task of sizing window shading devices by eliminating the use of sun charts and graphically finding the resultant size of the overhang projection and gap. The need was further felt when it was found that the personnel at the Energy Extension Center at Kansas State University were using a graphic chart developed by them to size the overhang, which was somewhat time consuming and not an attractive way to present the results to a client. The need is further compounded when it is realized that, it is hard to evaluate the shading performance of the resultant overhang over the period of the entire year unless a model is built and tested in a heliodon or by the use of other such time consuming methods. This is where SHADE takes the driver's seat and lets the user view the shadow pattern for the sized overhang and wing walls over a period of one year, and at any orientation, in no almost time. The results can also be printed using a graphics printer any time during the entire run of program.

Research was conducted to find out if there was any comparable software available in the market, before undertaking this thesis. No
such program was identified. It is hoped that SHADE will prove useful to passive solar designers.

The SHADE program is written using Turbo Pascal version 3.0 which supports a very limited use of graphic operations with little knwledge of computer programming language. It is not perfect nor is it methodically structured in its code. In other words, it could have probably been lot smaller and faster in its run, if it had been optimized using precise methods. The program has been tested to run successfully by some of the users (the user response has been included in the Appendix-F) and compared with results of an extensive model test inside the Kansas State University, Department of Architecture heliodon. The results in the form of photographs are included in the Appendix-A. Also, included in the Appendix-B are the solar position charts for various latitudes. It is possible that SHADE may still have some bugs in it, which went undetected. If such an error is encountered, the user is advised to reboot the system and start with a different set of values.

In conclusion, it can be affirmed that SHADE will save a considerable amount of time for the tasks that it is designed to address, if used correctly and with care.

## Appendix

## A. Heliodon Test Results

The photographs of the test inside heliodon at Department of Architecture, Kansas state University for following data are included here.

Latitude $=40$ degrees north
Window width $=3 \mathrm{ft}$.
window height $=5 \mathrm{ft}$.
Overhang projection $=2.30 \mathrm{ft}$.
Gap from top of window $=1.52 \mathrm{ft}$.
Orientation = 0 degrees (facing due south)

June 21 -->


March/Sept. 21 -->


Dec. 21 -->

10 a.m.
11 a.m.
12 p.m.

## B. Solar Position Charts

For 0 to 64 degrees North latitudes at an interval of 8 degrees are included here listing the solar altitude and azimuth angles for 21st day of each month.

Reproduced from - "ASHRAE Fundamentals Handbook", 1981.

Table 2 Solar Position and Related Angles for 0 Deg North Latitude

|  | Solar Time | Solar <br> Position |  | Profile (Shadow Line) Angles |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | Angles of Incidence Vertical Surfaces |  |  |  |  |  |  |  |  | $\begin{aligned} & \begin{array}{l} \text { Solar } \\ \text { Time } \end{array} \\ & \hline \mathbf{P M} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DATE | AM | ALT | AZ | N | NNE | NE. | ENE | E | ESE | SE | SSE | 5 | SSH | SH | HSW | N | NTE | NE | ENE | E | ESE | SE | SSE | S | SSW | SW | HSW | HOR |  |
| DEC | 7 | 14 | 66 |  |  | 35 | 20 | 15 | 14 | 15 | 19 | 31 | 83 |  |  |  |  | 70 | 48 | 28 | 14 | 25 | 45 | 67 | 88 |  |  | 76 |  |
|  | 8 | 27 | 63 |  |  | 59 | 38 | 30 | 27 | 29 | 34 | 49 | 82 |  |  |  |  | 74 | 54 | 37 | 28 | 33 | 48 | 67 | 86 |  |  | 63 | 4 |
|  | 9 | 40 | 58 |  |  | 75 | 59 | 45 | 41 | 41 | 46 | 58 | 80 |  |  |  |  | 80 | 63 | 50 | 41 | 42 | 52 | 67 | 83 |  |  | 50 |  |
|  | 10 | 53 | 49 |  |  | 87 | 71 | 60 | 54 | 53 | 56 | 63 | 76 |  |  |  |  | 88 | 74 | 63 | 55 | 53 | 57 | 67 | 79 |  |  | 37 | 2 |
|  | 11 | 62 | 31 |  |  |  | 86 | 75 | 67 | 63 | 63 | 66 | 3 | 83 |  |  |  |  | 86 | 76 | 68 | 63 | 63 | 67 | 74 | 83 |  | 28 | 2 |
|  | 12 | 67 | 0 |  |  |  | 86 | 90 | 81 | 73 | 68 | 67 | 68 | 73 | 81 |  |  |  |  | 90 | 81 | 74 | 68 | 67 | 68 | 74 | 81 | 23 | 12 |
| $\begin{gathered} \text { JAN } \\ \stackrel{+}{\mathrm{NO}} \end{gathered}$ | 7 | 14 | 69 |  | 83 | 31 | 19 | 15 | 14 | 15 | 20 | 35 |  |  |  |  | 88 | 66 | 45 | 25 | 14 | 28 | 48 | 70 |  |  |  | -6 | 5 |
|  | 8 | 28 | 67 |  |  | 55 | 37 | 30 | 28 | 30 | 37 | 54 | 89 |  |  |  |  | 71 | 52 | 36 | 28 | 35 | 51 | 70 | 90 |  |  | 62 | 4 |
|  | 9 | 42 | 63 |  |  | 71 | 54 | 45 | 42 | 43 | 49 | 63 | 85 |  |  |  |  | 77 | 61 | 48 | 42 | 45 | 55 | 70 | 86 |  |  | 48 | 3 |
