

Supplementary material

Chapter 2: Assessing the uncertainty of maize yield without nitrogen fertilization

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Supp. Table 2.1.

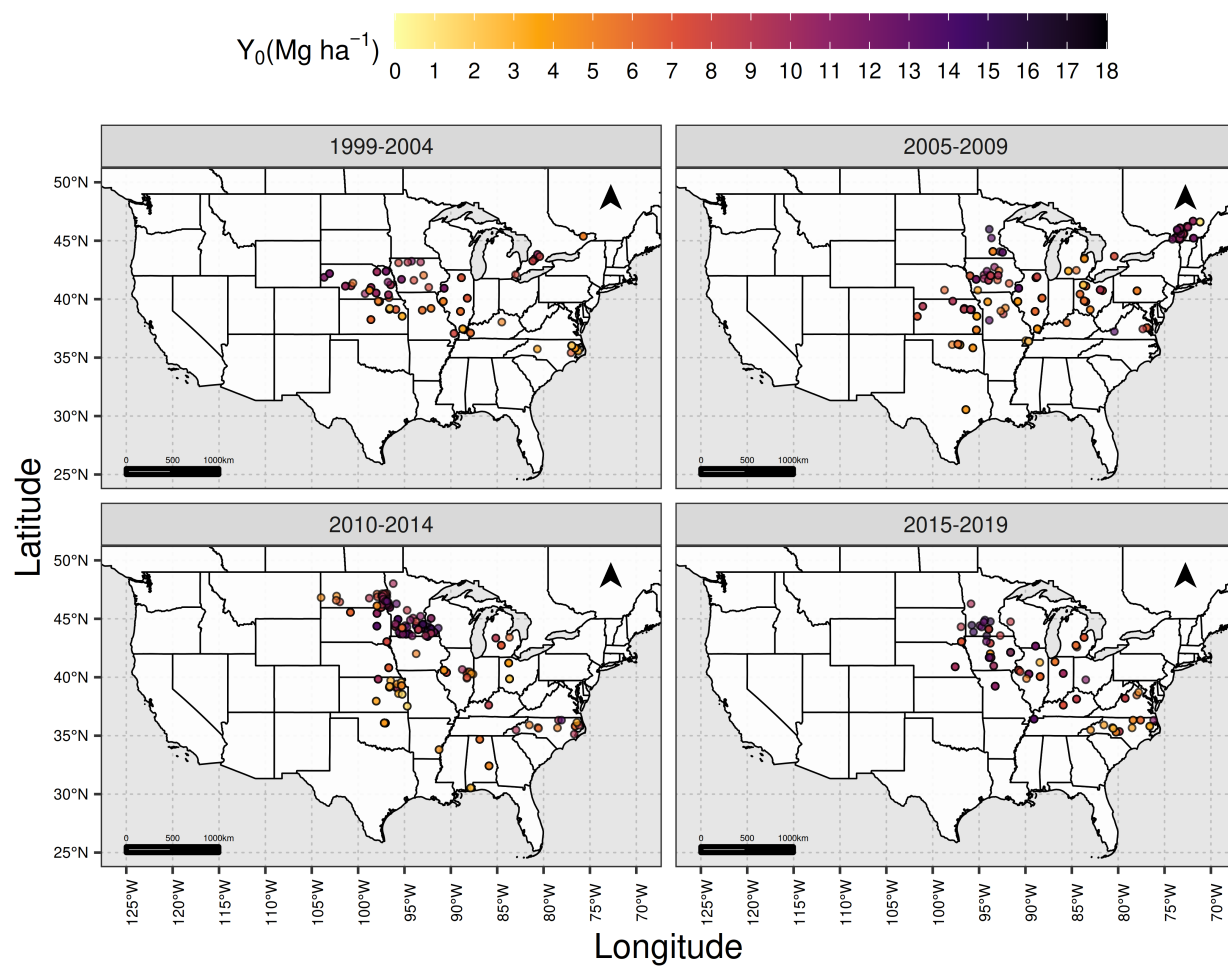
Data references, number of Y_0 (site-years), states and years covered by each source.

Source	Reference	Y_0 (site-years)	State/s	Year/s
1	Archontoulis (pers. comm.)	6 (6)	IA	2017-2018
2	Asebedo (2015)	5 (5)	KS	2012-2014
3	Barker (2011)	2 (2)	IA	2009-2010
4	Berg (2016)	14 (2)	SD	2014-2015
5	Cook et al. (2010)	5 (2)	PA	2007-2008
6	Correndo and Ciampitti (pers. comm.)	2 (1)	KS	2019
7	Corteva Agrisciences (pers. comm.)	130 (35)	IA, IL, IN, MN, MO, NE, SD, TN, WI	2011-2019
8	Coulter (pers. comm.)	11 (11)	MN	2015
9	Crozier et al. (2014)	4 (4)	NC	2010-2012
10	Edmonds et al. (2013)	4 (4)	OK	2005-2007
11	Ferdinand et al. (2003)	4 (2)	KS	2003
12	Foster 2014	5 (5)	KS	2012-2013
13	Franzluebbers (2018); Franzluebbers et al. (2018)	27 (27)	NC, VA	2014-2016
14	Gehl et al. (2005)	10 (10)	KS	2001-2002
15	Gordon (2003)	1 (1)	KS	2003
16	Henry et al. (2010)	8 (4)	OH	2007-2008
17	Hoben et al. (2011)	7 (7)	MI	2007-2008
18	Holland and Schepers (2010)	3 (3)	NE	2002-2004
19	Holou et al (2011)	2 (2)	MO	2008-2009
20	Janssen et al. (2006; 2011)	11 (8)	KS	2006-2010
21	Kelley and Moyer (2007; 2009)	18 (3)	KS	2005-2009
22	Kent et al. (2012)	8 (4)	MN	2011-2012
23	Lamond et al. (2001)	2 (2)	KS	2000-2001
24	Lindsey et al. (2015)	16 (4)	OH	2013-2014
25	Ma et al. (2005)	3 (3)	CAN	2000-2002
26	Maddux (2008)	3 (3)	KS	2006-2008
27	Mahama et al. (2016)	4 (4)	KS	2013-2014
28	Miller (2014)	32 (4)	OK	2013-2014
29	Miller et al. (2017)	4 (4)	OK	2013-2014
30	Mueller et al. (2013)	13 (13)	KS	2010-2011
31	Nafziger (pers. comm.)	140 (70)	IL	1999-2008
32	Rajkovich et al. (2017)	6 (6)	NC	2014-2015
33	Reese et al. (2014)	12 (4)	SD	2014-2015
34	Roberts et al. (2016)	2 (2)	AR	2011-2012
35	Rudnick et al. (2016)	9 (3)	NE	2012-2014
36	Ruf-Pachta et al. (2013)	4 (2)	KS	2005-2006
37	Ruiz-Diaz (2007)	6 (2)	IA	2005-2006
38	Ruiz-Diaz et al. (2008)	30 (30)	IA	2004-2006
39	Santoro (2015)	14 (3)	KY	2015-2016
40	Schwab and Murdock (2005)	4 (4)	KY	2003-2004
41	Shahandeh et al. (2011)	6 (3)	TX	2005-2007
42	Sharma (2014); Sharma et al. (2015, 2016a, 2016b)	51 (51)	ND	2011-2013
43	Shepard et al. (2011)	8 (8)	IL, OH	2006-2007
44	Sindelar et al. (2013; 2015)	36 (6)	MN	2009-2012

Source	Reference	Y_0 (site-years)	State/s	Year/s
45	Sistani et al. (2017)	2 (2)	KY	2007-2008
46	Stamper (2009)	8 (3)	KS	2007-2009
47	Steinke (pers. comm.)	18 (18)	MI	2011-2018
48	Torino et al. (2014)	10 (8)	AL	2010-2012
49	Tremblay (pers. comm.)	92 (92)	CAN	2000-20009
50	Tremblay et al. (2012)	46 (46)	IL, KS, MO, NE, OH, OK, VA, CAN	2006-2009
51	Tucker (2010)	10 (10)	KS	2006-2009
52	Walker et al. (2018)	14 (14)	MN	2014
53	Walsh et al. (2012)	9 (9)	OK	2005-2007
54	Wheeler (2014)	8 (8)	IL	2013
55	Williams et al. (2007a; 2007b)	25 (25)	NC	2000-2004
56	Williams et al. (2010)	6 (6)	MO	2000-2001
57	Wortmann et al. (2011)	32 (32)	NE	2002-2004
58	Yost et al. (2012; 2013; 2014)	58 (28)	MN	2009-2012
59	Zhu et al. (2015)	1 (1)	PA	2009

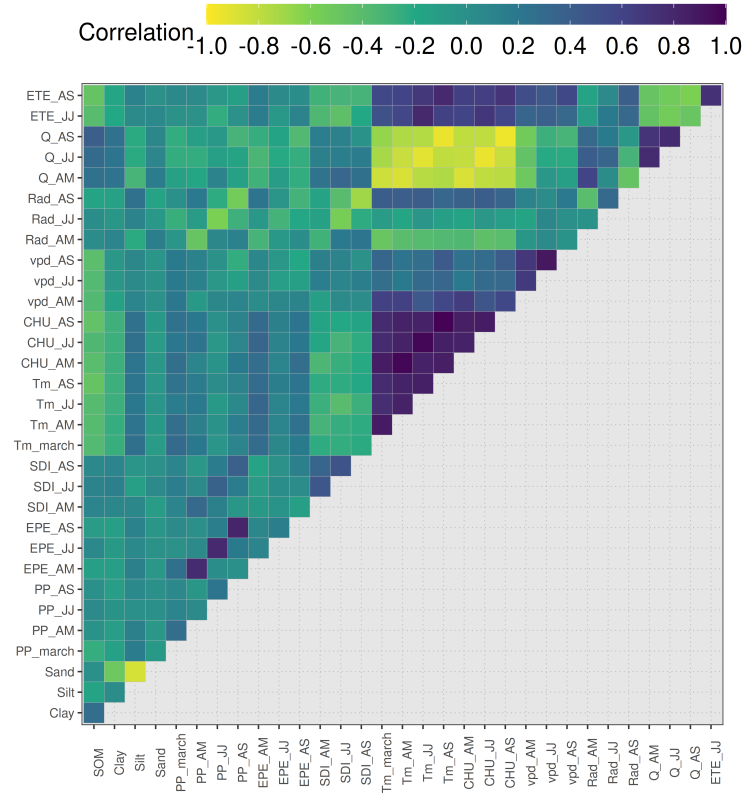
Supp. Figure 2.1.

Spatio-temporal distribution of maize nitrogen trials used for the analysis.



