Flow condensation heat transfer enhancement in a mini-channel with hydrophobic and hydrophilic patterns

Melanie M. Derby, Abhra Chatterjee, Yoav Peles, Michael K. Jensen

How to cite this manuscript

If you make reference to this version of the manuscript, use the following information:


Published Version Information


Copyright: © 2013 Elsevier Ltd.


Publisher’s Link: http://www.sciencedirect.com/science/article/pii/S0017931013007989

This item was retrieved from the K-State Research Exchange (K-REx), the institutional repository of Kansas State University. K-REx is available at http://krex.ksu.edu
Flow condensation heat transfer enhancement in a mini-channel with hydrophobic and hydrophilic patterns

Melanie M. Derby a,b,*, Abhra Chatterjee a, Yoav Peles a, Michael K. Jensen a

a Department of Mechanical, Aerospace, and Nuclear Engineering
Rensselaer Polytechnic Institute
Troy, NY 12180, United States

b Department of Mechanical and Nuclear Engineering
Kansas State University
Manhattan, KS 66502, United States

* Corresponding author

Telephone: 1 785 532 2606
Fax: 1 785 532 7057
Contact E-mail: derbym@ksu.edu
Abstract

The study examined the enhancement of flow condensation of steam on hydrophobic and hydrophilic surfaces. Six 1.06 mm mini-gaps were tested at pressures of 350kPa to 400kPa, average qualities of 0.2 to 0.95 and mass fluxes of 50 to 200 kg/m²s. The surfaces included hydrophilic copper, hydrophobic Teflon AF™, and four surfaces with combined Teflon and hydrophilic patterns; pattern selection was guided by an analytical model. Condensing heat transfer coefficients on hydrophobic and hydrophobic/hydrophilic patterned surfaces reached a value of up to 425,000 W/m²K, surpassing the hydrophilic surface by an order of magnitude. Enhancement factors of 3.2 to 13.4 times that of the hydrophilic channel were found in the hydrophobic channel; combined with a lack of dependence on mass flux or quality, the data strongly suggested that dropwise condensation was promoted and sustained throughout the flow condensation process on hydrophobic and patterned surfaces. For the hydrophilic copper mini-gap, heat transfer coefficients were a strong function of quality, as well as a function of mass flux at higher qualities, which demonstrated the development and growth of a liquid film as quality decreased, and were well predicted by the Kim et al. (2013) correlation, with a mean average error of 8.9%.

Keywords: Condensation, hydrophobic, hydrophilic, pattern, minichannel, microchannel
1. Introduction

Condensers are found in numerous industrial applications, such as power plants and water desalination systems, and more compact and effective condensers would reduce the systems’ size and weight while increasing power. In order to create improved condensers, fundamental advancements in condensation are needed. Macro-scale condensation has been well documented after over fifty years of study [1, 2]. More recently, smaller diameter channels have been shown to offer higher heat transfer coefficients than macro channels, yet mini- and micro-scale condensation has only been explored for the last ten to fifteen years [3, 4]. Despite larger heat transfer coefficients achieved by researchers at the mini- and micro-scales, few enhancements other than channel shape have been found at the mini- and micro-scale. Dropwise condensation, on external surfaces and in vapor space, offered an order of magnitude enhancement in heat transfer coefficients [5-13] but has seldom been applied to internal flows. However, promotion of dropwise condensation in internal condensation would reduce condenser size.

Condensation in mini- and micro-channels has garnered great interest over the last decade with an emphasis on refrigerants used for electronics cooling and miniaturized vapor compression cycles. Hydraulic diameter, mass flux, quality, and flow regime have been identified as the governing parameters of filmwise condensation. Heat transfer coefficients have been generally found to increase as diameter decreases at the mini- and micro-scales [14-16]. Condensation heat transfer coefficients increased with increasing mass flux and quality [3, 4, 17-20], with a few exceptions found at lower mass fluxes [14, 21]. Flow regimes affected condensation behavior; the absence of stratified flow, and the presence of annular flow at the mini- and micro-scales suggested that gravity does not play a significant role in small scale condensation [17, 20, 22-25].
Although mini- and micro-scale condensation heat transfer coefficients are higher than those found at the macro-scale, efforts to further enhance condensation heat transfer have focused on channel shape. In non-circular channels, condensate gathers in corners due to surface tension, thinning the liquid film in areas away from corners and enhancing the heat transfer coefficient. However, depending on channel length and other variables, length-averaged heat transfer coefficients in a circular tube may be higher or lower than a rectangular channel [14, 26]. It was expected that shapes with sharp corners would yield heat transfer enhancements [27], yet this has not been observed in all studies [28, 29].