|  | 10 | 54 | 54 |  |  | 84 | 70 | 60 | 55 | 55 | 59 | 67 | 80 |  |  |  |  | 85 | 72 | 62 | 56 | 55 | 60 | 70 | 82 |  |  | 36 | 2 |
|  | 11 | 65 | 35 |  |  |  | 84 | 75 | 69 | 65 | 66 | 69 | 76 | 86 |  |  |  |  | 85 | 76 | 69 | 66 | 66 | 70 |  | 16 |  | 25 | 1 |
|  | 12 | 70 | 0 |  |  |  |  | 90 | 82 | 76 | 71 | 70 | 71 | 76 | 82 |  |  |  |  | 90 | 82 | 76 | 72 | $\bigcirc$ | $\because$ | -6 | 82 | 20 | 12 |
| $\begin{aligned} & \text { FEB } \\ & + \\ & \mathrm{OCT}^{2} \end{aligned}$ | 7 | 15 | 79 |  | 53 | 25 | 18 | 15 | 15 | 18 | 25 | $\leq 4$ |  |  |  |  | 79 | 57 | 36 | 18 | 19 | 37 | 58 | -9 |  |  |  | -s | 5 |
|  | 8 | 29 | 78 |  | 73 | 46 | 35 | 30 | 30 | 34 | 45 | 69 |  |  |  |  | 81 | 62 | 14 | 32 | 31 | 43 | 60 | -9 |  |  |  | 61 | 4 |
|  | 9 | 44 | 75 |  | 82 | 63 | 51 | 45 | 44 | 48 | 58 | 75 |  |  |  |  | 85 | 69 | S | 46 | 4 | 51 | (a) | -4 |  |  |  | 46 | 3 |
|  | 10 | ¢8 | 69 |  | 89 | 76 | 66 | s0 | 58 | 61 | 67 | -8 |  |  |  |  | 89 | ${ }^{-8}$ | 68 | 01 | 58 | 61 | 69 | -9 |  |  |  | :2 | 2 |
|  | 11 | 72 | 54 |  |  | 87 | 80 | 75 | 72 | 72 | 74 | -4 | 8 |  |  |  |  | 87 | 81 | $\checkmark$ | $\because$ | $\because$ | -4 | $-9$ | \% |  |  | 18 | i |
|  | 12 | 79 | 0 |  |  |  |  | ¢ | 86 | 82 | 80 | -9 | 80 | s: | 86 |  |  |  |  | * | 86 | 82 | 80 | -9 | 8 | st |  | 11 | に |
| $\begin{gathered} \text { MAR } \\ + \\ \text { SEP } \end{gathered}$ | 7 | 15 | 90 | 90 | 35 | 21 | 16 | 15 | 16 | 21 | 35 | + |  |  |  | 90 | 08 | 4 | 2 | 15 | :- | 4 | 68 | 2) |  |  |  | - | $\leqslant$ |
|  | 8 | 30 | *) | 90 | 56 | 39 | 32 | 30 | 32 | 39 | 56 | 4) |  |  |  | () | $\square$ | 5 | - | : 0 | 3 | 52 | $\because$ | ( 1 |  |  |  | ${ }^{0}$ | 4 |
|  | 9 | 45 | 90 | 90 | 69 | s | 47 | 45 | 47 | 55 | 69 | 90 |  | . |  | * | $\because$ | (0) | 49 | 45 | 49 | (0) | 74 | 40 |  |  |  | 45 | 3 |
|  | 10 | 60 | 90 | 90 | -8 | 68 | 62 | (0) | 62 | 68 | \% | ( ${ }^{\text {a }}$ |  |  |  | 90 | -9 | 69 | 62 | 80 | 62 | 69 | 79 | 90 |  |  |  | 30 | 2 |
|  | 11 | $\cdots$ | 40 | * | 8. | 79 | 76 | 75 | 76 | - 9 | $\stackrel{5}{4}$ | 40 |  |  |  | * | 84 | 79 | -6 | - | -6 | -9 | 84 | 90 |  |  |  | 15 | 1 |
|  | 12 | 90 | *) | 0 | 90 | 90 | 90 | 90 | 4, | 90 | 90 | 4) |  |  |  | 90 | 9 | 40 | 90 | *) | 9 | 90 | $4)$ | \%) |  |  |  | 0 | 12 |
| $\begin{gathered} \text { APR } \\ ++ \\ \text { AUG } \end{gathered}$ | , | 15 | 102 | $\because$ | $\cdots$ | 17 | 15 | 15 | 18 | 26 | $s$ |  |  |  |  | -8 | 5 | 36 | 18 | 19 | 37 | 58 | 80 |  |  |  |  | 7 | 5 |
|  | 8 | 29 | 103 | 68 | $\pm$ | 33 | 30 | 30 | 35 | 47 | -4 |  |  |  |  | -8 | 59 | 42 | 31 | 32 | 45 | 63 | 82 |  |  |  |  | 61 | 4 |
|  | 9 | 44 | 106 | -4 | 5 | 48 | 44 | 45 | $\leq 1$ | 63 | 83 |  |  |  |  | -8 | 63 | 51 | 4 | 46 | 56 | 70 | 85 |  |  |  |  | 46 | 3 |
|  | 10 | 58 | 112 | $\bigcirc$ | $\infty$ | 60 | 58 | 60 | 66 | 76 | 90 |  |  |  |  | 78 | 68 | 61 | 58 | 61 | 68 | 78 | 90 |  |  |  |  | 32 | 2 |
|  | 11 | 71 | 128 | 78 | 73 | 7 | 72 | 75 | 81 | 88 |  |  |  |  |  | 78 | i4 | 71 | 72 | is | 81 | 88 |  |  |  |  |  | 19 | , |
|  | 12 | 78 | 180 | 78 | 79 | 82 | 86 | 90 |  |  |  |  |  |  |  | 78 | 79 | 82 | 86 | 90 |  |  |  |  |  |  |  | 12 | 12 |
| $\begin{gathered} \text { MAY } \\ + \\ \text { JUL } \end{gathered}$ | 7 | 14 | 111 | 35 | 20 | 15 | 14 | 15 | 19 | 31 | 83 |  |  |  |  | 70 | 48 | 28 | 14 | 25 | 45 | 66 | 88 |  |  |  |  | 76 | 5 |
|  | 8 | 28 | 113 | 54 | 37 | 30 | 28 | 30 | 37 | 55 |  |  |  |  |  | 70 | 51 | 35 | 28 | 36 | 52 | 71 |  |  |  |  |  | 62 | 4 |
|  | 9 | 42 | 117 | 63 | 49 | 43 | 42 | 45 | 54 | 71 |  |  |  |  |  | $\bigcirc$ | 55 | 45 | 42 | 48 | 61 | 77. |  |  |  |  |  | 48 | 3 |
|  | 10 | 54 | 126 | 67 | 59 | 55 | 55 | 60 | 70 | 84 |  |  |  |  |  | 70 | 60 | 55 | 56 | 62 | 72 | 85 |  |  |  |  |  | 36 | 2 |
|  | 11 | 65 | 145 | 09 | (6) | 65 | 69 | 75 | 84 |  |  |  |  |  |  | $\bigcirc$ | 66 | 66 | 69 | 76 | 85 |  |  |  |  |  |  | 25 |  |
|  | 12 | 70 | 180 | 70 | 71 | 76 | 82 | 90 |  |  |  |  |  |  |  | 70 | 72 | 76 | 82 | 90 |  |  |  |  |  |  |  | 20 | 12 |
| JUN | 7 | 14 | 114 | 31 | 19 | 15 | 14 | 15 | 20 | 35 |  |  |  |  |  | 67 | 45 | 25 | 14 | 28 | 48 | 70 |  |  |  |  |  | 76 | 5 |
|  | 8 | 27 | 117 | 49 | 34 | 29 | 27 | 30 | 38 | 59 |  |  |  |  |  | 67 | 48 | 33 | 28 | 37 | 54 | 74 |  |  |  |  |  | 63 | 4 |
|  | 9 | 40 | 122 | 58 | 46 | 41 | 41 | 45 | 55 | 75 |  |  |  |  |  | 67 | 52 | 42 | 41 | 50 | 63 | 80 |  |  |  |  |  | 50 | 3 |
|  | 10 | 53 | 131 | 63 | 56 | 53 | 54 | 60 | 71 | 87 |  |  |  |  |  | 67 | 57 | 53 | 55 | 63 | 74 | 88 |  |  |  |  |  | 37 | 2 |
|  | 11 | 62 | 149 | 66 | 63 | 63 | 67 | 75 | 86 |  |  |  |  |  |  | 67 | 63 | 63 | 68 | 76 | 86 |  |  |  |  |  |  | 28 | 1 |
|  | 12 | 67 | 180 | 62 | 68 | 73 | 81 | 90 |  |  |  |  |  |  |  | 67 | 68 | 74 | 81 | 90 |  |  |  |  |  |  |  | 23 | 12 |
|  |  |  |  | N | NWW | NW | HNW | W | WSW | SW | SSW | S | SSE | SE | ESE | N | NiNW | NH | HNW | w | HSW | SW | SSW | S | SSE | SE | ESE | HOR | PM |