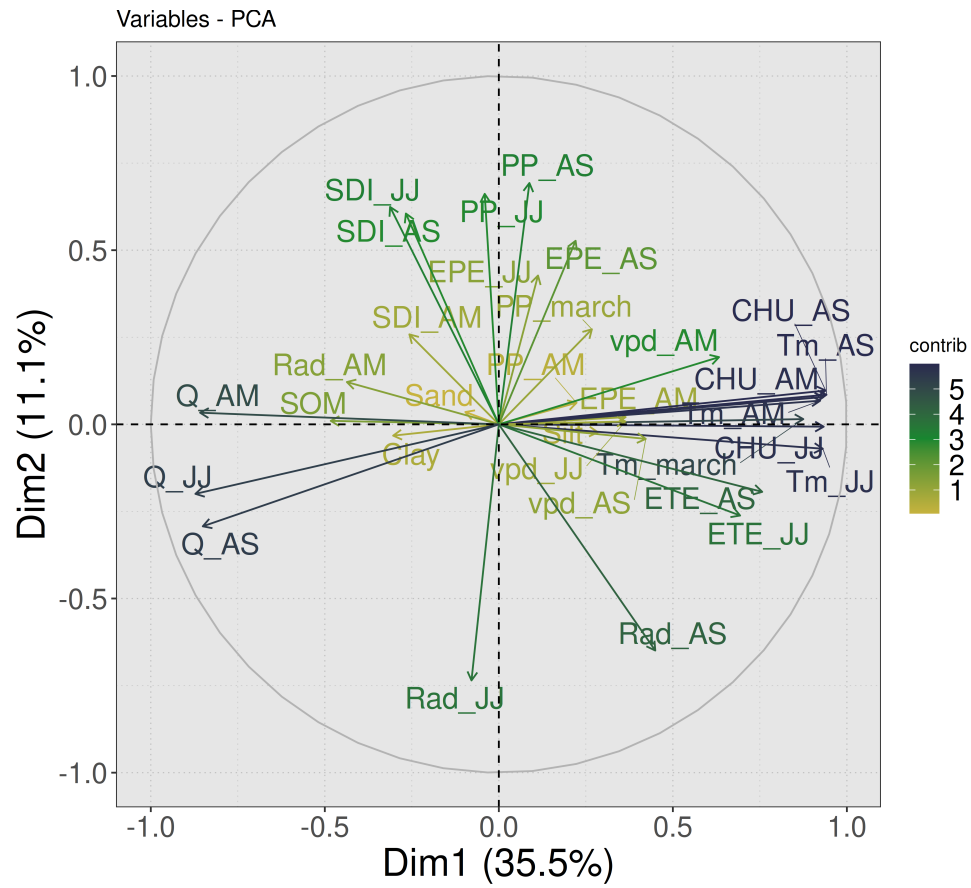
Supp. Figure 2.2.

Correlation matrix for continuous features used for the full model for maize yield prediction under N omission (Y_0 , Mg ha⁻¹).



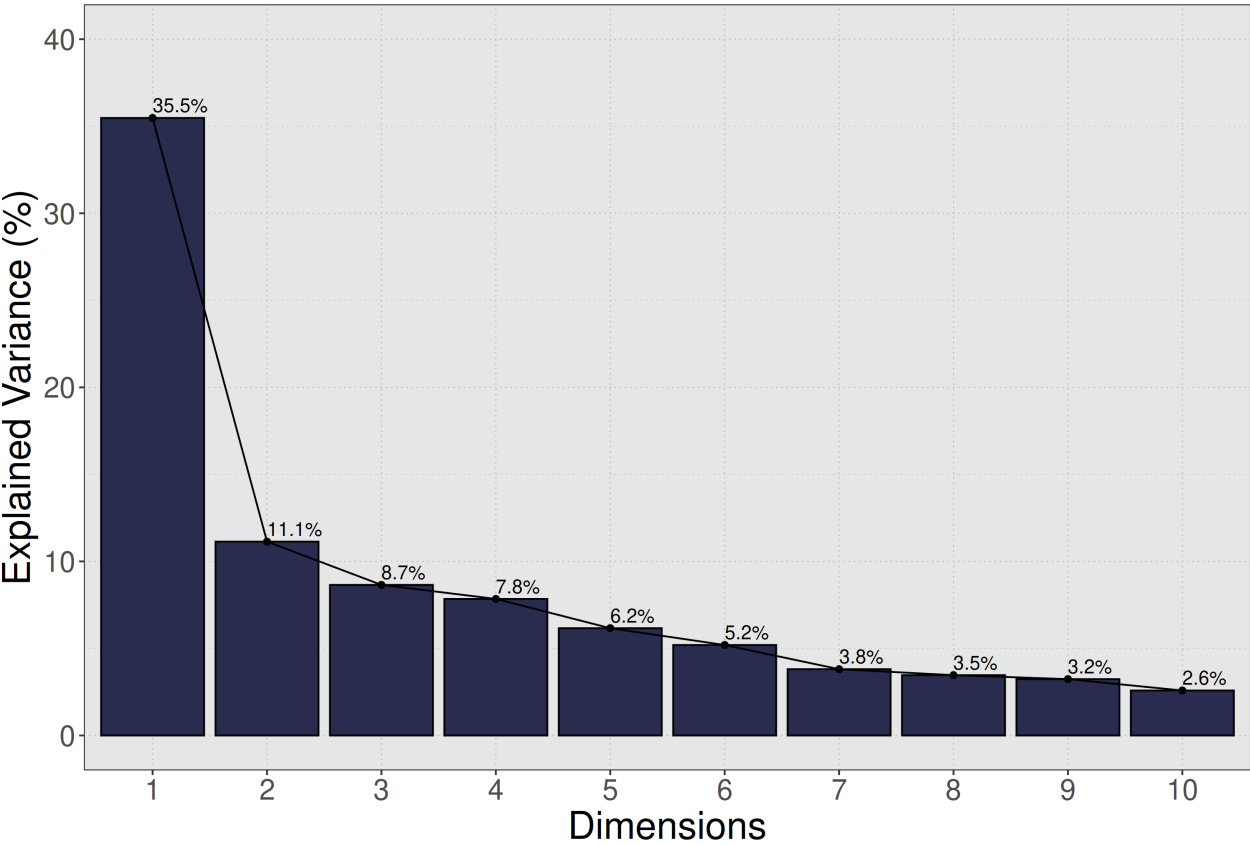
Supp. Figure 2.3A.

Biplot of principal components analysis for continuous features used for the full model for maize yield prediction under N omission (Y_0 , Mg ha⁻¹).



Supp. Figure 2.3B.

Contribution of dimensions to the principal components analysis for continuous features used for the full model for maize yield prediction under N omission (Y_0 , Mg ha^{-1}).



References (Supp. Table 2.1)

- Asebedo, A.R. 2015. Development of sensor-based nitrogen recommendation algorithms for cereal crops. Doctor of Philosophy Dissertation. Department of Agronomy, Kansas State University. <http://hdl.handle.net/2097/19229>
- Barker, D.W., 2011. Utilization of active canopy sensors for nitrogen fertilizer management in corn. Doctor of Philosophy Dissertation. Iowa State University. Graduate Theses and Dissertations, 10057. <https://lib.dr.iastate.edu/etd/10057>
- Berg, S.L., 2016. Evaluation of tillage, crop rotation, and cover crop impacts on corn nitrogen requirements in Southeastern South Dakota. Master of Science Thesis. South Dakota State University. <https://openprairie.sdstate.edu/etd/1017>
- Cook, J.C., Gallagher, R.S, Kaye, J.P., Lynch, J., Bradley, B., (2010). Optimizing vetch nitrogen production and corn nitrogen under No-Till Management. *Agron J.* 102,1491-1499. <https://doi.org/10.2134/agronj2010.0165>
- Crozier, C.R., Gehl, R.J., Hardy, D.H. and Heiniger, R.W. (2014), Nitrogen Management for High Population Corn Production in Wide and Narrow Rows. *Agron. J.*, 106, 66-72. <https://doi.org/10.2134/agronj2013.0280>
- Edmonds, D.E., Tubaña, B.S., Kelly, J.P., Crain, J.L., Edmonds, M.D., Solie, J.B., Taylor, R.K., Raun, W.R., 2013. Maize grain yield response to variable row nitrogen fertilization. *J. Plant Nutr.* 36(7), 1013-1024. <https://doi.org/10.1080/01904167.2011.585198>
- Ferdinand, L.J., Lamond, R.E., Gordon, W.B., Godsey, C.B., 2003. Fertilizer management for strip-till and no-till corn production. *Kansas Fertilizer Research* 2003, 78-81.
- <https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2003%20Kansas%20Fertilizer%20Research%20SRP921.pdf>
- Foster, T.J. 2012. The use of nitrogen timing and nitrification inhibitors as tools in corn and wheat production in Kansas. Master of Science Thesis. Department of Agronomy, Kansas State University. <http://hdl.handle.net/2097/17203>
- Franzluebbers, A.J., 2018. Soil-Test Biological Activity with the Flush of CO₂: III. Corn Yield Responses to Applied Nitrogen. *Soil Sci. Soc. Am. J.*, 82, 708-721. <https://doi.org/10.2136/sssaj2018.01.0029>
- Franzluebbers, A.J., Pershing, M.R., Crozier, C., Osmond, D., Schroeder-Moreno, M., 2018. Soil-Test Biological Activity with the Flush of CO₂: I. C and N Characteristics of Soils in Corn Production. *Soil Sci. Soc. Am. J.*, 82, 685-695. <https://doi.org/10.2136/sssaj2017.12.0433>
- Gehl, R.J., Schmidt, J.P., Maddux, L.D., Gordon, W.B., 2005. Corn yield response to nitrogen rate and timing in sandy irrigated soils. *Agron. J.*, 97, 1230-1238. <https://doi.org/10.2134/agronj2004.0303>
- Gordon, W.B., 2003. Controlled released urea for irrigated corn production. *Kansas Fertilizer Research* 2003, 66-68. <https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2003%20Kansas%20Fertilizer%20Research%20SRP921.pdf>
- Henry, D.C., Mullen, R.W., Dygert, C.E., Diedrick, K.A. and Sundermeier, A., 2010. Nitrogen contribution from red clover for corn following wheat in Western Ohio. *Agron. J.*, 102, 210-215. <https://doi.org/10.2134/agronj2009.0187>
- Hoben, J.P., Gehl, R.J., Millar, N., Grace, P.R., Robertson, G.P., 2011. Nonlinear nitrous oxide (N₂O) response to nitrogen fertilizer in on-farm corn crops of the US Midwest. *Global Change Biology* 17, 1140-1152. <https://doi.org/10.1111/j.1365-2486.2010.02349.x>
- Holland, K.H., Schepers, J.S., 2010. Derivation of a variable rate nitrogen application model for in-season fertilization of corn. *Agron. J.*, 102, 1415-1424. <https://doi.org/10.2134/agronj2010.0015>
- Holou, R.A.Y., Stevens, G., Kinomihou, V., 2011. Impact of nitrogen fertilization on nutrient removal by corn grain. *Crop Management*, 10, 1-9. <https://doi.org/10.1094/CM-2011-1223-02-RS>
- Janssen, K.A., Gordon, W.B., Lamond, R.E., 2006. Strip-till and no-till tillage/fertilizer systems compared for corn. *Kansas Fertilizer Research* 2006, 37-41. <https://doi.org/10.4148/2378-5977.3333>

Janssen, K.A., 2011. Evaluation of nitrogen rates and starter fertilizer for strip-till corn. *Kansas Fertilizer Research* 2010, 37-41. <https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2010%20Kansas%20Fertilizer%20Research%20SRP1049.pdf>

Kelley, K.W., Moyer, J.L., 2007. Effects of nitrogen fertilizer and previous double-cropping systems on subsequent corn yield. *Kansas Fertilizer Research* 2007, 15-17.