Surface modification, though rarely applied to internal flows, has dramatically enhanced external condensation. Fang et al. [16, 30] studied micro-scale steam condensation in silicon channels coated with self-assembled monolayers, thus creating hydrophobic, hydrophilic, and semi-hydrophobic surfaces. A film wetted the hydrophilic channel walls, while dropwise condensation at the inlet of the hydrophobic channel yielded a slightly (15%) higher heat flux compared to the hydrophilic tube. In contrast, significant enhancement has been found by promoting dropwise condensation of steam on external tubes and plates, which offered heat flux enhancements of 5 to 20 times that of filmwise condensation under the same conditions [5-13]. Surface modifications promote dropwise condensation by altering contact angles or lowering surface energies, using methods such as coating with polymers [31, 32] and self-assembled monolayers [33, 34], altering surface roughness [8] [11, 35], electroplating [36], and ion implantation [10].

There was an apparent tradeoff in two studies which examined the coexistence of dropwise and filmwise condensation on external surfaces; in one study [37], performance was superior when dropwise condensation existed on top of the tube and filmwise on the bottom, as the disruption of the liquid film by falling droplets enhanced heat transfer. In another study [38],
the best configuration was when filmwise condensation was on the upper part of the flat plate and dropwise condensation was on the lower part, since film rivulets would clean the dropwise condensation surface. Since the majority of heat transfer occurs through the smallest drops in dropwise condensation [39], droplet sweeping reduces droplet size, thus increasing heat transfer [40-42].

As there have been few studies on internal flow condensation enhancement other than channel shape, the objective of this study is to understand the effects of surface modifications on condensation in a mini-gap. Surface modifications promote dropwise condensation, and the condensation enhancement of hydrophobic surfaces is examined.

2. Experimental Method and Apparatus

In order to achieve dropwise condensation in an internal flow, patterned hydrophobic/hydrophilic surfaces were fabricated in a 1.06-mm mini-gap. Six patterns were selected to test on the basis of analytical modeling. Condensation heat transfer coefficients were measured and tested in an open loop steam experimental apparatus.

2.1 Analytical modeling for pattern selection

An analytic model guided the selection of hydrophobic/hydrophilic patterns. The geometry was a mini-gap with specified height, \( d \), and cooled length, \( L_{\text{tot}} \); the channel was cooled on one side and assumed to be adiabatic on the remaining three (Fig. 1). The cooled length contained both hydrophilic and hydrophobic strips. At a specified quality, it was assumed that all liquid gathered on hydrophilic segments with a specified contact angle \( \beta \), determined from experiments. The liquid droplet was modeled using a parabola, and the integral of all liquid droplets yielded the total liquid area. Also, the number of hydrophilic strips was specified by the user, and the remaining area was hydrophobic.
The length of the channel occupied by liquid, and thus filmwise condensation, $L_{FWC}$, was

$$L_{FWC} = NL_{droplet}$$

for droplets on $N$ hydrophilic areas of length $L_{droplet}$, while the length occupied by dropwise condensation $L_{PWC}$ was the difference between the total length and filmwise condensation length.

The area occupied by liquid was then related to the void fraction according to:

$$1 - \alpha = \frac{A_l}{dL_{tot}}$$

Butterworth [43] determined a simple curve fit based on the work of Lockhart and Martinelli [2] to relate void fraction to quality via the Martinelli parameter $X$,

$$\alpha = \frac{1}{1 + 0.28X^{0.71}}$$

where $X$ was defined for four cases. The flow was assumed to be laminar, such that the pertinent Martinelli parameter $X_{vv}$ for viscous liquid-viscous vapor was defined as

$$X_{vv} = \left(\frac{1 - X}{X}\right)\frac{\rho_l \mu_l}{\rho_v \mu_v}$$

where the fluid properties (liquid and vapor densities, $\rho_l$ and $\rho_v$, and liquid and vapor viscosities, $\mu_l$ and $\mu_v$) were evaluated for steam. The Butterworth [43] equation linked the void fraction,
obtained through geometry, to quality—a parameter of interest because condensation heat transfer coefficients have been found to be a strong function of quality [3, 28, 44].