Dates vary year to year within plus or minus two days of the twenty first day of the month

Table 3 Solar Position and Related Angles for 8 Deg North Latitude


Dates vary year to year within plus or minus two days of the tuenty.first day of the month.


Table 5 Solar Position and Related Angles for 24 Deg North Latitude

es vary year to year within plus or minus two days of the twenty-first day of the month.

CHAPTER 27
1981 Fundamentals Handbook
Table 6 Solar Position and Related Angles for 32 Deg North Latitude



Dates vary year to year within plus or minus two days of the twenty-first day of the month

## Fenestration

Table 8 Solar Position and Related Angles for 48 Deg North Latitude

|  | Solar Tlume | Pod |  |  |  |  | Profl | Mil (S | Shadow | Lne) | Angles |  |  |  |  |  |  |  |  |  | les of | Incld | ence V | ertical | al Surfa | aces |  |  | Solar <br> Time |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Date | AM | ALT | AZ | N | NNE | NE | ENE | E | ESE | SE | SSE | S | SSW | SW | WSw | N | NNE | NE | ENE | E | ESE | SE | SSE | S | SSW | SW | WSW | HOR | PM |
| DEC | 8 | 1 | 53 |  |  | 5 | 1 | 1 |  | 1 |  | 1 | 2 |  |  |  |  | 82 | 60 | 37 | 15 | 8 | 30 | 53 | 75 |  |  | 89 | 4 |
|  | 9 | 8 | 41 |  |  |  | 24 | 12 | 9 | 8 | 8 | 10 |  |  |  |  |  |  | 72 | 50 | 28 | 9 | 20 | 42 | 64 | 86 |  | 82 | 3 |
|  | 10 | 14 | 28 |  |  |  | 68 | 27 | 17 | 14 | 14 | 15 | 21 | 40 |  |  |  |  | 84 | 63 | 41 | 22 | 15 | 31 | 52 | 74 |  | 76 | 2 |
|  | 11 | 17 | 14 |  |  |  |  | 51 | 27 | 20 | 17 | 18 | 21 | 31 | 66 |  |  |  |  | 76 | 55 | 35 | 19 | 22 | 40 | 61 | 82 | 73 | 1 |
|  | 12 | 19 | 20 |  |  |  |  | 90 | 41 | 25 | 20 | 19 | 20 | 25 | 41 |  |  |  |  | 90 | 69 | 48 | 29 | 19 | 29 | 48 | 69 | 71 | 12 |
| JAN | 8. | 3 | 59 |  |  | 20 | 6 | , | 4 | 4 | 4 | 6 | 15 |  |  |  |  | 80 | 58 | 36 | 13 | 10 | 32 | 55 | 77 |  |  | 87 | 4 |
| + | 9 | 11 | 43 |  |  |  | 29 | 16 | 12 | 11 | 12 | 15 | 25 | 78 |  |  |  |  | 70 | 48 | 27 | 11 | 23 | 44 | 66 | 88 |  | 79 | 3 |
| NOV | 10 | 17 | 29 |  |  |  | 68 | 32 | 21 | 17 | 17 | 19 | 26 | 48 |  |  |  |  | 83 | 62 | 41 | 23 | 18 | 34 | 54 | 75 |  | 73 | 2 |
|  | 11 | 21 | 15 |  |  |  |  | 55 | 32 | 24 | 21 | 21 | 25 | 37 | 71 |  |  |  |  | 76 | 55 | 36 | 22 | 25 | 42 | 62 | 83 | 69 | 1 |
|  | 12 | 22 | 0 |  |  |  |  | 90 | 47 | 30 | 24 | 22 | 24 | 30 | 47 |  |  |  |  | 90 | 69 | 49 | 31 | 22 | 31 | 49 | 69 | 68 | 12 |
| FEB | 7 | 2 | 72 |  | 23 | 4 | 2 | 2 | 2 | 2 | 3 | 6 |  |  |  |  | 86 | 63 | 41 | 18 | 5 | 27 | 49 | 72 |  |  |  | 88 | 5 |
|  | 8 | 11 | 60 |  |  | 37 | 18 | 13 | 11 | 11 | 14 | 21 | 56 |  |  |  |  | 75 | 53 | 32 | 13 | 19 | 39 | 61 | 83 |  |  | 79 | 4 |
| OCT | 9 | 19 | 47 |  |  | 83 | 39 | 25 | 20 | 19 | 21 | 27 | 45 |  |  |  |  | 88 | 67 | 46 | 27 | 19 | 31 | 50 | 71 |  |  | 71 | 3 |
|  | 10 | 25 | 33 |  |  |  | 69 | 41 | 30 | 26 | 26 | 30 | 40 | 66 |  |  |  |  | 81 | 61 | 42 | 28 | 27 | 41 | 59 | 79 |  | 65 | 2 |
|  | 11 | 30 | 17 |  |  |  |  | 63 | 42 | 33 | 30 | 31 | 36 | 51 | 81 |  |  |  |  | 75 | 56 | 40 | 30 | 34 | 48 | 66 | 85 | 60 |  |
|  | 12 | 31 | 0 |  |  |  |  | 90 | 58 | 41 | 33 | 31 | 33 | 41 | 58 |  |  |  |  | 90 | 71 | 53 | 38 | 31 | 38 | 53 | 71 | 59 | 12 |
| MAR | 7 | 10 | 79 |  | 42 | 18 | 12 | 10 | 10 | 12 | 18 | 42 |  |  |  |  | 79 | 57 | 35 | 15 | 15 | 35 | 57 | 79 |  |  |  | 80 | 5 |
| $\stackrel{+}{+}$ | 8 | 20 | 67 |  |  | 44 | 27 | 21 | 20 | 21 | 26 | 42 | 88 |  |  |  |  | 70 | 49 | 30 | 20 | 29 | 48 | 68 88 | 89 |  |  | 70 | 4 |
| SEP | 9 | 28 | 53 |  |  | 75 | 46 | 34 | 29 | 28 | 32 | 42 | ${ }^{66}$ |  |  |  |  | 83 | 63 | 45 | 31 | 29 | 41 | 58 | 78 |  |  | 62 | 3 |
|  | 10 | 35 | 38 |  |  |  | 70 | 49 | 39 | 36 | 36 | 42 | 59 | 80 |  |  |  |  | 78 | 60 | 45 | 36 | 38 | 50 | 66 | 84 |  | 55 | 2 |
|  | 11 | 40 | 20 |  |  |  |  | 68 | 52 | 43 | 40 | 42 | 49 | 63 | 87 |  |  |  |  | 75 | 59 | 46 | 40 | 44 | 56 | 71 | 88 | 50 | 1 |
|  | 12 | 42 | 0 |  |  |  |  | 90 | 67 | 52 | 44 | 42 | 44 | 52 | 67 |  |  |  |  | 90 | 73 | 58 | 47 | 42 | 47 | 58 | 73 | 48 | 12 |
| APR | 6 | 9 | 98 | 48 | 17 | 11 | 9 | 9 | 10 | 14 | 31 |  |  |  |  | 82 | 60 | 38 | 17 | 12 | 31 | 53 | 75 |  |  |  |  | 81 | 6 |
|  | 7 | 19 | 87 |  | 46 | 27 | 20 | 19 | 20 | 24 | 38 | 80 |  |  |  |  | 72 | 51 | 31 | 19 | 27 | 45 | 66 | 87 |  |  |  | 71 | 5 |
| AUG | 8 | 29 | 75 |  | 77 | 47 | 34 | 29 | 29 | 32 | 42 | 64 |  |  |  |  | 84 | 64 | 46 | 32 | 29 | 40 | 58 | 77 |  |  |  | 61 |  |
|  | 9 | 38 | 61 |  |  | 70 | 51 | 42 | 38 | 39 | 45 | 58 | 82 |  |  |  |  | 77 | 60 | 46 | 38 | 41 | 52 | 68 | 85 |  |  | 52 | 3 |
|  | 10 | 46 | 45 |  |  |  | 70 | 56 | 48 | 46 | 48 | 55 | 69 | 90 |  |  |  |  | 75 | 61 | 50 | 46 | 50 | 60 | 74 | 90 |  | 44 | 2 |
|  | 11 | 51 | 24 |  |  |  | 89 | 72 | 60 | 53 | 52 | 54 | 61 | 74 |  |  |  |  | 89 | 75 | 63 | 54 | 52 | 55 | 65 | 77 |  | 39 | 1 |
|  | 12 | 54 | 0 |  |  |  |  | 90 | 74 | 62 | 56 | 54 | 56 | 62 | 74 |  |  |  |  | 90 | 77 | 65 | 57 | 54 | 57 | 65 | 77 | 36 | 12 |
| MAY | 5 | 5 | 114 | 13 | 7 | 6 | 5 | 6 | 8 | 15 |  |  |  |  |  | 66 | 43 | 21 | 6 | 25 | 47 | 69 |  |  |  |  |  | 85 | 7 |
| JUL | 6 | 15 | 104 | 48 | 24 | 17 | 15 | 15 | 18 | 27 | 60 |  |  |  |  | 77 | 55 | -34 | 17 | 20 | 39 | 60 | 81 |  |  |  |  | 75 | , |
|  | 7 | 25 | 93 | 83 | 47 | 32 | 26 | 25 | 27 | 34 | 54 |  |  |  |  | 87 | 67 | 47 | 31 | 25 | 35 | 53 | 72 |  |  |  |  | 65 | 5 |
|  | 8 | 35 | 82 |  | 71 | 49 | 39 | 35 | 35 | 41 | 53 | 78 |  |  |  |  | 78 | 61 | 45 | 36 | 37 | 49 | 65 | 83 |  |  |  | 55 | 4 |
|  | 9 | 44 | 68 |  | 89 | 68 | 54 | 46 | 44 | 47 | 54 | 69 |  |  |  |  | 89 | 74 | 59 | 48 | 44 | 49 | 60 | 75 |  |  |  | 46 | 3 |
|  | 10 | 53 | 51 |  |  | 85 | 70 | 60 | 54 | 53 | 57 | 65 | 78 |  |  |  |  | 86 | 73 | 62 | 55 | 53 |  | 68 |  |  |  | 37 |  |
|  | 11 | 59 | 29 |  |  |  | 86 | 74 | 65 | 61 | 60 | 63 | 70 | 81 |  |  |  |  | 87 | 76 | 67 | 61 | 60 | 64 | 71 | 82 |  | 31 | 1 |
|  | 12 | 62 | 0 |  |  |  |  | 90 | 78 | 69 | 64 | 62 | 64 | 69 | 78 |  |  |  |  | 90 | 80 | 71 | 64 | 62 | 64 | 71 | 80 | 28 | 12 |
| JUN | 5 |  | 117 |  |  |  | 8 | 9 | 12 | 24 |  |  |  |  |  | 64 | 42 | 20 | 9 | 28 | 50 | 72 |  |  |  |  |  | 82 | 7 |
|  | 6 | 17 | 106 | 48 | 26 | 19 | 17 | 18 | 22 | 33 | 70 |  |  |  |  | 75 | 53 | 33 | 18 | 23 | 42 | 63 | 84 |  |  |  |  | 73 | 6 |
|  | 7 | 27 | 96 | 79 | 47 | 33 | 28 | 27 | 30 | 39 | 61 |  |  |  |  | 85 |  | 46 |  | 28 |  | 56 | 75 |  |  |  |  | 63 | 5 |
|  | 8 | 37 | 85 |  | 69 | 50 | 41 | 37 | 38 | 44 | 58 | 83 |  |  |  |  | 76 | 59 | 45 | 37 | 40 | 52 | 68 | 86 |  |  |  | 53 | 4 |
|  | 9 | 47 | 72 |  | 86 | 67 | 55 | 48 | 47 | 50 | 58 | 74 |  |  |  |  | 87 | 72 | 59 | 50 | 47 | 52 | 63 | 78 |  |  |  | 43 | 3 |
|  | 10 | 56 | 55 |  |  | 83 | 70 | 71 | 56 | 56 | 60 | 69 | 81 |  |  |  |  | 85 | 73 | ${ }^{63}$ | 57 | 56 | 62 | 71 | 83 |  |  | 34 | 2 |
|  | 11 | 63 | 31 |  |  |  | 86 | 75 | 67 | 63 | 63 | 66 | 73 | 83 |  |  |  |  | 86 | 76 | 68 | 64 | 63 | 67 | 74 | 84 |  | 27 | 1 |
|  | 12 | 65 | 0 |  |  |  |  | 90 | 80 | 72 | 67 | 65 | 67 | 72 | 80 |  |  |  |  | 90 | 81 | 73 | 67 | 65 | 67 | 73 | 81 | 25 | 12 |
|  |  |  |  | N | NNW | NW | WNW | w | WSW | SW | SSW | S | SSE | SE | ESE | N | NNW | NW | WNW | w | wSw | SW | SSW | S | SSE | SE | ESE | HOR | PM |

Dates vary year to year within plus or minus two days of the iwenty-first day of the month