<https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2007%20Kansas%20Fertilizer%20Research%20SRP993.pdf> Kelley, K.W., Moyer, J.L., 2009. Effects of nitrogen fertilizer and previous double-cropping systems on subsequent corn yield. *Kansas Fertilizer Research* 2009, 71-73. <http://hdl.handle.net/2097/16970>

Kent, W.A., Coulter, J.A., Kaiser, D.E., Lambd, J.A., Vetsch, J.A., 2012. Continuous corn response to residue, sulfur and nitrogen management. ASA-CSSA-SSSA Annual Meeting. Visions for a Sustainable Planet. Oct. 21-24, 2012, OH. <https://scisoc.confex.com/crops/2012am/webprogram/Paper73050.html>

Lamond, R.E., Martin, V.L., Gordon, W.B., Olsen, C.J., 2001. Effects of nitrogen rates and sources on no-till corn. *Kansas Fertilizer Research* 2001, 63-64.

<https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2001%20Kansas%20Fertilizer%20Research%20SRP885.pdf>

Lindsey, A.J., Thomison, P.R., Barker, D.J. and Mullen, R.W., 2015. Drought-Tolerant Corn Hybrid Response to Nitrogen Application Rate in Ohio. *Crop, Forage & Turfgrass Management*, 1, 1-8 cftm2015.0168. <https://doi.org/10.2134/cftm2015.0168>

Ma, B.L., Subedi, K.D., Cota, C. 2005. Comparison of crop-based indicators with soil nitrate test for corn nitrogen requirement. *Agron. J.*, 97, 462-471. <https://doi.org/10.2134/agronj20055.0462> Maddux, L.D., 2008. Effect of various fertilizer materials on irrigated corn and dryland grain sorghum. *Kansas Fertilizer Research* 2008, 57-58. <https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2008%20Kansas%20Fertilizer%20Research%20SRP1012.pdf>

Mahama, G.Y., Prasad, P.V.V., Roozeboom, K.L., Nippert, J.B., Rice, C.W., 2016. Response of maize to cover crops, fertilizer nitrogen rates, and economic return. *Agron. J.*, 108, 17-31. <https://doi.org/10.2134/agronj15.0136>

Miller, E.C., 2014. I. Nitrogen and water use efficiency as influenced by maize hybrid and irrigation II. Predicting pre-plant nitrogen applications to maize using indicator crop N-rich reference strips. Doctor of Philosophy Dissertation. Oklahoma State University. <https://hdl.handle.net/11244/25687>

Mueller, N.D., Ruiz Diaz, D.A., Dille, J.A., Shoup, D.E., Mengel, D.B., Murray, L.W., 2013. Winter annual weed management and nitrogen rate effects on corn yield. *Agron. J.*, 105, 1077-1086. <https://doi.org/10.2134/agronj2012.0344>

Rajkovich, S., Osmond, D., Weisz, R., Crozier, C., Israel, D., Austin, R., 2017. Evaluation of nitrogen-loss prevention amendments in maize and wheat in North Carolina. *Agron. J.*, 109, 1811-1824. <https://doi.org/10.2134/agronj2016.03.0153>

Reese, C.L., Clay, D.E., Clay, S.A., Bich, A.D., Kennedy, A.C., Hansen, S.A., Moriles, J., 2014. Winter cover crops impact on corn production in semiarid regions. *Agron. J.*, 106, 1479-1488. <https://doi.org/10.2134/agronj13.0540>

Roberts, T.L., Slaton, N.A., Kelley, J.P., Greub, C.E., Fulford, A.M., 2016. Fertilizer nitrogen recovery efficiency of furrow-irrigated corn. *Agron. J.*, 108, 2123-2128. <https://doi.org/10.2134/agronj2016.02.0092>

Rudnick, D., Irmak, S., Ferguson, R., Shaver, T., Djaman, K., Slater, G., Dereuter, A. Ward, N., Francis, D., Schmer, M., Wienhold, B., Van Donk, S. 2016. Economic return versus crop water productivity of maize for various nitrogen rates under full irrigation, limited irrigation, and rainfed settings in south central Nebraska. *J. Irrig. Drain. Eng.* 142(6), 04016017. [https://doi.org/10.1061/\(ASCE\)IR.1943-4774.0001023](https://doi.org/10.1061/(ASCE)IR.1943-4774.0001023)

Ruf-Pachta, E.K., Rule, D.M., Dille, J.A., 2013. Corn and Palmer amaranth (*Amaranthus palmeri*) interactions with nitrogen in dryland and irrigated environments. *Weed Science*, 61(2), 249-258. <https://doi.org/10.1614/WS-D-11-00095.1>

- Ruiz Diaz, D.A., Hawkins, J.A., Sawyer, J.E., Lundvall, J.P., 2008. Evaluation of in-season nitrogen management strategies for corn production. *Agron. J.*, 100, 1711-1719. <https://doi.org/10.2134/agronj2008.0175>
- Ruiz-Diaz, D.A., 2007. Assessment of nitrogen supply from poultry manure applied to corn. Doctor of Philosophy Dissertation. Iowa State University. Retrospective theses and dissertations. 15603. <https://lib.dr.iastate.edu/rtd/15603>
- Santoro, M.J., 2018. Corn grain yield components and nutrient accumulation in response to nitrogen, plant density and hybrid. Master Science Thesis. University of Kentucky. Theses and Dissertations – Plant and Soil Sciences. <https://doi.org/10.13023/ETD.2018.064>
- Schwab, G.J., Murdock, L.W., 2005. Nitrogen fertilization of corn grown in Kentucky. <http://www.uky.edu/Ag/Agronomy/Extension/soils/Research/Nitrogen%20Fert.pdf>
- Shahandeh, H., Wright, A.L., Hons, F.M. 2011. Use of soil nitrogen parameters and texture for spatially-variable nitrogen fertilization. *Precision Agric* 12, 146–163. <https://doi.org/10.1007/s11119-010-9163-8>
- Sharma, L.K., 2014. Evaluation of active optical ground-based sensors to detect early nitrogen deficiencies in corn. Doctor of Philosophy Dissertation. North-Dakota State University. <https://hdl.handle.net/10365/27309>
- Sharma, L.K., Bu, H., Denton, A., Franzen, D.W., 2015. Active-Optical Sensors Using Red NDVI Compared to Red Edge NDVI for Prediction of Corn Grain Yield in North Dakota, U.S.A. *Sensors*, 15(11), 27832-27853. <https://doi.org/10.3390/s151127832>
- Sharma, L.K., Bu, H., Franzen, D.W., 2016a. Comparison of Two Ground-Based Active-Optical Sensors for In-Season Estimation of Corn (*Zea mays*, L.) Yield. *J. Plant Nutr.*, 39, 957-966. <https://doi.org/10.1080/01904167.2015.1109109>
- Sharma, L.K., Franzen, D.W., Denton, A., 2016b. Use of corn height measured with an acoustic sensor improves yield estimation with ground based active optical sensors. *Computers and Electronics in Agriculture*, 124, 254-262. <https://doi.org/10.1016/j.compag.2016.04.016>
- Shepard, A., Thomison, P., Nafziger, E., Mullen, R., Clucas, C., 2011. NutriDense corn response to nitrogen rates. *Agron. J.*, 103, 169-174. <https://doi.org/10.2134/agronj2010.0313>
- Sindelair, A.J., Coulter, J.A., Lamb, J.A., Vetsch, J.A., 2015. Nitrogen, stover, and tillage management affect nitrogen use efficiency in continuous corn. *Agron. J.* 107, 843–850 (2015) <https://doi.org/10.2134/agronj14.0535>
- Sindelar, A.J., Coulter, J.A., Lamb, J.A., Vetsch, J., 2013, Agronomic Responses of Continuous Corn to Stover, Tillage, and Nitrogen Management. *Agron. J.*, 105, 1498-1506. <https://doi.org/10.2134/agronj2013.0181>
- Sistani, K.R., Simmons, J.R., Warren, J.G., Higgins, S., 2017. Nitrogen source and application method impact on corn yield and nutrient uptake. *J. Plant Nutr.*, 40(6), 878-889. <https://doi.org/10.1080/01904167.2016.1262410>
- Torino, M.S., Ortiz, B.V., Fulton, J.P., Balkcom, K.S., Wood, C.W., 2014. Evaluation of vegetation indices for early assessment of corn status and yield potential in the southeastern United States. *Agron. J.*, 106, 1389-1401. <https://doi.org/10.2134/agronj13.0578>
- Tremblay, N., Bouroubi, Y.M., Bélec, C., Mullen, R.W., Kitchen, N.R., Thomason, W.E., Ebelhar, S., Mengel, D.B., Raun, W.R., Francis, D.D., Vories, E.D. Ortiz-Monasterio, I., 2012. Corn response to nitrogen is influenced by soil texture and weather. *Agron. J.*, 104, 1658-1671. <https://doi.org/10.2134/agronj2012.0184>
- Tucker, A.N., 2010. Nitrogen management of corn with sensor technology. Doctor of Philosophy Dissertation. Kansas State University. <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.870.9450&rep=rep1&type=pdf>

- Walker, Z.T., Coulter, J.A., Russelle, M.P., Venterea, R.T., Mallarino, A.P., Lauer, J.G., Yost, M.A. 2017. Do soil tests help forecast nitrogen response in first-year corn following alfalfa on fine-textured soils? *Soil Sci. Soc. Am. J.*, 81, 1640-1651. <https://doi.org/10.2136/sssaj2017.06.0183>
- Walsh, O., Raun, W., Klatt, A., Solie, J., 2012. Effect of delayed nitrogen fertilization on maize (*Zea mays* L.) grain yields and nitrogen use efficiency. *J. Plant Nutr.*, 35(4), 538-555. <https://doi.org/10.1080/01904167.2012.644373>
- Wheeler, J., 2014. Nitrogen rate optimization for grain yield within fall and spring applications. Master of Science Thesis. University of Illinois. Theses and Dissertations, 125. <https://ir.library.illinoisstate.edu/etd/125>
- Williams, J.D., Crozier, C.R., White, J.G., Heiniger, R.W., Sripada, R.P., Crouse, D.A., 2007a. Illinois soil nitrogen test predicts Southeastern U.S. Corn economic optimum nitrogen rates. *Soil Sci. Soc. Am. J.*, 71, 735-744. <https://doi.org/10.2136/sssaj2006.0135>
- Williams, J.D., Crozier, C.R., White, J.G., Sripada, R.P., Crouse, D.A., 2007b. Comparison of Soil Nitrogen Tests for Corn Fertilizer Recommendations in the Humid Southeastern USA. *Soil Sci. Soc. Am. J.*, 71, 171-180. <https://doi.org/10.2136/sssaj2006.0057>
- Williams, J.D., Kitchen, N.R., Scharf, P.C., Stevens, W.E., 2010. Within-field nitrogen response in corn related to aerial photograph color. *Precision Agric* 11, 291-305. <https://doi.org/10.1007/s11119-009-9137-x>
- Wortmann, C.S., Tarkalson, D., Shapiro, C. Dobermann, A., Ferguson, R., Hergert, G., Walters, D., 2011. Nitrogen use efficiency of irrigated corn for three cropping systems in Nebraska. *Agron. J.* 103, 76-84. <https://doi.org/10.2134/agronj2010.0189>
- Yost, M.A., Coulter, J.A., Russelle, M.P., 2013. First-year corn after alfalfa showed no response to fertilizer nitrogen under no-tillage. *Agron. J.* 105, 208-214. <https://doi.org/10.2134/agronj2012.0334>
- Yost, M.A., Coulter, J.A., Russelle, M.P., Sheaffer, C.C., Kaiser, D.E., 2012. Alfalfa nitrogen credit to first-year corn: Potassium, regrowth, and tillage timing effects. *Agron. J.* 104, 953-962. <https://doi.org/10.2134/agronj2011.0384>
- Yost, M.A., Morris, T.F., Russelle, M.P., Coulter, J.A., 2014. Second-year corn after alfalfa often requires no fertilizer nitrogen. *Agron. J.*, 106, 659-669. <https://doi.org/10.2134/agronj2013.0362>
- Zhu, Q., Schmidt, J.P., Bryant, R.B., 2015. Maize (*Zea mays* L.) yield response to nitrogen as influenced by spatio-temporal variations of soil-water-topography dynamics. *Soil and Tillage Res.* 146(B), 174-183. <https://doi.org/10.1016/j.still.2014.10.006>

Supplementary material

Chapter 3: Unraveling uncertainty drivers of the maize yield response to nitrogen:

A Bayesian and machine learning approach

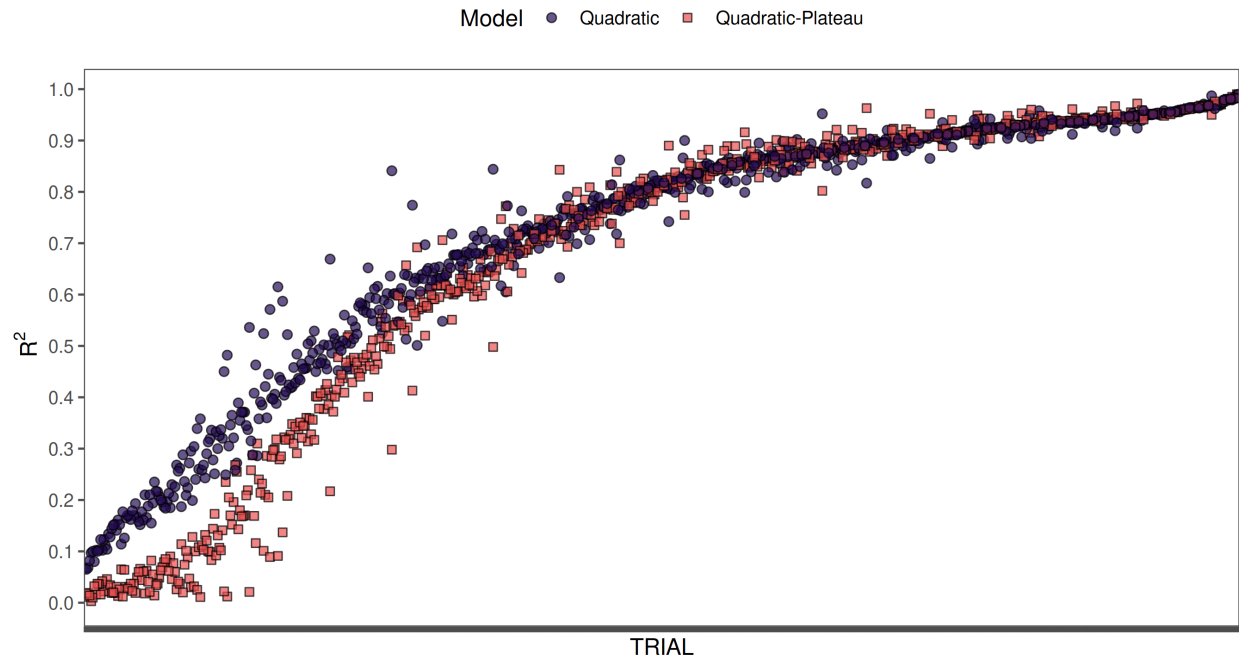
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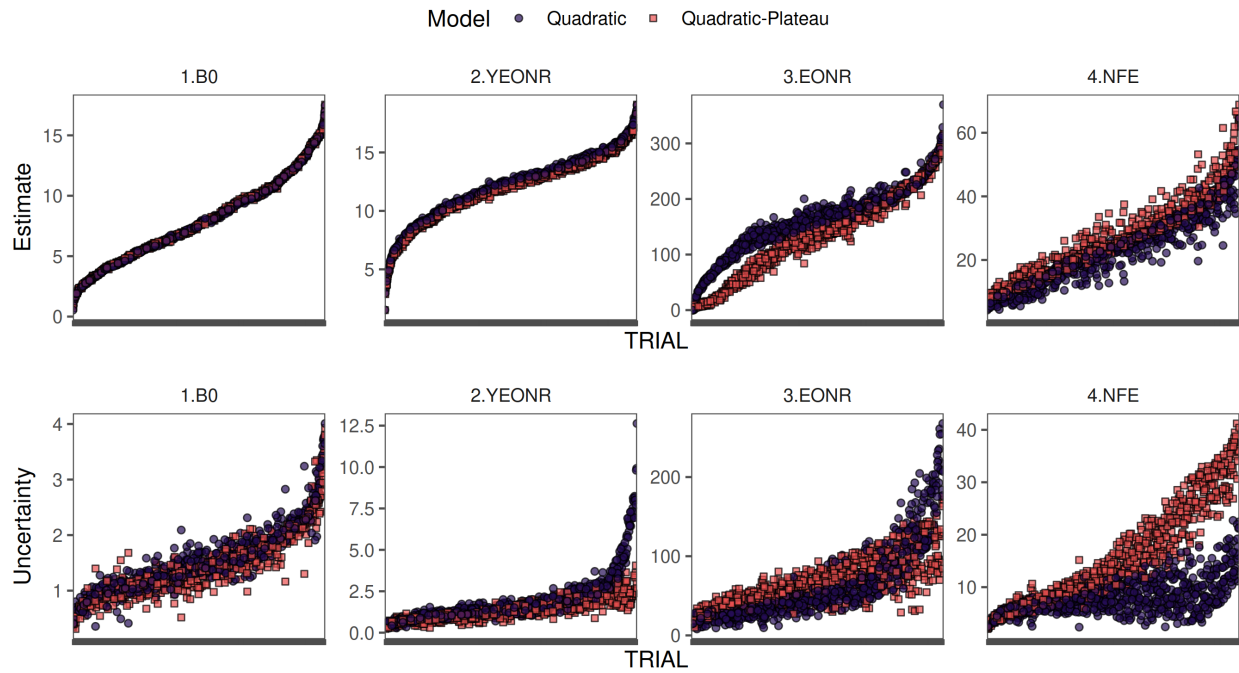
Supp. Figure 3.1.

Comparison of performance (R^2 median from posterior samples) obtained with quadratic and quadratic-plateau models for the 730 maize N response curves under study.



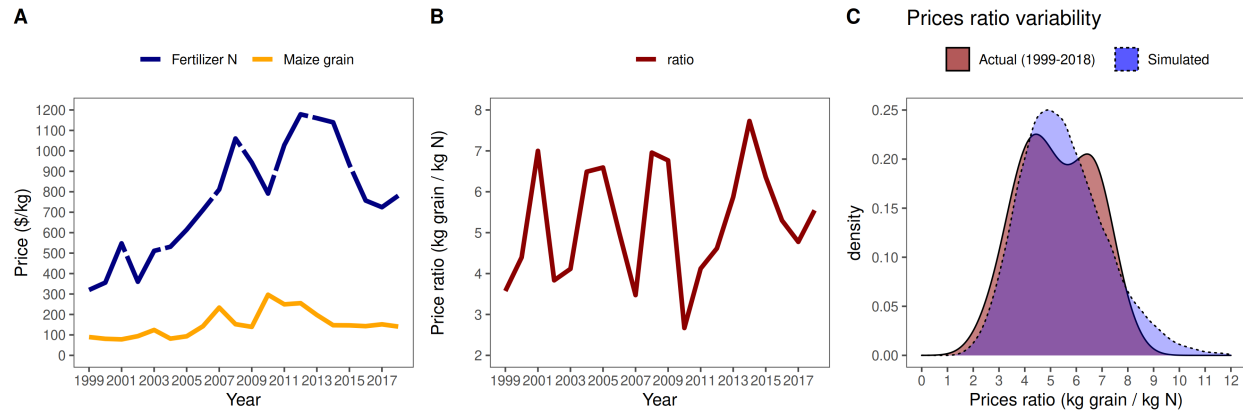
Supp. Figure 3.2.

Comparison of maize N response descriptors of interest (B0, YEONR, EONR, NFE) obtained with quadratic and Quadratic-Plateau models for the 730 maize N response curves under study.



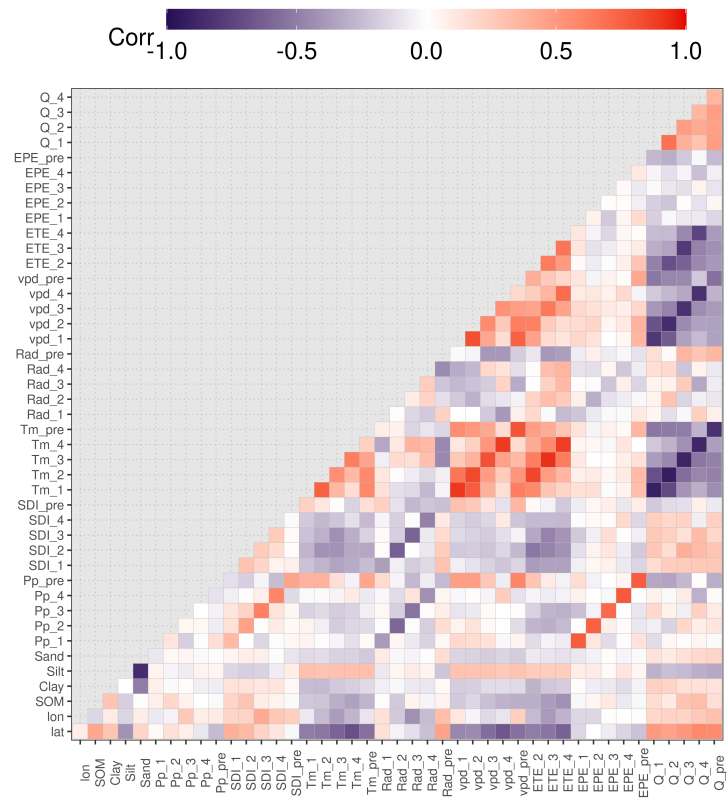
Supp. Figure 3.3.

Historical (1999-2018) maize grain and fertilizer N prices (A), prices ratios (B), and actual and simulated probability distributions of prices ratios (C). Simulated prices ratio distribution was used as a prior in the Bayesian analysis framework, representing a stochastic component associated with prices variability when performing the EONR calculations.



Supp. Figure 3.4.

Correlation matrix showing the linear association among the continuous covariates used for predicting the components (B0, YEONR, EONR, NFE) of maize yield response to N.



Supp. Table 3.1.

Data references, number of curves (site-years), states and years covered by each source.