Table 9 Solar Position and Related Angles for 56 Deg North Latitude

|  | Solar Tlme | Solar Position |  | Proflle (Shadow Line) Angles |  |  |  |  |  |  |  |  |  |  |  |  | Angles of Incidence Vertical Surfaces |  |  |  |  |  |  |  |  |  |  |  | Solar Time$\qquad$PM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Date | AM | ALT | AZ | N | NNE | NE | ENE | E | ESE | SE | SSE | S | SSW | SW | wSW | N | NNE | NE | ENE | E | ESE | SE | SSE | S | SSW | SW | wsw | HOR |  |
| DEC | $\begin{array}{r} 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{r} 2 \\ 7 \\ 10 \\ 11 \end{array}$ | $\begin{gathered} 40 \\ 27 \\ 14 \\ 0 \end{gathered}$ |  |  |  | $\begin{array}{r} 6 \\ 53 \end{array}$ | $\begin{array}{r} 3 \\ 14 \\ 35 \\ 90 \end{array}$ | $\begin{array}{r} \mathbf{2} \\ 9 \\ 16 \\ 26 \end{array}$ | $\begin{array}{r} 2 \\ 7 \\ 11 \\ 15 \end{array}$ | $\begin{array}{r} 2 \\ 7 \\ 10 \\ 11 \end{array}$ | $\begin{array}{r} 2 \\ 7 \\ 10 \\ 11 \end{array}$ | $\begin{array}{r} 4 \\ 10 \\ 12 \\ 11 \end{array}$ | $\begin{aligned} & 23 \\ & 21 \\ & 18 \\ & 15 \end{aligned}$ | $\begin{aligned} & 48 \\ & 26 \end{aligned}$ |  |  |  | $\begin{aligned} & 72 \\ & 85 \end{aligned}$ | $\begin{aligned} & 50 \\ & 63 \\ & 76 \\ & 90 \end{aligned}$ | $\begin{aligned} & 27 \\ & 40 \\ & 54 \\ & 68 \end{aligned}$ | $\begin{array}{r} 5 \\ 19 \\ 32 \\ 46 \end{array}$ | $\begin{array}{r} 18 \\ 8 \\ 13 \\ 25 \end{array}$ | $\begin{aligned} & 41 \\ & 28 \\ & 17 \\ & 11 \end{aligned}$ | $\begin{aligned} & 63 \\ & 50 \\ & 37 \\ & 25 \end{aligned}$ | $\begin{aligned} & 85 \\ & 73 \\ & 59 \\ & 46 \end{aligned}$ | $\begin{aligned} & 82 \\ & 68 \end{aligned}$ | $\begin{aligned} & 88 \\ & 88 \\ & 80 \\ & 79 \end{aligned}$ | 3 2 1 12 |
| $\begin{gathered} \text { JAN } \\ + \\ \text { NOV } \end{gathered}$ | $\begin{array}{r} 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{r} 5 \\ 10 \\ 13 \\ 14 \end{array}$ | $\begin{array}{r} 42 \\ 28 \\ 14 \\ 0 \end{array}$ |  |  |  | $\begin{aligned} & 15 \\ & 59 \end{aligned}$ | $\begin{array}{r} 8 \\ 20 \\ 43 \\ 90 \end{array}$ | $\begin{array}{r} 6 \\ 13 \\ 21 \\ 33 \end{array}$ | $\begin{array}{r} 5 \\ 10 \\ 15 \\ 19 \end{array}$ | $\begin{array}{r} 5 \\ 10 \\ 13 \\ 15 \end{array}$ | $\begin{aligned} & 7 \\ & 11 \\ & 13 \\ & 14 \end{aligned}$ | $\begin{aligned} & 12 \\ & 15 \\ & 16 \\ & 15 \end{aligned}$ | $\begin{aligned} & 58 \\ & 31 \\ & 24 \\ & 19 \end{aligned}$ | $\begin{aligned} & 59 \\ & 33 \end{aligned}$ |  |  |  | $\begin{aligned} & 71 \\ & 84 \end{aligned}$ | $\begin{aligned} & 48 \\ & 62 \\ & 76 \\ & 90 \end{aligned}$ | $\begin{aligned} & 26 \\ & 40 \\ & 54 \\ & 68 \end{aligned}$ | $\begin{array}{r} 6 \\ 19 \\ 33 \\ 47 \end{array}$ | $\begin{aligned} & 20 \\ & 12 \\ & 15 \\ & 26 \end{aligned}$ | $\begin{aligned} & 42 \\ & 30 \\ & 19 \\ & 14 \end{aligned}$ | $\begin{aligned} & 64 \\ & 52 \\ & 39 \\ & 26 \end{aligned}$ | $\begin{aligned} & 87 \\ & 74 \\ & 60 \\ & 47 \end{aligned}$ | 82 68 | $\begin{aligned} & 85 \\ & 80 \\ & 77 \\ & 76 \end{aligned}$ | 3 2 1 12 |
| $\begin{aligned} & \text { FEB } \\ & +\underset{O C T}{ } \end{aligned}$ | $\begin{array}{r} 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{r} 7 \\ 13 \\ 19 \\ 22 \\ 23 \end{array}$ | $\begin{gathered} 59 \\ 46 \\ 31 \\ 16 \\ 0 \end{gathered}$ |  |  | $\begin{aligned} & 26 \\ & 88 \end{aligned}$ | $\begin{aligned} & 11 \\ & 31 \\ & 66 \end{aligned}$ | $\begin{array}{r} 8 \\ 19 \\ 33 \\ 56 \\ 90 \end{array}$ | $\begin{array}{r} 7 \\ 14 \\ 23 \\ 33 \\ 48 \end{array}$ | $\begin{array}{r} 7 \\ 13 \\ 19 \\ 25 \\ 31 \end{array}$ | $\begin{array}{r} 8 \\ 15 \\ 19 \\ 22 \\ 25 \end{array}$ | $\begin{aligned} & 13 \\ & 19 \\ & 22 \\ & 23 \\ & 23 \end{aligned}$ | $\begin{aligned} & 39 \\ & 33 \\ & 30 \\ & 27 \\ & 25 \end{aligned}$ | $\begin{aligned} & 55 \\ & 40 \\ & 31 \end{aligned}$ | $\begin{aligned} & 74 \\ & 48 \end{aligned}$ |  |  | ${ }_{89} 8$ | $\begin{aligned} & 54 \\ & 68 \\ & 82 \end{aligned}$ | $\begin{aligned} & 32 \\ & 46 \\ & 61 \\ & 75 \\ & 90 \end{aligned}$ | $\begin{aligned} & 11 \\ & 26 \\ & 40 \\ & 55 \\ & 69 \end{aligned}$ | $\begin{aligned} & 16 \\ & 13 \\ & 23 \\ & 36 \\ & 49 \end{aligned}$ | $\begin{aligned} & 37 \\ & 27 \\ & 21 \\ & 23 \\ & 32 \end{aligned}$ | $\begin{aligned} & 59 \\ & 47 \\ & 36 \\ & 27 \\ & 23 \end{aligned}$ | $\begin{aligned} & 82 \\ & 69 \\ & 56 \\ & 43 \\ & 32 \end{aligned}$ | $\begin{aligned} & 77 \\ & 63 \\ & 49 \end{aligned}$ | 84 69 | $\begin{aligned} & 83 \\ & 77 \\ & 71 \\ & 68 \\ & 67 \end{aligned}$ | 4 3 2 1 12 |
| $\begin{gathered} \text { MAR } \\ \stackrel{+}{\text { SEP }} \end{gathered}$ | $\begin{array}{r} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{gathered} 8 \\ 16 \\ 16 \\ 23 \\ 29 \\ 33 \\ 34 \end{gathered}$ | $\begin{gathered} 77 \\ 64 \\ 50 \\ 35 \\ 18 \\ 0 \end{gathered}$ |  | 40 | $\begin{aligned} & 15 \\ & 41 \\ & 78 \end{aligned}$ | $\begin{aligned} & 10 \\ & 24 \\ & 43 \\ & 69 \end{aligned}$ | $\begin{array}{r} 9 \\ 18 \\ 29 \\ 44 \\ 64 \\ 90 \end{array}$ | $\begin{gathered} 8 \\ 16 \\ 14 \\ 33 \\ 43 \\ 45 \end{gathered}$ | $\begin{aligned} & 10 \\ & 17 \\ & 23 \\ & 29 \\ & 36 \\ & 44 \end{aligned}$ | $\begin{aligned} & 14 \\ & 21 \\ & 26 \\ & 30 \\ & 33 \\ & 36 \end{aligned}$ | $\begin{aligned} & 34 \\ & 34 \\ & 34 \\ & 34 \\ & 34 \\ & 34 \end{aligned}$ | $\begin{aligned} & 80 \\ & 56 \\ & 46 \\ & 40 \\ & 36 \end{aligned}$ | $\begin{aligned} & 72 \\ & 59 \\ & 44 \end{aligned}$ | $\begin{aligned} & 83 \\ & 60 \end{aligned}$ |  | 80 | $\begin{aligned} & 58 \\ & 71 \\ & 75 \end{aligned}$ | $\begin{aligned} & 36 \\ & 50 \\ & 65 \\ & 79 \end{aligned}$ | $\begin{aligned} & 15 \\ & 30 \\ & 45 \\ & 60 \\ & 75 \\ & 90 \end{aligned}$ | $\begin{aligned} & 13 \\ & 17 \\ & 29 \\ & 43 \\ & 57 \\ & 72 \end{aligned}$ | $\begin{aligned} & 33 \\ & 25 \\ & 24 \\ & 31 \\ & 41 \\ & 54 \end{aligned}$ | $\begin{aligned} & 55 \\ & 44 \\ & 36 \\ & 31 \\ & 33 \\ & 40 \end{aligned}$ | $\begin{aligned} & 78 \\ & 66 \\ & 54 \\ & 44 \\ & 37 \\ & 34 \end{aligned}$ | $\begin{aligned} & 87 \\ & 74 \\ & 62 \\ & 50 \\ & 40 \end{aligned}$ | $\begin{aligned} & 81 \\ & 67 \\ & 54 \end{aligned}$ | $\begin{aligned} & 86 \\ & 72 \end{aligned}$ | $\begin{aligned} & 82 \\ & 74 \\ & 67 \\ & 61 \\ & 57 \\ & 56 \end{aligned}$ | $\begin{array}{r} 5 \\ 4 \\ 3 \\ 2 \\ 1 \\ 12 \end{array}$ |