Source	Reference	Curves (site-years)	State/s	Year/s
1	Asebedo (2015)	4 (4)	KS	2012-2014
2	Berg (2016)	14 (2)	SD	2014-2015
3	Correndo and Ciampitti (pers. comm.)	4 (2)	KS	2019, 2020
4	Corteva Agrisciences (pers. comm.)	109 (19)	IA, IL, IN, MN, MO, NE, SD, TN, WI	2011-2019
5	Coulter (pers. comm.)	10 (10)	MN	2015
6	Crozier et al. (2014)	3 (3)	NC	2010-2012
7	Foster 2014	5 (5)	KS	2012-2013
8	Gordon (2003)	1 (1)	KS	2003
9	Hoben et al. (2011)	7 (7)	MI	2007-2008
10	Holland and Schepers (2010)	3 (3)	NE	2002-2004
11	Janssen et al. (2011)	4 (4)	KS	2006-2010
12	Lindsey et al. (2015)	16 (4)	OH	2013-2014
13	Miller et al. (2017)	4 (4)	OK	2013-2014
14	Nafziger (pers. comm.)	134 (68)	IL	1999-2008
15	Rajkovich et al. (2017)	4 (4)	NC	2014-2015
16	Rudnick et al. (2016)	9 (3)	NE	2012-2014
17	Ruiz-Diaz (2007)	6 (2)	IA	2005-2006
18	Ruiz-Diaz et al. (2008)	30 (30)	IA	2004-2006
19	Shahandeh et al. (2011)	5 (3)	TX	2005-2007
20	Sharma (2014); Sharma et al. (2015, 2016a, 2016b)	48 (48)	ND	2011-2013
21	Shepard et al. (2011)	8 (8)	IL, OH	2006-2007
22	Sindelar et al. (2013; 2015)	30 (6)	MN	2009-2012
23	Steinke (pers. comm.)	17 (15)	MI	2011-2018
24	Torino et al. (2014)	10 (8)	AL	2010-2012
25	Tremblay (pers. comm.)	79 (79)	CAN	2000-20009
26	Tremblay et al. (2012)	41 (41)	IL, KS, MO, NE, OH, OK, VA, CAN	2006-2009
27	Tucker (2010)	9 (9)	KS	2006-2009
28	Walker et al. (2018)	14 (14)	MN	2014
29	Wheeler (2014)	7 (7)	IL	2013
30	Wortmann et al. (2011)	32 (32)	NE	2002-2004
31	Yost et al. (2012; 2013; 2014)	58 (32)	MN	2009-2012
32	Zhu et al. (2015)	1 (1)	PA	2009

Supp. Table 3.2.

Details of metrics (scoring rules) used for the assessment of agreement between predicted and observed values of B0, YEONR, EONR, and NFE. P_i : predicted value for the i^{th} trial; O_i : observed value at the i^{th} trial; n : size of the learning sample.

#	Scoring rule	Details	Formula
1	RMSE	Root mean square error	$\sqrt{\frac{1}{n} \sum_{i=1}^n (P_i - O_i)^2}$
2	RRMSE	Relative RMSE	$\frac{\sqrt{\frac{1}{n} \sum_{i=1}^n (P_i - O_i)^2}}{\bar{O}}$
3	MBE	Mean bias error	$\frac{1}{n} \sum_{i=1}^n (P_i - O_i) = \bar{P} - \bar{O}$
4	ME	Nash-Sutcliffe model efficiency	$1 - \frac{\sum_{i=1}^n (P_i - \bar{O})^2}{\sum_{i=1}^n (O_i - \bar{O})^2}$
5	KGE	Kling-Gupta model efficiency	$1 - \sqrt{(r - 1)^2 + (\frac{s_P}{s_O} - 1)^2 + (\frac{\bar{P}}{\bar{O}} - 1)^2}$
6	CCC	Concordance correlation coefficient	$\frac{2s_{PO}}{s_P^2 + s_O^2 + (\bar{O} - \bar{P})^2}$
7	R ²	Coefficient of determination	$\frac{s_{PO}^2}{s_P^2 s_O^2}$

where,

$$s_P = \sqrt{\frac{1}{n} \sum_{i=1}^n (P_i - \bar{P})^2}$$

$$s_O = \sqrt{\frac{1}{n} \sum_{i=1}^n (O_i - \bar{O})^2}$$

$$s_{PO} = \frac{1}{n} \sum_{i=1}^n (P_i - \bar{P})(O_i - \bar{O})$$

and

$$r = \frac{s_{PO}}{s_P s_O}$$

References (Supp. Table 3.1)

Asebedo, A.R. 2015. Development of sensor-based nitrogen recommendation algorithms for cereal crops. Doctor of Philosophy Dissertation. Department of Agronomy, Kansas State University. <http://hdl.handle.net/2097/19229>

Berg, S.L., 2016. Evaluation of tillage, crop rotation, and cover crop impacts on corn nitrogen requirements in Southeastern South Dakota. Master of Science Thesis. South Dakota State University. <https://openprairie.sdstate.edu/etd/1017>

Crozier, C.R., Gehl, R.J., Hardy, D.H. and Heiniger, R.W. (2014), Nitrogen Management for High Population Corn Production in Wide and Narrow Rows. Agron. J., 106, 66-72. <https://doi.org/10.2134/agronj2013.0280>

Foster, T.J. 2012. The use of nitrogen timing and nitrification inhibitors as tools in corn and wheat production in Kansas. Master of Science Thesis. Department of Agronomy, Kansas State University. <http://hdl.handle.net/2097/17203>

- Gordon, W.B., 2003. Controlled released urea for irrigated corn production. *Kansas Fertilizer Research* 2003, 66-68. <https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2003%20Kansas%20Fertilizer%20Research%20SRP921.pdf>
- Hoben, J.P., Gehl, R.J., Millar, N., Grace, P.R., Robertson, G.P., 2011. Nonlinear nitrous oxide (N₂O) response to nitrogen fertilizer in on-farm corn crops of the US Midwest. *Global Change Biology* 17, 1140–1152. <https://doi.org/10.1111/j.1365-2486.2010.02349.x>
- Holland, K.H., Schepers, J.S., 2010. Derivation of a variable rate nitrogen application model for in-season fertilization of corn. *Agron. J.*, 102, 1415-1424. <https://doi.org/10.2134/agronj2010.0015>
- Janssen, K.A., 2011. Evaluation of nitrogen rates and starter fertilizer for strip-till corn. *Kansas Fertilizer Research* 2010, 37-41. <https://www.agronomy.k-state.edu/services/soiltesting/publications-and-reports/documents/kansas-fertilizer-researcher-reports/2010%20Kansas%20Fertilizer%20Research%20SRP1049.pdf>
- Lindsey, A.J., Thomison, P.R., Barker, D.J. and Mullen, R.W., 2015. Drought-Tolerant Corn Hybrid Response to Nitrogen Application Rate in Ohio. *Crop, Forage & Turfgrass Management*, 1, 1-8 cftm2015.0168. <https://doi.org/10.2134/cftm2015.0168>
- Miller, E.C., Bushong, J.T., Raun, W.R., Joy, M., Abit, M., and Arnall, Brian, D., 2017. Predicting early season nitrogen rates of corn using indicator crops. *Agron. J.* 109, 2863-2870. <https://doi.org/10.2134/agronj2016.09.0519>
- Rajkovich, S., Osmond, D., Weisz, R., Crozier, C., Israel, D., Austin, R., 2017. Evaluation of nitrogen-loss prevention amendments in maize and wheat in North Carolina. *Agron. J.*, 109, 1811-1824. <https://doi.org/10.2134/agronj2016.03.0153>
- Rudnick, D., Irmak, S., Ferguson, R., Shaver, T., Djaman, K., Slater, G., Dereuter, A. Ward, N., Francis, D., Schmer, M., Wienhold, B., Van Donk, S. 2016. Economic return versus crop water productivity of maize for various nitrogen rates under full irrigation, limited irrigation, and rainfed settings in south central Nebraska. *J. Irrig. Drain. Eng.* 142(6), 04016017. [https://doi.org/10.1061/\(ASCE\)IR.1943-4774.0001023](https://doi.org/10.1061/(ASCE)IR.1943-4774.0001023)
- Ruiz Diaz, D.A., Hawkins, J.A., Sawyer, J.E., Lundvall, J.P., 2008. Evaluation of in-season nitrogen management strategies for corn production. *Agron. J.*, 100, 1711-1719. <https://doi.org/10.2134/agronj2008.0175>
- Ruiz-Diaz, D.A., 2007. Assessment of nitrogen supply from poultry manure applied to corn. Doctor of Philosophy Dissertation. Iowa State University. Retrospective theses and dissertations. 15603. <https://lib.dr.iastate.edu/rtd/15603>
- Shahandeh, H., Wright, A.L., Hons, F.M. 2011. Use of soil nitrogen parameters and texture for spatially-variable nitrogen fertilization. *Precision Agric* 12, 146–163. <https://doi.org/10.1007/s11119-010-9163-8>
- Sharma, L.K., 2014. Evaluation of active optical ground-based sensors to detect early nitrogen deficiencies in corn. Doctor of Philosophy Dissertation. North-Dakota State University. <https://hdl.handle.net/10365/27309>
- Sharma, L.K., Bu, H., Denton, A., Franzen, D.W., 2015. Active-Optical Sensors Using Red NDVI Compared to Red Edge NDVI for Prediction of Corn Grain Yield in North Dakota, U.S.A. *Sensors*, 15(11), 27832-27853. <https://doi.org/10.3390/s151127832>
- Sharma, L.K., Bu, H., Franzen, D.W., 2016a. Comparison of Two Ground-Based Active-Optical Sensors for In-Season Estimation of Corn (*Zea mays*, L.) Yield. *J. Plant Nutr.*, 39, 957-966. <https://doi.org/10.1080/01904167.2015.1109109>
- Sharma, L.K., Franzen, D.W., Denton, A., 2016b. Use of corn height measured with an acoustic sensor improves yield estimation with ground based active optical sensors. *Computers and Electronics in Agriculture*, 124, 254-262. <https://doi.org/10.1016/j.compag.2016.04.016>
- Shepard, A., Thomison, P., Nafziger, E., Mullen, R., Clucas, C., 2011. NutriDense corn response to nitrogen rates. *Agron. J.*, 103, 169-174. <https://doi.org/10.2134/agronj2010.0313>

- Sindelair, A.J., Coulter, J.A., Lamb, J.A., Vetsch, J.A., 2015. Nitrogen, stover, and tillage management affect nitrogen use efficiency in continuous corn. *Agron. J.* 107, 843–850 (2015) <https://doi.org/10.2134/agronj14.0535>
- Sindelar, A.J., Coulter, J.A., Lamb, J.A., Vetsch, J., 2013. Agronomic Responses of Continuous Corn to Stover, Tillage, and Nitrogen Management. *Agron. J.*, 105, 1498-1506. <https://doi.org/10.2134/agronj2013.0181>
- Torino, M.S., Ortiz, B.V., Fulton, J.P., Balkcom, K.S., Wood, C.W., 2014. Evaluation of vegetation indices for early assessment of corn status and yield potential in the southeastern United States. *Agron. J.*, 106, 1389-1401. <https://doi.org/10.2134/agronj13.0578>
- Tremblay, N., Bouroubi, Y.M., Bélec, C., Mullen, R.W., Kitchen, N.R., Thomason, W.E., Ebelhar, S., Mengel, D.B., Raun, W.R., Francis, D.D., Vories, E.D. Ortiz-Monasterio, I., 2012. Corn response to nitrogen is influenced by soil texture and weather. *Agron. J.*, 104, 1658-1671. <https://doi.org/10.2134/agronj2012.0184>
- Tucker, A.N., 2010. Nitrogen management of corn with sensor technology. Doctor of Philosophy Dissertation. Kansas State University. <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.870.9450&rep=rep1&type=pdf>
- Walker, Z.T., Coulter, J.A., Russelle, M.P., Venterea, R.T., Mallarino, A.P., Lauer, J.G., Yost, M.A. 2017. Do soil tests help forecast nitrogen response in first-year corn following alfalfa on fine-textured soils? *Soil Sci. Soc. Am. J.*, 81, 1640-1651. <https://doi.org/10.2136/sssaj2017.06.0183>
- Wheeler, J., 2014. Nitrogen rate optimization for grain yield within fall and spring applications. Master of Science Thesis. University of Illinois. Theses and Dissertations, 125. <https://ir.library.illinoisstate.edu/etd/125>
- Wortmann, C.S., Tarkalson, D., Shapiro, C. Dobermann, A., Ferguson, R., Hergert, G., Walters, D., 2011. Nitrogen use efficiency of irrigated corn for three cropping systems in Nebraska. *Agron. J.* 103, 76–84. <https://doi.org/10.2134/agronj2010.0189>
- Yost, M.A., Coulter, J.A., Russelle, M.P., 2013. First-year corn after alfalfa showed no response to fertilizer nitrogen under no-tillage. *Agron. J.* 105, 208–214. <https://doi.org/10.2134/agronj2012.0334>
- Yost, M.A., Coulter, J.A., Russelle, M.P., Sheaffer, C.C., Kaiser, D.E., 2012. Alfalfa nitrogen credit to first-year corn: Potassium, regrowth, and tillage timing effects. *Agron. J.* 104, 953–962. <https://doi.org/10.2134/agronj2011.0384>
- Yost, M.A., Morris, T.F., Russelle, M.P., Coulter, J.A., 2014. Second-year corn after alfalfa often requires no fertilizer nitrogen. *Agron. J.*, 106, 659-669. <https://doi.org/10.2134/agronj2013.0362>
- Zhu, Q., Schmidt, J.P., Bryant, R.B., 2015. Maize (*Zea mays* L.) yield response to nitrogen as influenced by spatio-temporal variations of soil–water-topography dynamics. *Soil and Tillage Res.* 146(B), 174-183. <https://doi.org/10.1016/j.still.2014.10.006>

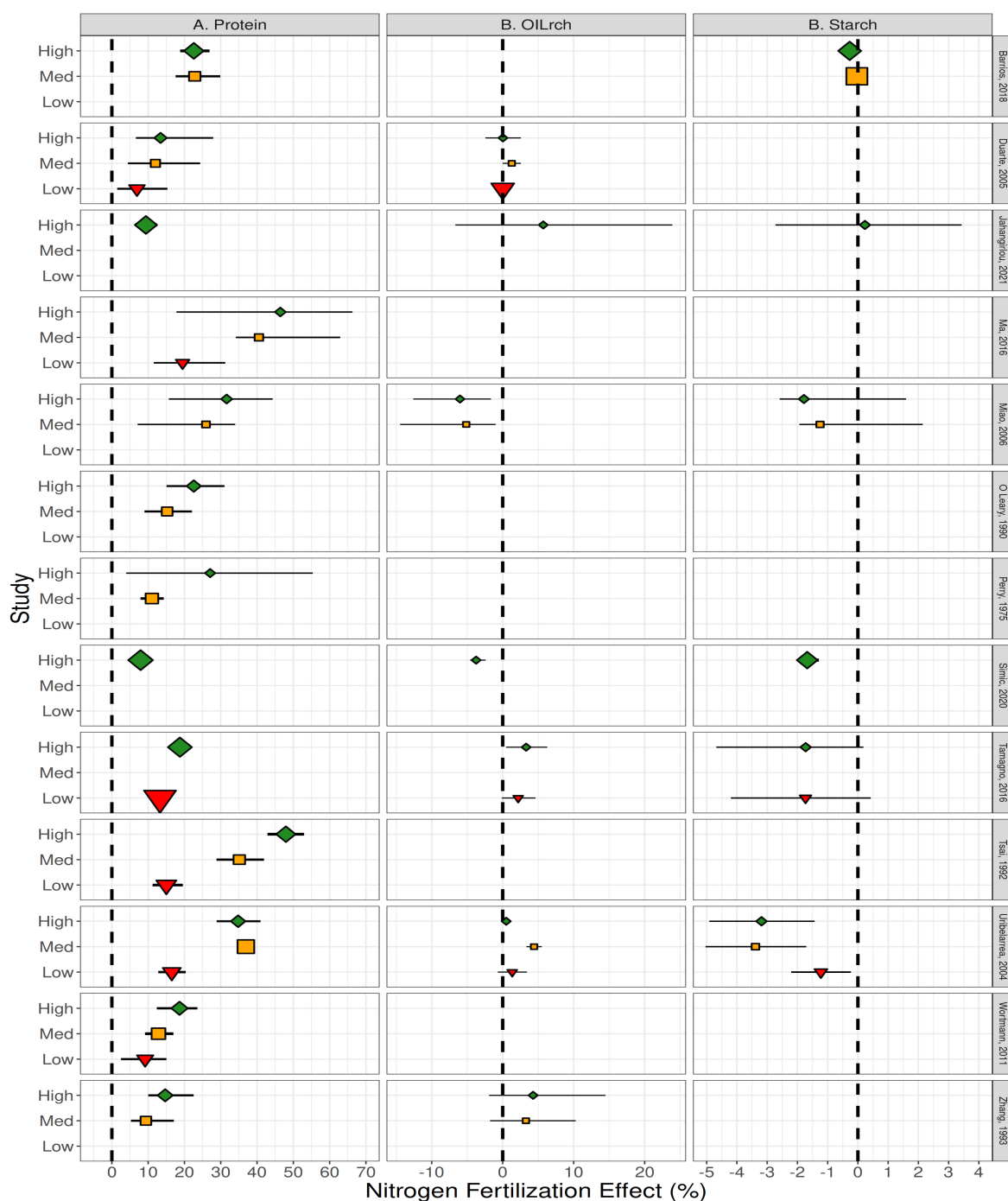
Supplementary Material

Chapter 4: Do water and nitrogen management practices impact maize grain quality?

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Supplementary Figure 4.2. By-study summary of effect sizes (%) of nitrogen fertilization on maize grain quality components (A – Protein, B – Starch, and C – Oil) considering the rate level (Low $<70 \text{ kg N ha}^{-1}$, Med $71\text{-}150 \text{ kg N ha}^{-1}$, and High $>150 \text{ kg N ha}^{-1}$). Within each variable, symbols represent the mean effect, shape size represents the weight, and whiskers their respective 95% confidence intervals (CI, whiskers), which were transformed from $\ln\text{RR}$ into percentage ($\exp(\ln\text{RR})-1 \times 100$), as the protein, starch or oil concentration variation in N fertilized compared to their respective control (0 kg N ha^{-1}).

Supplementary Material

Chapter 5: Footprints of maize nitrogen management on the following soybean crop

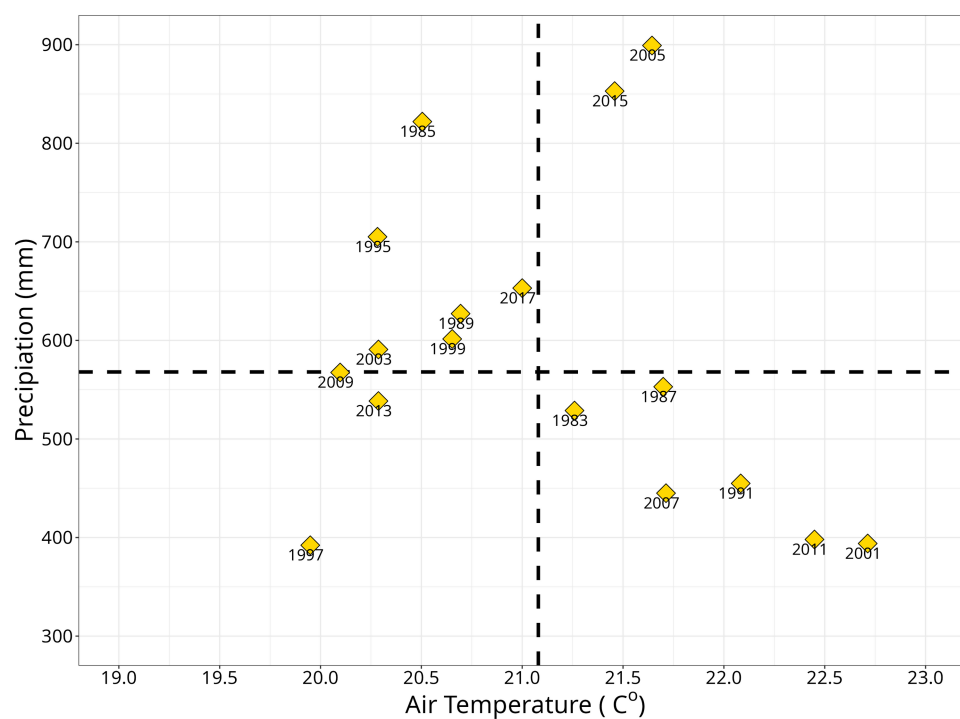
Author:

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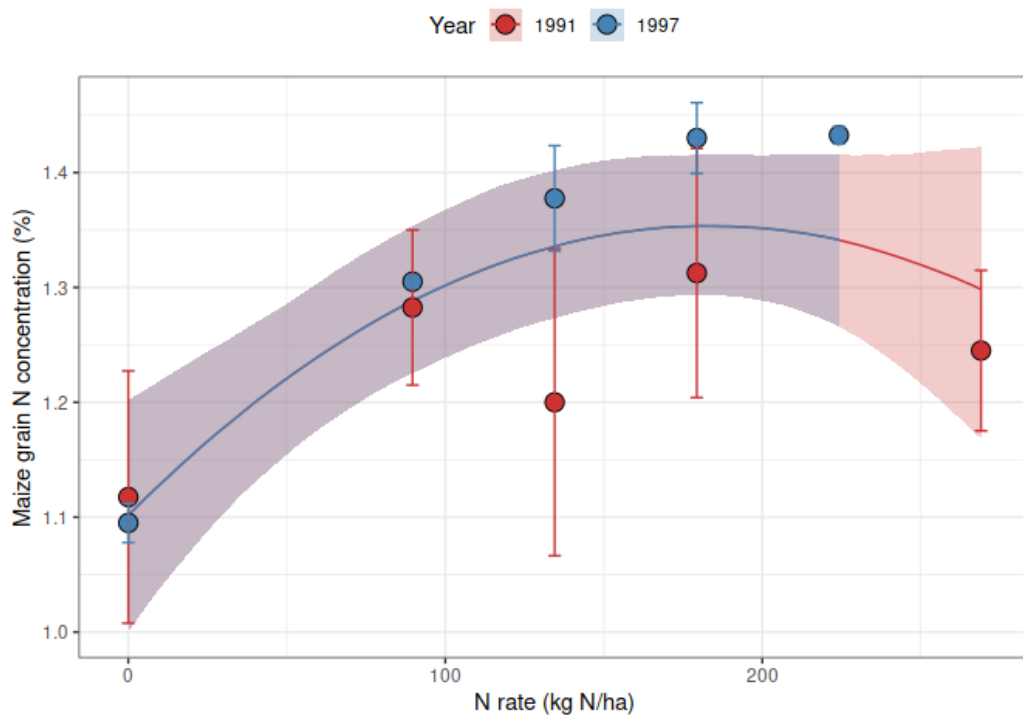
e-mail: correndo@ksu.edu

Supplementary Table 5.1. General soil and crop management practices at the long-term maize-soybean rotation nutrition trial. Kansas River Valley Experiment Field, Topeka, KS.