| $\begin{gathered} \text { APR } \\ \stackrel{+}{+} \end{gathered}$ | $\begin{array}{r} 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{r} 1 \\ 10 \\ 18 \\ 26 \\ 34 \\ 40 \\ 44 \\ 46 \end{array}$ | $\begin{gathered} 109 \\ 97 \\ 84 \\ 71 \\ 56 \\ 40 \\ 21 \\ 0 \end{gathered}$ | $56$ | $\begin{array}{r} 2 \\ 19 \\ 49 \\ 83 \end{array}$ | $\begin{array}{r} 2 \\ 12 \\ 27 \\ 48 \\ 74 \end{array}$ | $\begin{aligned} & 1 \\ & 10 \\ & 20 \\ & 33 \\ & 50 \\ & 71 \end{aligned}$ | $\begin{gathered} 2 \\ 10 \\ 18 \\ 27 \\ 39 \\ 53 \\ 70 \\ 90 \end{gathered}$ | $\begin{array}{r} 2 \\ 11 \\ 19 \\ 26 \\ 34 \\ 43 \\ 55 \\ 69 \end{array}$ | $\begin{aligned} & 3 \\ & 15 \\ & 23 \\ & 29 \\ & 34 \\ & 40 \\ & 47 \\ & 55 \end{aligned}$ | $\begin{aligned} & 21 \\ & 32 \\ & 34 \\ & 36 \\ & 39 \\ & 41 \\ & 44 \\ & 48 \end{aligned}$ | $\begin{aligned} & 72 \\ & 96 \\ & 50 \\ & 47 \\ & 46 \\ & 46 \end{aligned}$ | $\begin{aligned} & 74 \\ & 61 \\ & 53 \\ & 48 \end{aligned}$ | $\begin{aligned} & 84 \\ & 67 \\ & 55 \end{aligned}$ | $\begin{aligned} & 88 \\ & 69 \end{aligned}$ | 71 84 | $\begin{aligned} & 49 \\ & 61 \\ & 74 \\ & 87 \end{aligned}$ | $\begin{aligned} & 26 \\ & 39 \\ & 53 \\ & 67 \\ & 81 \end{aligned}$ | $\begin{array}{r} 4 \\ 19 \\ 33 \\ 48 \\ 62 \\ 77 \end{array}$ | $\begin{aligned} & 19 \\ & 12 \\ & 19 \\ & 32 \\ & 46 \\ & 61 \\ & 75 \\ & 90 \end{aligned}$ | $\begin{aligned} & 41 \\ & 30 \\ & 24 \\ & 26 \\ & 35 \\ & 47 \\ & 61 \\ & 74 \end{aligned}$ | $\begin{aligned} & 64 \\ & 52 \\ & 42 \\ & 36 \\ & 35 \\ & 40 \\ & 49 \\ & 60 \end{aligned}$ | $\begin{aligned} & 86 \\ & 74 \\ & 63 \\ & 53 \\ & 46 \\ & 43 \\ & 44 \\ & 50 \end{aligned}$ | $\begin{aligned} & 84 \\ & 73 \\ & 62 \\ & 54 \\ & 48 \\ & 46 \end{aligned}$ | $\begin{aligned} & 81 \\ & 69 \\ & 58 \\ & 50 \end{aligned}$ | 86 73 60 | $\begin{aligned} & 89 \\ & 74 \end{aligned}$ | $\begin{aligned} & 89 \\ & 80 \\ & 72 \\ & 64 \\ & 56 \\ & 50 \\ & 46 \\ & 44 \end{aligned}$ | 7 6 5 4 3 2 1 12 |
| $\begin{gathered} \text { MAY } \\ + \\ \text { JUL } \end{gathered}$ | $\begin{array}{r} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{gathered} 1 \\ 8 \\ 8 \\ 16 \\ 25 \\ 33 \\ 41 \\ 48 \\ 52 \\ 54 \end{gathered}$ | $\begin{array}{r} 126 \\ 113 \\ 102 \\ 89 \\ 76 \\ 62 \\ 44 \\ 23 \\ 0 \end{array}$ | $\begin{gathered} 21 \\ 21 \\ 56 \end{gathered}$ | $\begin{aligned} & 1 \\ & 12 \\ & 28 \\ & 51 \\ & 77 \end{aligned}$ | $\begin{array}{r} 1 \\ 9 \\ 20 \\ 33 \\ \$ 1 \\ 72 \end{array}$ | $\begin{aligned} & 1 \\ & 8 \\ & 8 \\ & 17 \\ & 27 \\ & 39 \\ & 54 \\ & 71 \\ & 89 \end{aligned}$ | $\begin{array}{r} 1 \\ 9 \\ 17 \\ 25 \\ 34 \\ 45 \\ 58 \\ 73 \\ 90 \end{array}$ | $\begin{aligned} & 2 \\ & 12 \\ & 20 \\ & 20 \\ & 33 \\ & 4 \\ & 50 \\ & 61 \\ & 74 \end{aligned}$ | $\begin{aligned} & 7 \\ & 22 \\ & 28 \\ & 33 \\ & 37 \\ & 42 \\ & 48 \\ & 54 \\ & 63 \end{aligned}$ | $\begin{aligned} & 57 \\ & 50 \\ & 48 \\ & 48 \\ & 50 \\ & 52 \\ & 56 \end{aligned}$ | $\begin{aligned} & 89 \\ & 70 \\ & 61 \\ & 57 \\ & 55 \\ & 54 \end{aligned}$ | $\begin{aligned} & 83 \\ & 70 \\ & 62 \\ & 56 \end{aligned}$ | $\begin{aligned} & 89 \\ & 74 \\ & 63 \end{aligned}$ | 74 | 54 67 79 | $\begin{aligned} & 32 \\ & 45 \\ & 58 \\ & 70 \\ & 83 \end{aligned}$ | $\begin{aligned} & 10 \\ & 23 \\ & 37 \\ & 51 \\ & 64 \\ & 78 \end{aligned}$ | $\begin{aligned} & 13 \\ & 9 \\ & 20 \\ & 33 \\ & 47 \\ & 62 \\ & 76 \\ & 89 \end{aligned}$ | $\begin{aligned} & 36 \\ & 25 \\ & 20 \\ & 25 \\ & 36 \\ & 48 \\ & 62 \\ & 76 \\ & 90 \end{aligned}$ | $\begin{aligned} & 58 \\ & 47 \\ & 37 \\ & 33 \\ & 34 \\ & 41 \\ & 52 \\ & 64 \\ & 77 \end{aligned}$ | 81 69 58 50 44 44 48 55 65 | $\begin{aligned} & 79 \\ & 69 \\ & 60 \\ & 54 \\ & 51 \\ & 52 \\ & 57 \end{aligned}$ | $\begin{aligned} & 89 \\ & 79 \\ & 69 \\ & 61 \\ & 56 \\ & 54 \end{aligned}$ | $\begin{aligned} & 86 \\ & 75 \\ & 65 \\ & 57 \end{aligned}$ | $\begin{aligned} & 89 \\ & 77 \\ & 65 \end{aligned}$ | 77 | 89 82 74 65 57 49 42 38 36 | 8 7 6 5 4 3 2 1 12 |
| JUN | $\begin{array}{r} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ \hline \end{array}$ | $\begin{array}{r} 4 \\ 11 \\ 28 \\ 28 \\ 36 \\ 44 \\ 51 \\ 56 \\ 57 \\ \hline \end{array}$ | $\begin{array}{r} 127 \\ 115 \\ 92 \\ 92 \\ 79 \\ 64 \\ 46 \\ 25 \\ 0 \\ \hline \end{array}$ | $\begin{aligned} & 7 \\ & 25 \\ & 87 \\ & 87 \end{aligned}$ | $\begin{aligned} & 5 \\ & 15 \\ & 52 \\ & 52 \\ & 75 \end{aligned}$ | $\begin{aligned} & 4 \\ & 12 \\ & 36 \\ & 36 \\ & 52 \\ & 71 \\ & 89 \end{aligned}$ | $\begin{array}{r} 4 \\ 11 \\ 29 \\ 29 \\ 41 \\ 55 \\ 72 \\ 88 \end{array}$ | $\begin{aligned} & 5 \\ & 13 \\ & 28 \\ & 28 \\ & 36 \\ & 47 \\ & 99 \\ & 74 \\ & 90 \end{aligned}$ | $\begin{array}{r} 8 \\ 17 \\ 30 \\ 30 \\ 36 \\ 44 \\ 53 \\ 63 \\ 76 \end{array}$ | $\begin{aligned} & 28 \\ & 31 \\ & 37 \\ & 37 \\ & 41 \\ & 45 \\ & 51 \\ & 57 \\ & 66 \end{aligned}$ | $\begin{aligned} & 56 \\ & 56 \\ & 53 \\ & 52 \\ & 53 \\ & 56 \\ & 59 \\ & \hline \end{aligned}$ | $\begin{aligned} & 75 \\ & 66 \\ & 61 \\ & 58 \\ & 57 \end{aligned}$ | $\begin{aligned} & 86 \\ & 74 \\ & 69 \\ & 59 \\ & \hline \end{aligned}$ | $\begin{aligned} & 77 \\ & 66 \\ & \hline \end{aligned}$ | 76 | 53 69 89 89 | $\begin{aligned} & 31 \\ & 43 \\ & 69 \\ & 69 \\ & 81 \end{aligned}$ | $\begin{aligned} & 9 \\ & 23 \\ & 90 \\ & 50 \\ & 60 \\ & 76 \\ & 79 \end{aligned}$ | $\begin{aligned} & 15 \\ & 12 \\ & 34 \\ & 34 \\ & 48 \\ & 61 \\ & 75 \\ & 89 \end{aligned}$ | $\begin{aligned} & 37 \\ & 28 \\ & 28 \\ & 28 \\ & 37 \\ & 50 \\ & 63 \\ & 76 \\ & 90 \\ & \hline \end{aligned}$ | 60 49 36 36 37 44 54 65 78 | $\begin{aligned} & 82 \\ & 71 \\ & 53 \\ & 53 \\ & 48 \\ & 47 \\ & 51 \\ & 58 \\ & 68 \\ & \hline \end{aligned}$ | $\begin{aligned} & 72 \\ & 72 \\ & 63 \\ & 57 \\ & 55 \\ & 56 \\ & 60 \end{aligned}$ | $\begin{aligned} & 81 \\ & 72 \\ & 64 \\ & 59 \\ & 57 \end{aligned}$ | $\begin{aligned} & 88 \\ & 77 \\ & 68 \\ & 60 \\ & \hline \end{aligned}$ | $\begin{aligned} & 79 \\ & 68 \end{aligned}$ | 78 | 86 79 62 62 54 46 39 34 33 | $\begin{array}{r} 8 \\ 7 \\ 5 \\ 5 \\ 4 \\ 3 \\ 2 \\ 1 \\ 12 \\ \hline \end{array}$ |
|  |  |  |  | N | NNW | NW | WNW | W | WSW | SW | SSW | S | SSE | SE | ESE | N | NNW | NW | WNW | W | WSW | SW | SSW | S | SSE | SE | ESE | HOR | PM |

Table 10 Solar Position and Related Angles for 64 Deg North Latitude

| Date | Solar <br> Tlime <br> AM | $\begin{gathered} \text { Solar } \\ \text { Position } \end{gathered}$ |  | Profile (Shadow Line) Angles |  |  |  |  |  |  |  |  |  |  |  |  | Angles of Incidence Verical Surface |  |  |  |  |  |  |  |  |  |  |  | Solar <br> Time <br> PM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | ALT | 12 | N | NNE | NE | ENE | E | ESE | SE | SSE | S | SSW | Sw | WSW | N | NNE | NE | ENE | E | ESE | SE | SSE | 5 | SSW | SW | WSW | HOR |  |
| DEC | $\begin{aligned} & 11 \\ & 17 \end{aligned}$ | $\begin{aligned} & 2 \\ & 3 \end{aligned}$ | $\begin{array}{r} 14 \\ 0 \end{array}$ |  |  |  |  | $\begin{aligned} & 7 \\ & 90 \end{aligned}$ | $7$ | $\begin{aligned} & 2 \\ & 4 \end{aligned}$ | $\begin{aligned} & 2 \\ & 3 \end{aligned}$ | $\begin{aligned} & 2 \\ & 3 \end{aligned}$ | $\begin{aligned} & 2 \\ & 3 \end{aligned}$ | $\begin{aligned} & 3 \\ & 4 \end{aligned}$ | $11$ |  |  |  |  | $\begin{aligned} & 76 \\ & 90 \end{aligned}$ | $\begin{aligned} & 54 \\ & 68 \end{aligned}$ | $\begin{aligned} & 31 \\ & 45 \end{aligned}$ | $\begin{array}{r} 9 \\ 23 \end{array}$ | $\begin{array}{r} 14 \\ 3 \end{array}$ | $\begin{aligned} & 36 \\ & 23 \end{aligned}$ | $\begin{aligned} & 59 \\ & 45 \end{aligned}$ | $\begin{aligned} & 81 \\ & 68 \end{aligned}$ | $\begin{aligned} & 88 \\ & 87 \end{aligned}$ | $\begin{gathered} 1 \\ 12 \end{gathered}$ |
| $\begin{gathered} \text { JAN } \\ + \\ \text { NOV } \end{gathered}$ | $\begin{aligned} & 10 \\ & 11 \\ & 12 \end{aligned}$ | $\begin{aligned} & 3 \\ & 5 \\ & 6 \end{aligned}$ | $\begin{gathered} 28 \\ 14 \\ 0 \end{gathered}$ |  |  |  | 27 | $\begin{array}{r} 6 \\ 20 \\ 90 \end{array}$ | $\begin{array}{r} 4 \\ 9 \\ 15 \end{array}$ | $\begin{aligned} & 3 \\ & 6 \\ & 8 \end{aligned}$ | $\begin{aligned} & 3 \\ & 5 \\ & 6 \end{aligned}$ | $\begin{aligned} & 3 \\ & 5 \\ & 6 \end{aligned}$ | $\begin{aligned} & 4 \\ & 6 \\ & 6 \end{aligned}$ | $\begin{array}{r} 10 \\ 10 \\ 8 \end{array}$ | 32 |  |  |  | 84 | $\begin{aligned} & 62 \\ & 76 \\ & 90 \end{aligned}$ | $\begin{aligned} & 40 \\ & 54 \\ & 68 \end{aligned}$ | $\begin{aligned} & 17 \\ & 31 \\ & 45 \end{aligned}$ | $\begin{array}{r} 6 \\ 10 \\ 23 \end{array}$ | 28 15 6 | $\begin{aligned} & 51 \\ & 37 \\ & 23 \end{aligned}$ | $\begin{aligned} & 73 \\ & 59 \\ & 45 \end{aligned}$ | 82 68 | $\begin{aligned} & 87 \\ & 85 \\ & 84 \end{aligned}$ | $\begin{gathered} 2 \\ 1 \\ 12 \end{gathered}$ |
| $\begin{aligned} & \text { FEB } \\ & +\underset{C T}{ } \end{aligned}$ | $\begin{array}{r} 8 \\ 9 \\ 9 \\ 10 \\ 12 \end{array}$ | $\begin{array}{r} 3 \\ 8 \\ 12 \\ 14 \\ 15 \end{array}$ | $\begin{gathered} 58 \\ 45 \\ 30 \\ 15 \\ 0 \end{gathered}$ |  |  | 11 | $\begin{aligned} & 5 \\ & 20 \\ & 98 \end{aligned}$ | $\begin{array}{r} 3 \\ 11 \\ 23 \\ 44 \\ 90 \end{array}$ | $\begin{array}{r} 3 \\ 8 \\ 15 \\ 23 \\ 35 \end{array}$ | $\begin{array}{r} 3 \\ 8 \\ 12 \\ 16 \\ 21 \end{array}$ | $\begin{array}{r} 3 \\ 8 \\ 12 \\ 14 \\ 16 \end{array}$ | $\begin{array}{r} 5 \\ 11 \\ 14 \\ 15 \\ 15 \end{array}$ | $\begin{aligned} & 17 \\ & 19 \\ & 19 \\ & 18 \\ & 16 \end{aligned}$ | $\begin{aligned} & 86 \\ & 39 \\ & 27 \\ & 21 \end{aligned}$ | $\begin{aligned} & 64 \\ & 35 \end{aligned}$ |  |  | 77 | $\begin{aligned} & 54 \\ & 68 \\ & 83 \end{aligned}$ | $\begin{aligned} & 32 \\ & 46 \\ & 61 \\ & 75 \\ & 90 \end{aligned}$ | $\begin{array}{r} 9 \\ 24 \\ 39 \\ 54 \\ 68 \end{array}$ | 14 8 19 33 47 | $\begin{aligned} & 36 \\ & 23 \\ & 14 \\ & 16 \\ & 27 \end{aligned}$ | 58 45 32 21 15 | $\begin{aligned} & 81 \\ & 67 \\ & 54 \\ & 40 \\ & 27 \end{aligned}$ | $\begin{aligned} & 90 \\ & 75 \\ & 61 \\ & 47 \end{aligned}$ | $\begin{aligned} & 83 \\ & 68 \end{aligned}$ | $\begin{aligned} & 87 \\ & 82 \\ & 78 \\ & 76 \\ & 75 \end{aligned}$ | $\begin{array}{r} 4 \\ 3 \\ 2 \\ 1 \\ 12 \end{array}$ |
| $\begin{gathered} \text { MAR } \\ \stackrel{+}{\text { SEP }} \end{gathered}$ | $\begin{array}{r} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{r} 7 \\ 13 \\ 18 \\ 22 \\ 25 \\ 26 \end{array}$ | $\begin{array}{r} 76 \\ 63 \\ 48 \\ 33 \\ 17 \\ 0 \end{array}$ |  | 36 | $\begin{aligned} & 12 \\ & 37 \\ & 81 \end{aligned}$ | $\begin{array}{r} 8 \\ 19 \\ 37 \\ 67 \end{array}$ | $\begin{array}{r} 7 \\ 14 \\ 24 \\ 37 \\ 59 \\ 90 \end{array}$ | $\begin{array}{r} 7 \\ 13 \\ 19 \\ 27 \\ 37 \\ 52 \end{array}$ | $\begin{array}{r} 8 \\ 13 \\ 18 \\ 23 \\ 28 \\ 35 \end{array}$ | $\begin{aligned} & 11 \\ & 16 \\ & 20 \\ & 23 \\ & 25 \\ & 28 \end{aligned}$ | $\begin{aligned} & 26 \\ & 26 \\ & 26 \\ & 26 \\ & 26 \\ & 26 \end{aligned}$ | $\begin{aligned} & 69 \\ & 44 \\ & 36 \\ & 31 \\ & 28 \end{aligned}$ | $\begin{aligned} & 63 \\ & 45 \\ & 35 \end{aligned}$ | $\begin{aligned} & 78 \\ & 52 \end{aligned}$ |  | 81 | $\begin{aligned} & 59 \\ & 73 \\ & 77 \end{aligned}$ | $\begin{aligned} & 37 \\ & 51 \\ & 66 \\ & 81 \end{aligned}$ | $\begin{aligned} & 15 \\ & 30 \\ & 45 \\ & 60 \\ & 75 \\ & 90 \end{aligned}$ | $\begin{aligned} & 11 \\ & 14 \\ & 26 \\ & 41 \\ & 59 \\ & 70 \end{aligned}$ | $\begin{aligned} & 32 \\ & 22 \\ & 18 \\ & 25 \\ & 37 \\ & 51 \end{aligned}$ | 54 42 31 24 26 34 | 77 63 51 39 30 26 | $\begin{aligned} & 85 \\ & 72 \\ & 58 \\ & 45 \\ & 34 \end{aligned}$ | $\begin{aligned} & 79 \\ & 64 \\ & 51 \end{aligned}$ | $\begin{aligned} & 85 \\ & 70 \end{aligned}$ | $\begin{aligned} & 83 \\ & 77 \\ & 72 \\ & 68 \\ & 65 \\ & 64 \end{aligned}$ | $\begin{array}{r} 5 \\ 4 \\ 3 \\ 2 \\ 1 \\ 12 \end{array}$ |