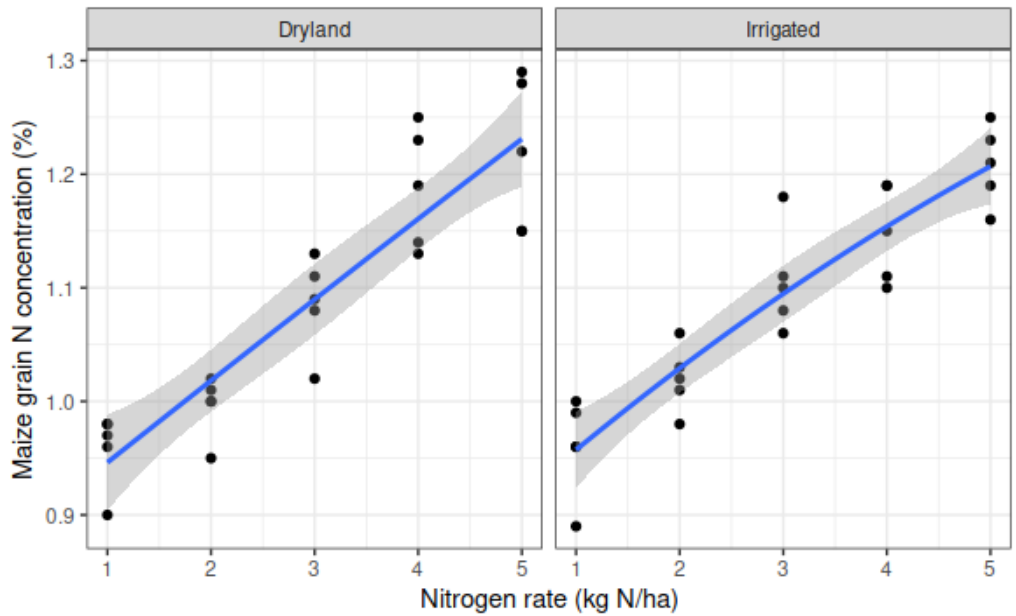
Crop	Year	Hybrid or Variety	Seed rate (seeds m⁻²)	Sowing date	Harvest date	Irrigation (mm)
Maize	1983	BoJac 603	6.2	04-21	09-09	243
	1985	Pioneer 3377	6.2	04-16	09-04	149
	1987	Pioneer 3377	6.2	04-22	09-02	228
	1989	Pioneer 3377	6.4	04-18	09-18	418
	1991	Jacques 7820	6.2	04-09	09-05	287
	1993	Jacques 7820	6.2	04-22	09-17	0
	1995	Mycogen 7250	6.2	04-06	09-25	153
	1997	DeKalb DKC626	6.2	-	-	92
	1999	DeKalb DKC626	7.1	04-13	-	108
	2001	Golden Harvest H2547	7.1	04-20	10-02	162
	2003	Pioneer 33R77	7.1	04-11	09-16	235
	2005	DeKalb DKC63-81	7.1	04-18	10-07	96
	2007	Asgrow RX785	7	04-23	09-06	106
	2009	DeKalb DKC63-42		05-06	-	25
	2011	DeKalb DKC63-49	6.8	04-18	09-06	180
	2013	Pioneer 1151	7.1	04-30	09-24	244
	2015	Pioneer 1105	7.6	04-14	09-10	164
	2017	Pioneer 1257	7.5	04-25	09-20	204
	2019	Pioneer 1197	7.8	04-22	09-16	110



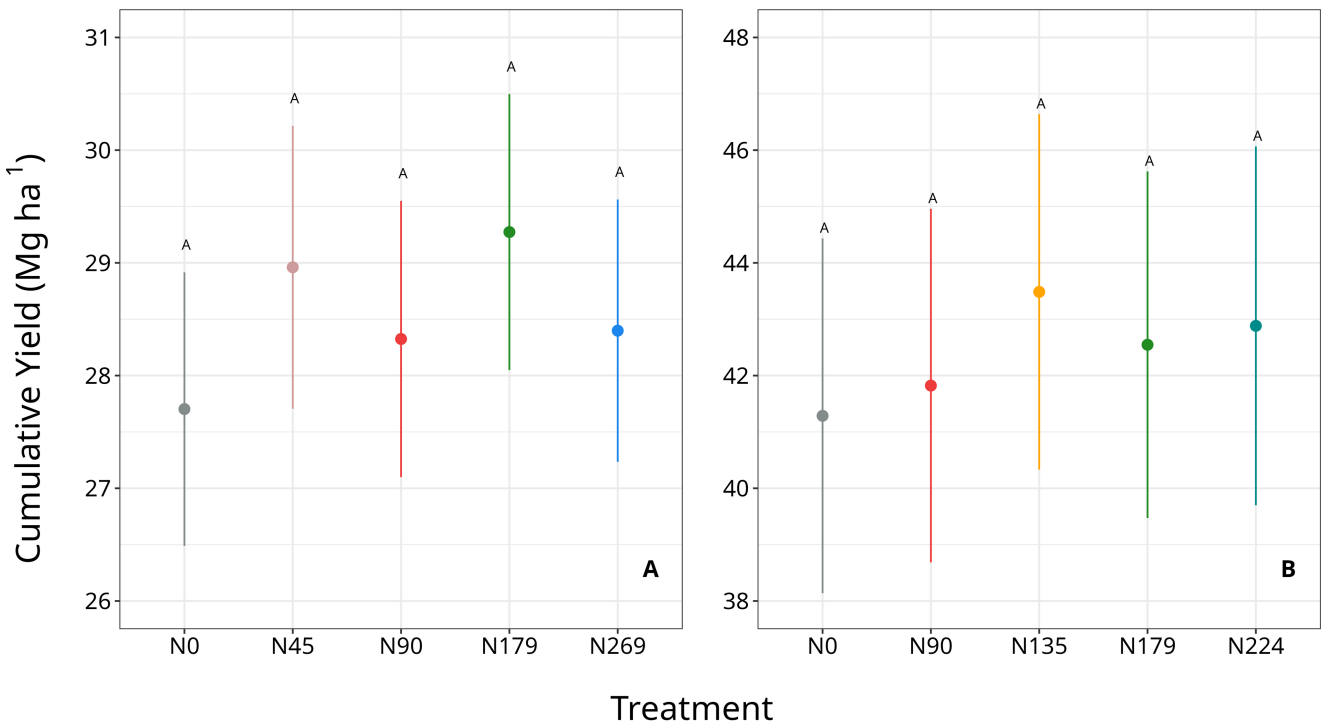
Supplementary Figure 5.1. Weather classification of maize cropping seasons over time. Case study I, Kansas River Valley Field Experiment.



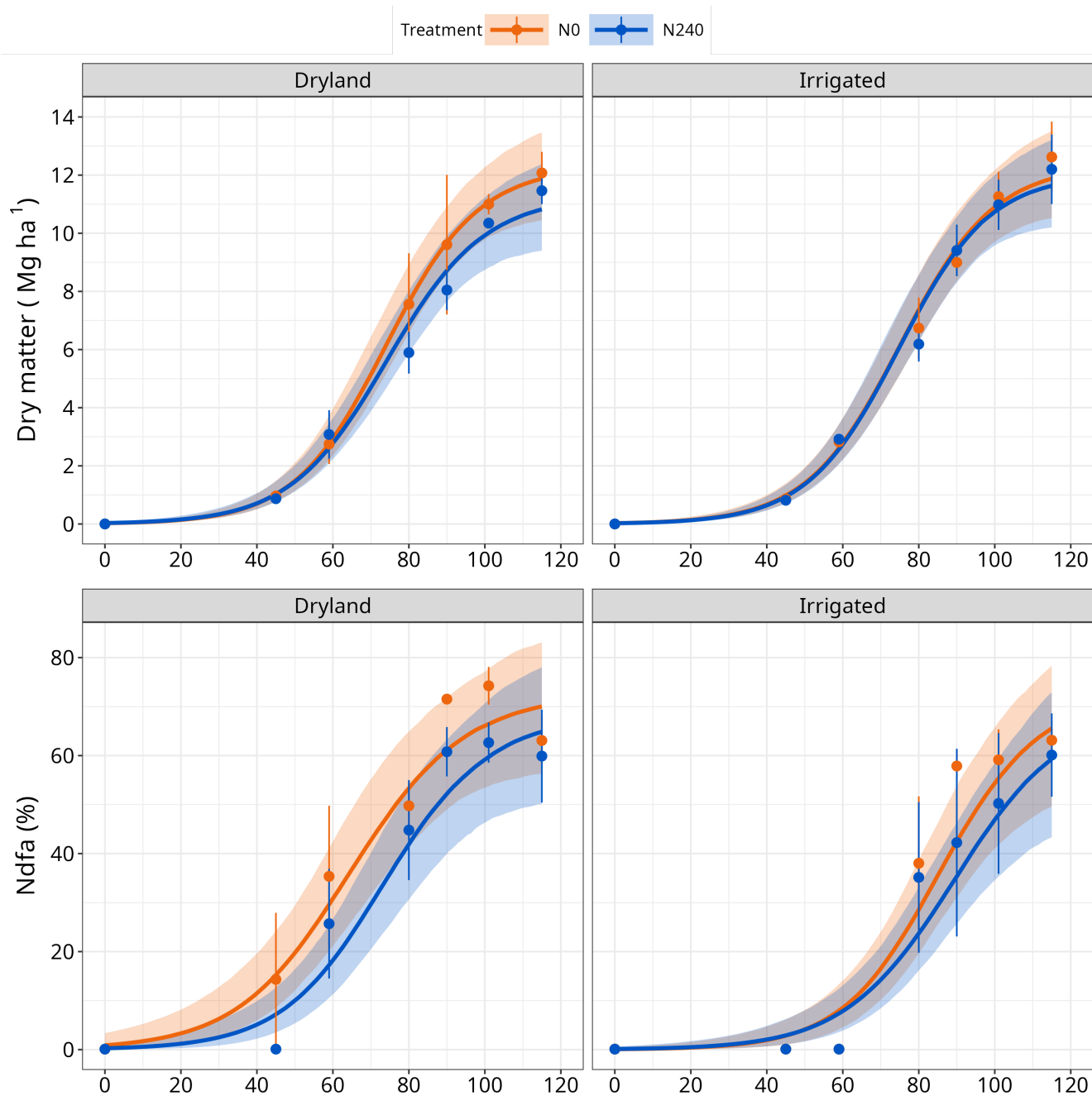
Supplementary Figure 5.2A. Model of maize grain N concentration as a function of N rate based on 1991 and 1997 measurements. Case study II.



Supplementary Figure 5.2B. Model of maize grain N concentration as a function of N rate. Case study II. 2019 cropping season.



Supplementary Figure 5.3. Accumulated soybean seed production (Mg ha^{-1}) depending on different N rates on the previous maize crops over the years for the two periods under study (A: 1983-1994, and B: 1997-2020) in the case study I, Kansas River Valley Experiment Field, Topeka, Kansas. Whiskers represent the 95%-credible intervals (from Bayesian posterior distributions).



Supplementary Figure 5.4. Soybean dry matter accumulation (Mg ha^{-1}) and nitrogen derived from atmosphere (Ndfa, %) during the 2020 cropping season. Case study II. Scandia, KS.