| $\begin{gathered} \text { APR } \\ \stackrel{+}{\text { AUG }} \end{gathered}$ | $\begin{array}{r} 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{array}{r} 4 \\ 10 \\ 17 \\ 23 \\ 29 \\ 34 \\ 37 \\ 38 \end{array}$ | $\begin{array}{r} 108 \\ 95 \\ 82 \\ 67 \\ 92 \\ 36 \\ 18 \\ 0 \end{array}$ | $\begin{aligned} & 12 \\ & 64 \end{aligned}$ | $\begin{array}{r} 6 \\ 22 \\ 51 \end{array}$ | $\begin{array}{r} 4 \\ 13 \\ 27 \\ 48 \\ 77 \end{array}$ | $\begin{aligned} & 4 \\ & 11 \\ & 20 \\ & 31 \\ & 48 \\ & 71 \end{aligned}$ | $\begin{array}{r} 4 \\ 10 \\ 17 \\ 25 \\ 35 \\ 48 \\ 67 \\ 90 \end{array}$ | $\begin{array}{r} 5 \\ 12 \\ 17 \\ 23 \\ 30 \\ 38 \\ 49 \\ 64 \end{array}$ | $\begin{array}{r} 9 \\ 16 \\ 21 \\ 25 \\ 29 \\ 34 \\ 40 \\ 47 \end{array}$ | $\begin{aligned} & 45 \\ & 32 \\ & 31 \\ & 31 \\ & 33 \\ & 34 \\ & 37 \\ & 40 \end{aligned}$ | $\begin{aligned} & 64 \\ & 48 \\ & 42 \\ & 39 \\ & 38 \\ & 38 \end{aligned}$ | $\begin{aligned} & 90 \\ & 65 \\ & 52 \\ & 44 \\ & 40 \end{aligned}$ | $\begin{aligned} & 77 \\ & 59 \\ & 47 \end{aligned}$ | $\begin{aligned} & 84 \\ & 64 \end{aligned}$ | 72 85 | $\begin{aligned} & 49 \\ & 63 \\ & 77 \end{aligned}$ | $\begin{aligned} & 27 \\ & 41 \\ & 55 \\ & 69 \\ & 84 \end{aligned}$ | $\begin{aligned} & 6 \\ & 20 \\ & 35 \\ & 50 \\ & 64 \\ & 79 \end{aligned}$ | $\begin{aligned} & 19 \\ & 12 \\ & 19 \\ & 32 \\ & 46 \\ & 61 \\ & 75 \\ & 90 \end{aligned}$ | $\begin{aligned} & 41 \\ & 29 \\ & 22 \\ & 23 \\ & 32 \\ & 45 \\ & 58 \\ & 72 \end{aligned}$ | $\begin{aligned} & 64 \\ & 51 \\ & 40 \\ & 32 \\ & 30 \\ & 35 \\ & 44 \\ & 56 \end{aligned}$ | $\begin{aligned} & 86 \\ & 73 \\ & 61 \\ & 49 \\ & 41 \\ & 36 \\ & 37 \\ & 43 \end{aligned}$ | 82 69 98 48 40 38 | $\begin{aligned} & 90 \\ & 77 \\ & 64 \\ & 53 \\ & 43 \end{aligned}$ | $\begin{aligned} & 83 \\ & 69 \\ & 56 \end{aligned}$ | 67 72 | $\begin{aligned} & 86 \\ & 80 \\ & 73 \\ & 67 \\ & 61 \\ & 56 \\ & 53 \\ & 52 \end{aligned}$ | 7 6 5 4 3 2 1 12 |
| $\begin{gathered} \text { MAY } \\ + \\ \text { JUL } \end{gathered}$ | $\begin{array}{r} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{array}$ | $\begin{aligned} & 6 \\ & 12 \\ & 18 \\ & 24 \\ & 31 \\ & 37 \\ & 42 \\ & 45 \\ & 46 \end{aligned}$ | $\begin{array}{r} 125 \\ 112 \\ 99 \\ 86 \\ 71 \\ 56 \\ 39 \\ 70 \\ 0 \end{array}$ | $\begin{aligned} & 10 \\ & 29 \\ & 64 \end{aligned}$ | $\begin{array}{r} 7 \\ 16 \\ 32 \\ 56 \\ 83 \end{array}$ | $\begin{aligned} & 6 \\ & 13 \\ & 22 \\ & 35 \\ & 53 \\ & 76 \end{aligned}$ | $\begin{aligned} & 6 \\ & 12 \\ & 18 \\ & 27 \\ & 38 \\ & 54 \\ & 72 \end{aligned}$ | $\begin{aligned} & 7 \\ & 12 \\ & 18 \\ & 25 \\ & 32 \\ & 42 \\ & 55 \\ & 71 \\ & 90 \end{aligned}$ | $\begin{aligned} & 11 \\ & 16 \\ & 21 \\ & 26 \\ & 31 \\ & 37 \\ & 45 \\ & 56 \\ & 70 \end{aligned}$ | $\begin{aligned} & 31 \\ & 28 \\ & 29 \\ & 31 \\ & 34 \\ & 37 \\ & 42 \\ & 48 \\ & 56 \end{aligned}$ | 88 54 45 42 42 43 45 48 | $\begin{aligned} & 81 \\ & 62 \\ & 53 \\ & 49 \\ & 47 \\ & 46 \end{aligned}$ | $\begin{aligned} & 75 \\ & 62 \\ & 53 \\ & 48 \end{aligned}$ | $\begin{aligned} & 83 \\ & 67 \\ & 56 \end{aligned}$ | $\begin{aligned} & 88 \\ & 70 \end{aligned}$ | 58 68 81 | $\begin{aligned} & 33 \\ & 47 \\ & 60 \\ & 74 \\ & 87 \end{aligned}$ | $\begin{aligned} & 11 \\ & 26 \\ & 40 \\ & 54 \\ & 67 \\ & 81 \end{aligned}$ | $\begin{aligned} & 14 \\ & 12 \\ & 22 \\ & 36 \\ & 50 \\ & 64 \\ & 78 \end{aligned}$ | $\begin{aligned} & 36 \\ & 25 \\ & 20 \\ & 25 \\ & 36 \\ & 48 \\ & 62 \\ & 76 \\ & 90 \end{aligned}$ | $\begin{aligned} & 58 \\ & 46 \\ & 36 \\ & 30 \\ & 31 \\ & 38 \\ & 49 \\ & 61 \\ & 75 \end{aligned}$ | $\begin{aligned} & 80 \\ & 68 \\ & 56 \\ & 46 \\ & 40 \\ & 38 \\ & 42 \\ & 50 \\ & 61 \end{aligned}$ | 90 77 66 56 48 44 45 50 | 86 74 63 54 48 46 | $\begin{aligned} & 81 \\ & 69 \\ & 59 \\ & 50 \end{aligned}$ | $\begin{aligned} & 85 \\ & 73 \\ & 61 \end{aligned}$ | $\begin{aligned} & 88 \\ & 75 \end{aligned}$ | $\begin{aligned} & 84 \\ & 78 \\ & 72 \\ & 66 \\ & 59 \\ & 53 \\ & 48 \\ & 45 \\ & 44 \end{aligned}$ | 8 7 6 5 4 3 2 1 12 |
| JUN | $\begin{array}{r} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ \hline \end{array}$ | $\begin{array}{r} 9 \\ 15 \\ 21 \\ 28 \\ 34 \\ 40 \\ 45 \\ 48 \\ 49 \\ \hline \end{array}$ | $\begin{array}{r} 126 \\ 114 \\ 101 \\ 87 \\ 73 \\ 58 \\ 40 \\ 21 \\ 0 \\ \hline \end{array}$ | $\begin{aligned} & 15 \\ & 33 \\ & 64 \end{aligned}$ | $\begin{aligned} & 10 \\ & 20 \\ & 35 \\ & 57 \\ & 81 \end{aligned}$ | $\begin{aligned} & 9 \\ & 16 \\ & 25 \\ & 38 \\ & 55 \\ & 75 \end{aligned}$ | $\begin{aligned} & 9 \\ & 15 \\ & 21 \\ & 30 \\ & 41 \\ & 59 \\ & 73 \end{aligned}$ | $\begin{aligned} & 11 \\ & 16 \\ & 21 \\ & 28 \\ & 35 \\ & 45 \\ & 57 \\ & 72 \\ & 90 \\ & \hline \end{aligned}$ | $\begin{aligned} & 17 \\ & 21 \\ & 25 \\ & 29 \\ & 34 \\ & 40 \\ & 48 \\ & 58 \\ & 72 \\ & \hline \end{aligned}$ | $\begin{aligned} & 47 \\ & 36 \\ & 34 \\ & 35 \\ & 37 \\ & 41 \\ & 45 \\ & 51 \\ & 59 \\ & \hline \end{aligned}$ | $\begin{aligned} & 62 \\ & 51 \\ & 47 \\ & 46 \\ & 46 \\ & 48 \\ & 48 \\ & 52 \end{aligned}$ | $\begin{aligned} & 85 \\ & 67 \\ & 58 \\ & 53 \\ & 50 \\ & 49 \\ & \hline \end{aligned}$ | $\begin{aligned} & 79 \\ & 65 \\ & 57 \\ & 52 \\ & \hline \end{aligned}$ | $\begin{aligned} & 85 \\ & 70 \\ & 59 \\ & \hline \end{aligned}$ | $\begin{aligned} & 89 \\ & 72 \\ & \hline \end{aligned}$ | 54 67 80 | $\begin{aligned} & 32 \\ & 46 \\ & 59 \\ & 72 \\ & 85 \end{aligned}$ | $\begin{aligned} & 12 \\ & 26 \\ & 39 \\ & 53 \\ & 67 \\ & 80 \end{aligned}$ | $\begin{aligned} & 17 \\ & 15 \\ & 24 \\ & 37 \\ & 50 \\ & 64 \\ & 77 \end{aligned}$ | $\begin{aligned} & 37 \\ & 28 \\ & 23 \\ & 28 \\ & 37 \\ & 50 \\ & 63 \\ & 76 \\ & 90 \\ & \hline \end{aligned}$ | $\begin{aligned} & 59 \\ & 48 \\ & 39 \\ & 34 \\ & 34 \\ & 41 \\ & 51 \\ & 63 \\ & 76 \\ & \hline \end{aligned}$ | $\begin{aligned} & 82 \\ & 69 \\ & 58 \\ & 49 \\ & 43 \\ & 42 \\ & 45 \\ & 53 \\ & 63 \\ & \hline \end{aligned}$ | 79 68 58 51 48 48 53 | $\begin{aligned} & 88 \\ & 76 \\ & 66 \\ & 57 \\ & 52 \\ & 49 \\ & \hline \end{aligned}$ | $\begin{aligned} & 83 \\ & 71 \\ & 61 \\ & 53 \\ & \hline \end{aligned}$ | $\begin{aligned} & 87 \\ & 74 \\ & 63 \\ & \hline \end{aligned}$ | $\begin{aligned} & 89 \\ & 76 \\ & \hline \end{aligned}$ | $\begin{aligned} & 81 \\ & 75 \\ & 69 \\ & 62 \\ & 56 \\ & 50 \\ & 45 \\ & 42 \\ & 41 \\ & \hline \end{aligned}$ | $\begin{array}{r} 8 \\ 7 \\ 6 \\ 5 \\ 4 \\ 3 \\ 2 \\ 1 \\ 12 \end{array}$ |
|  |  |  |  | N | NNW | NW | WNW | W | WSW | SW | SSW | 5 | SSE SE | SE | ESE | N | NNW | NW | WNW | w | WSW | sw | SSW | S | SSE | SE | ESE | HOR | PM |

## C. UsS. and Word Maps

To locate latitude for a given place.
U.S. map reproduced from "Designing with the LOF Sun Angle Calculator", distributed by Libbey-Owens-Ford Company, Toledo, Ohio, 1974.

World map reproduced from "World Master World Atlas" by Rand McNally \& Company, Chicago, 1981.



## D. Sizing Overhang

For a south facing $3^{\prime} \times 5^{\prime}$ window at 40 degrees north latitude using Graph developed by - Dave Boyd of Engineering Extension Programs. Distributed by the Technical Energy Information Services of the KSU Cooperative Extension Services, 1983.


Fig. 6

## E. Sizing Wing Wall

Manually sizing wing wall for a south facing 3 'x5' window, at 40 degrees north latitude.

Phase-II : Sizing Wing Wall
Input values -
Window Orientation : 0
Month of Year For 100\% Shade : 5
Day of Month For 100\% Shade : 21
Beginning Hour of Day For $100 \%$ Shade (Time-1) : 9
Ending Hour of Day For $100 \%$ Shade (Time-2) : 15
Month of Year For 100\% Sun : 11
Day of Month For $100 \%$ Sun : 15
Beginning Hour of Day For $100 \%$ Sun (Time-3) : 9
Ending Hour of Day For $100 \%$ Sun (Time-4) : 15
Output -
Right Wing Wall Projection (RWWP) : 1.00 ft. Right Wing Wall Gap (RWWG) : l.00 ft.
Left Wing Wall Projection (LWWP) : 1.00 ft .
Left Wing Wall Gap (LWWG) : 1.00 ft .

F. User Response

A summary of the user response is included here.

A summary of response by Professor Dale Bryant, currently CAD Software Development Manager, OCTAL Inc.,WA.

## Uses :

"...The program is mathematically accurate...It does what it says it does. It does it quickly and with a minimum of confusion..."
"...The inclusion of sizing wing walls makes the program more versatile than many others which only consider horizontal overhangs..."
"...It seems pretty clean from the user standpoint. The inputs all do exactly what they say they do. The defaults all work and update properly, and the error mesages during the solar simulation all make perfect sense..."

## Drawbacks :

"...The user interface is inconsistent. The main menu structure would have worked for all other input as well..."
"...The program has no way of saving or retrieving data to and from computer files...The inability to save the design of a window makes the program of questionable usefulness in real-design situation..."
"...The program appears to have been written by someone with little programming experience...The program works, but it is hard to read, and relatively poorly organized. Many routines are far too long and, and there is much code that is unnecessary..."

## SHADE

Computer program for sizing and analyzing fixed SHAding DEvices
Please indicate briefly your response for following items: (Use extra sheet of paper, if needed)

* Usefulness :
* Ease of Operation :
*Bugs :
* Adequacy of Documentation :
* Enhancement :

Comments:

Thanks for spending some time.
Your response is highly appreciated.
Name :
Date : $\qquad$
Occupation $\qquad$

## G. Program Listing

SHADE is written using Turbo Pascal version 3.0 for IBM PCs and compatibles.

## Note

The program listing and a compiled copy of SHADE is included in the Department of Architecture copy of this thesis report

## Bibliography

Brown, G. Z.. Sun. Wind and Light. John Wiley \& Sons, 1985.
Brown, G. Z., John S. Reynolds, M. Susan Ubbelchde, Susan Pledger. Upsidedown - The Salem Example Revisited. John Wiley \& Sons, 1983.

Bennett, R.. Sun Angles for Design. Robert Bennett, 1978.
Foley, J. D. , A. Van Dam. Fundamentals of Interactive Computer Graphics. Addison-Wesly Publishing Company Inc., 1982.

Givoni, B.. Man. Climate and Architecture. Van Nostrand Reinhold Company, 1981.

Mazria, Edward. The Passive Solar Energy Book. Rodale Press, Emmaus, PA., 1979.

Mitchell, William J., Robin S. Liggett, Thomas Kvan. The Art of Computer Graphics Programming. Van Nostrand Reinhold Company, New York, 1987.

Olgyay, Victor. Design with Climate. Princeton University Press, Princeton, NJ., 1973.

Olgyay, Aladar, Victor Olgyay. Solar Control and Shading Devices. Princeton University Press, Princeton, NJ., 1976.

Stein Benjamin, John S. Reynolds, William J. McGuiness. Mechanical and Electrical Equipment for Buildings - Seventh Edition. John Wiley \& Sons, 1986.
"A Method of Estimating Monthly Average Solar Radiation on Shaded Receivers". D. M. Utzinger and S. A. Klien. Solar Energy, vol. 23, pp.369-378, Pergamon Press Ltd., 1979.
"A simple Method for Sizing_Overhangs". Michael Utzinger. Solar Age, July 1980.
"Microcomputer Methods for Solar Design and Analysis". Building Applications and Regulatory Support Branch, U. S. Govt. Printing Office, 1981.
"Passive Solar Design Handbook", Vol. 2 of 2. Los Alamos Scientific Laboratory and Others, January 1980.
"Sun Angle Calculator". Libbey-Owens-Ford Company, 1974.
"Turbo Pascal", Reference Manual, Version 2.0. Borland International Inc., CA., 1983.

# COMPUTER PROGRAM FOR SIZING AND ANALYZING FIXED SHADING DEVICES (SHADE) 

by

VINOD S. CHATURVEDI
B.Arch., Bombay University, India, 1985

## AN ABSTRACT OF A THESIS

submitted in partial fulfillment of the
requirements for the degree

## MASTER OF ARCHITECTURE

Department of Architecture
College of Architecture and Design

KANSAS STATE UNIVERSITY Manhattan, Kansas

## Abstract

The computer program SHADE allows architects working in the preliminary design phase to size and evaluate the performance of fixed shading devices, such as horizontal overhangs or vertical wing walls, for any window at any latitude. It is also a useful tool for lay persons and students of architecture who are interested in learning more about Environmental Systems in Architecture. It is written using Turbo Pascal version 3.0 for IBM PCs or compatibles with color monitors.

It is developed to size and locate fixed horizontal overhang in Phase-I and vertical wing walls in Phase-II, for any window at any latitude. The limitation for sizing overhangs is that, they only can be sized correctly and practically for windows facing within 10 degrees east or west of due south. The edge effect of the overhang can be addressed by suitably sizing the overhang extension beyond the left or right edge of the window in Phase-III. The strongest and perhaps the most useful feature of SHADE is the shadow pattern simulation of the shading devices in Phase-IV. The performance of a shading device can be evaluated by viewing its shadow pattern at one hour intervals for the entire year, even at different window orientations. The percentage of window area in direct sunlight and shade is also displayed.

A hard copy of the graphics or text output can be easily printed at the stroke of a key anytime during the entire execution of the program.


[^0]:    1 The northern hemisphere is used in all the explanations in introduction. But since the sun motion is symmetrical about the equator, whatever happens in northern hemisphere will be repeated in southern hemisphere six months later.

[^1]:    ${ }^{1}$ From "Sizing Fixed Overhangs for Solar Collectors", a handout by Energy Extension Center, Kansas State University.

[^2]:    Use the same keyboard commands as in Phase-IV to view the shadow pattern for the entire year, or press "F7" to exit.

    Pressing function "F7" key will return the user to the Main Menu.
    Use the "down" arrow key to go to the bottom of Main Menu to exit from program SHADE and return to the operating system.

[^3]:    ${ }^{1}$ It is the dry bulb temperature range within which human beings will feel comfortable, when combined with the effect of relative humidity, wind speed, metabolic and clothing level.

[^4]:    1 British thermal unit.
    2 The total surface area in square feet of four outside faces of the building + area of one roof divided by total cubic feet of volume enclosed by the skin.