Supplementary Material

Chapter 6: Revisiting linear regression to test agreement in continuous predicted-observed datasets

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Supplementary material for Section 6.2. Theoretical framework.

1. Symmetry in the error-in-variables model.

The parameter (slope and intercept) estimators for the general model Eq. (1) can be expressed Eq. (2) (y vs. x) and as X_i as a function of Y_i , Eq. (3), where γ and ϕ represent the intercept and slope, respectively.

$$\begin{aligned} y_i &= Y_i + \varepsilon_i, \\ x_i &= X_i + \mu_i, \\ Y_i &= \alpha + \beta X_i. \end{aligned} \quad (1)$$

$$\hat{y}_i = \hat{\alpha} + \hat{\beta} x_i, \quad (2)$$

$$\hat{x}_i = \hat{\gamma} + \hat{\phi} y_i. \quad (3)$$

This distinction is particularly relevant for the OLS regression where the orientation matters. If we select a model that is asymmetric (OLS) and project Eq. (2) and Eq. (3) in the same axis-orientation (y as vertical, x as horizontal), they will produce two different regression lines (**Figure 6.2A-B**). In contrast, if the selected model is symmetric, lines derived from Eq. (2) and Eq. (3) will be coincident and algebraically invertible (*i.e.*, reciprocal slopes, $\hat{\beta} = 1/\hat{\phi}$), which is the case of MA and SMA models.

2. Estimating the intercept

For all the regression models here, the estimation of the intercept ($\hat{\alpha}$) is simply reduced to **Eq. (4)**, which is ultimately dependent on the previous estimation of the slope ($\hat{\beta}$) (Warton et al., 2006). This simplification takes advantage of these regression lines passing through the centroid of the data given by the variable means coordinates ($\bar{x}$, $\bar{y}$).

$$\hat{\alpha} = \bar{y} - \hat{\beta} \bar{x}. \quad (4)$$

3. Background of error decomposition using linear regression

This section is intended to offer a comparison, up to our knowledge, of the three main approaches in the literature to decompose error using linear regression. As we provided evidence in the article, SMA offers results closer to optimal as compared to the alternative approaches.

3.1. Error decomposition with OLS-line

Willmott (1981) proposed the utilization of two error indices as additive components of the MSE. In order to provide a geometric interpretation of the components proposed by Willmott (1981), we multiply *MSE* by the sample size (*n*) and express the decomposition in terms of the total sum of squares (*TSS*). Using OLS regression of *P* vs. *O*, Willmott proposed following *TSS* components (**Supplementary Table 1**): i) the sum of unsystematic differences (*SUD*), related to imprecision, and ii) the sum of systematic differences (*SSD*), related to inaccuracy.

Geometrically, *SUD_{OLS}* represents the sum of the areas of *n* squares obtained from the difference between the actual *P_i* and the value given by the OLS-line ($\hat{P}_i$) (**Supplementary Figure 1A**); while *SSD_{OLS}* represents the sum of the areas of *n* squares obtained from the difference between the OLS-line and the 1:1 line (where *P_i* = *O_i*) (not shown). Willmott (1981) proposed the sum of *SUD_{OLS}* plus *SSD_{OLS}* as equal to *TSS*. Therefore, unsystematic and systematic proportions of the error can be simply estimated as ratios of the components to the *TSS*. This represents a very simple and straightforward approach. For example, the illustrative dataset displayed on **Supplementary Figure 1A** has a *TSS* = 38.25, being *SUD_{OLS}* = 21.53, *SSD_{OLS}* = 16.72 (See **Correndo et al. (2021) for demonstration**). Nonetheless, the use of a symmetric regression model such as the SMA (instead of OLS) to estimate the line-of-best-fit would result in a more reliable summary-line and thus error decomposition, as demonstrated below.

3.2. Error decomposition with MA-line

Duveiller et al. (2016) proposed an alternative method to decompose the square error but using a symmetric regression. Their approach consists in using the MA residuals (h_i) to obtain the unsystematic error component. Authors estimate the MA-line (and its residuals) by deriving the first principal component and its eigenvalues from the variance-covariance matrix (See Supplementary material of Duveiller et al. (2016)). The residuals of the MA line, h_i (**Supplementary Figure 1C**), can be considered the radius of a square. Based on this, authors propose the sum of unsystematic differences (SUD_{MA}) equal to the sum of $2h_i^2$. Geometrically, SUD_{MA} was designed to represent the sum of (rotated) squares area, which diagonal ($2h_i$) is perpendicular to the MA line (**Supplementary Figure 1B**). However, , since SUD_{MA} is based on a different data-projection (rotated axis, $x'y'$), this approach offers an independent estimation of the unsystematic component. Unfortunately, this implies that SUD_{MA} cannot be considered as an additive component of the sum of squares -TSS- (based on the original xy -projection), which is our intention -See **Correndo et al. (2021) for demonstration**-. Consequently, Duveiller et al. (2016) have not specified a formula for the computation of the systematic error component.

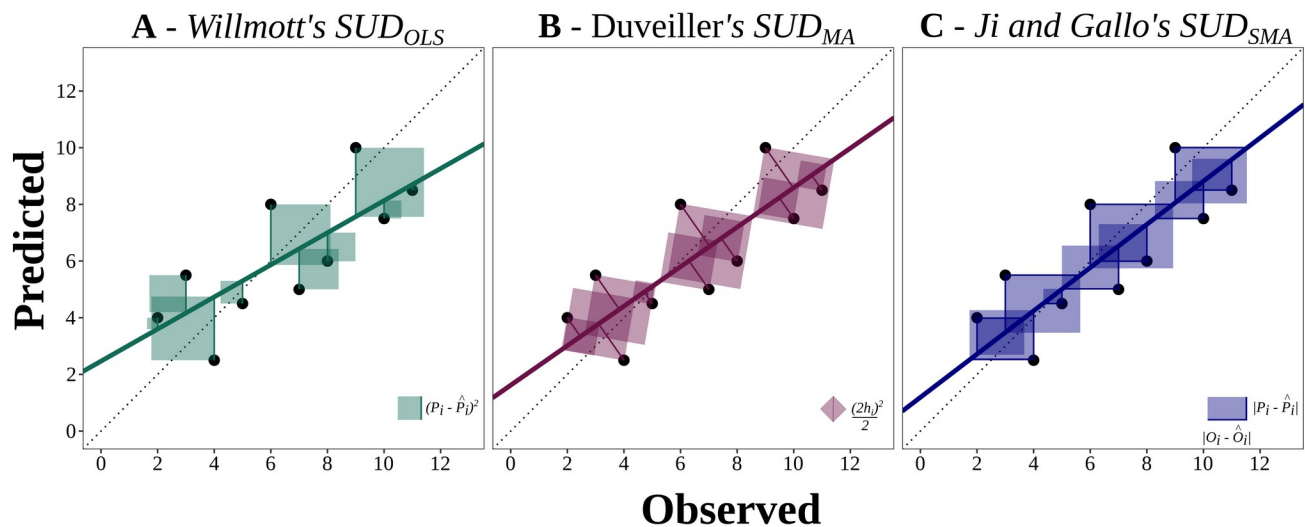
3.3. Error decomposition with SMA-line

The third alternative for error decomposition uses SMA regression, referred by authors as geometric mean functional relationship (Ji and Gallo, 2006). Authors proposed the sum of unsystematic differences (SUD_{SMA}) as equal to the loss function minimized by the SMA-line (**Supplementary Table 1**). This corresponds to the sum of product of differences between the SMA-line and both P_i and O_i values simultaneously. Geometrically, the SUD_{SMA} represents the sum of “triangle-rectangles” formed from the difference between the data points (P_i, O_i) and the SMA-line (**Supplementary Figure 1C**). Authors assumed that $SSD_{SMA} = TSS - SUD_{SMA}$ but have not specified the formula for it. However, it is possible to specify SSD_{SMA} as the sum of square differences between the SMA-line and the 1:1-line (**Supplementary Table 1**). This can be done in two equivalent forms: i) as the sum of square differences between the SMA-line-values for observed ($\hat{O}_i$) and the 1:1-line-values (where $O_i = P_i$); or ii) as the sum of square differences between the SMA-line-values for predicted ($\hat{P}_i$) and the 1:1 line-values (where $P_i = O_i$). Geometrically, the SSD_{SMA} represents the sum of the area of n squares formed between the SMA-line and the 1:1 line (**Supplementary Figure 1C**). Thus, it can be proven that the

sum of SUD_{SMA} (n rectangles) + SSD_{SMA} (n squares) = TSS (n squares). Results then intuitive that as the SMA-line approaches the 1:1 line, the lack of accuracy will approach zero ($SSD_{SMA} \rightarrow 0$), and most of the error will be on the unsystematic (lack of precision) component ($SUD_{SMA} \rightarrow TSS$).

Supplementary Table 6.1. Error decomposition using alternative regression lines. For Willmott (1981), $\hat{P}_i$ represents the fitted value of P obtained from the OLS regression of P vs. O.

Error Components	OLS	MA	SMA
	<i>Willmott (1981)</i>	<i>Duveiller et al. (2016)</i>	<i>Adapted from Ji and Gallo (2006)</i>
Total Sum of Squares (TSS)	$\sum_{i=1}^n (O_i - P_i)^2$		
Sum of Unsystematic Differences (SUD) -lack of precision-	$\sum_{i=1}^n (P_i - \hat{P}_i)^2$	$\sum_{i=1}^n 2h_i^2$	$\sum_{i=1}^n P_i - \hat{P}_i O_i - \hat{O}_i $
Sum of Systematic Differences (SSD) -lack of accuracy-	$\sum_{i=1}^n (O_i - \hat{P}_i)^2$	-	$\sum_{i=1}^n (O_i - \hat{P}_i)^2,$ $\equiv$ $\sum_{i=1}^n (P_i - \hat{O}_i)^2.$
Notes	$TSS = SUD_{OLS} + SSD_{OLS}$	No SSD term	$TSS = SUD_{SMA} + SSD_{SMA}$



Supplementary Figure 6.1. Geometric representation of the sum of unsystematic differences proposed by Willmott (1981) (A, SUD_{OLS}), Duveiller et al. (2016) (B, SUD_{MA}), and Ji and Gallo (2006) (C, SUD_{SMA}), using asymmetric (A) and symmetric regression lines (B, C). $SUD_{OLS} = 21.53$; $SUD_{MA} = 30.87$, $SUD_{SMA} = 32.39$.

REFERENCES

- Correndo, A.A., Hefley, T., Holzworth, D., Ciampitti, I.A., 2021. R-Code Tutorial: Revisiting linear regression to test agreement in continuous predicted-observed datasets. *Harvard Dataverse*, V3. <https://doi.org/10.7910/DVN/EJS4M0>
- Duveiller, G., Fasbender, D., Meroni, M., 2016. Revisiting the concept of a symmetric index of agreement for continuous datasets. *Sci. Rep.* 6, 1–14. <https://doi.org/10.1038/srep19401>
- Ji, L., Gallo, K., 2006. An agreement coefficient for image comparison. *Photogramm. Eng. Remote Sensing.* 7, July 2006, 823-833. <https://doi.org/10.14358/PERS.72.7.823>
- Willmott, C.J., 1981. On the validation of models. *Phys. Geogr.* 2, 184–194. <https://doi.org/10.1080/02723646.1981.10642213>