The remaining variables were dropwise and filmwise condensation heat transfer coefficients, $h_{DWC}$ and $h_{FWC}$. Due to the lack of reported dropwise condensation in internal flow, the dropwise condensation heat transfer coefficient was approximated using the work of Baojin et al. [8], who observed dropwise condensation heat transfer coefficients of 60,000 W/m²K for steam condensation on a vertical, unmodified titanium surface with 80% dropwise condensation coverage. For the purposes of this model, dropwise condensation heat transfer coefficients on the hydrophobic condensation surface were conservatively estimated to be 40,000 W/m²K. The filmwise heat transfer coefficient was calculated directly from the average film thickness in the hydrophilic areas, and length-averaged heat transfer coefficients were estimated,

$$h_{\text{avg}} = \frac{h_{DWC} + h_{FWC}}{2}.$$

The number of hydrophilic strips, $N$, and quality were supplied as inputs to the model, while the model predicted the length of hydrophilic strip $L_{\text{droplet}}$ and subsequently, the length-averaged heat transfer coefficient. The dropwise condensation heat transfer coefficient was approximated from a study of condensation with low flow rates on a vertical, unmodified titanium surface; the area averaged heat transfer coefficient for 80% dropwise condensation was 60,000 W/m²K [8], and the hydrophobic dropwise condensation heat transfer coefficients for this model were conservatively estimated to be 40,000 W/m²K. At qualities of 0.95, the length-averaged heat transfer coefficients remained close to the assumed dropwise condensation value. However, as quality decreased, the model showed a significant effect of the number of hydrophilic strips on the average heat transfer coefficient. In Fig. 2, the left hand side represents fewer, larger liquid droplets, and as the number of hydrophilic strips increased, there are more,
smaller droplets. At lower qualities ($x<0.50$) more, smaller hydrophilic strips mean that a larger channel length is occupied by liquid in order to fit the same volume of liquid. At low qualities ($x=0.05$), liquid on only one hydrophilic strip ($N=1$) spread over a length of 1.6 mm (17% of the channel total), while the four droplets ($N=4$) combined accounted for 3.1 mm (33%) of the channel. Fewer hydrophilic strips were predicted to be more effective at achieving higher condensation heat transfer coefficients, because the droplets occupied less of the total length, thus exposing more area to the high dropwise condensation heat transfer coefficients.

As a result of this modeling, six surfaces were selected and fabricated: completely hydrophilic ($N\to\infty$), completely hydrophobic ($N=0$), and four patterned surfaces ($N=1,2,3,$ and 7).

### 2.2 Hydrophobic/hydrophilic surface patterning

Hydrophilic surfaces promote filmwise condensation, but it was hypothesized that hybrid hydrophobic/hydrophilic surfaces would gather the liquid on the hydrophilic regions, thus promoting dropwise condensation in the hydrophobic regions. Oxygen-free copper surfaces were coated with Teflon AF™ and selectively patterned to form hydrophobic and hydrophilic patterned surfaces for condensation. Due to the size of the copper coupon, dip-coating the Teflon was the preferred application method, following a procedure similar to that used for the creation of pool boiling surfaces by Betz et al. [45]. First, selected regions, such as the coupon backside and thermocouple holes, were covered in Kapton tape to prevent Teflon coating. Next, the copper channel was cleaned with isopropyl alcohol and plasma etched. The surfaces were then dipped in a solution of Teflon AF 1601S, 6% solids dissolved in FC72, diluted (1:24) with solvent FC40. Once coated, the coupons were heated at 165 °C for 24 hours to evaporate the
solvent. The process was successful in creating a conformal Teflon coating of thickness 260 nm ± 25 nm, as determined through destructive testing and imaging (Fig. 3). The contact angles of water on untreated hydrophilic copper and hydrophobic Teflon AF™ surfaces were measured using an optical goniometer (Fig. 4) and were 40° and 120°, respectively.

After coating with Teflon, patterns were transferred from a patterned silicon hard mask to the channel via a plasma etch, creating hydrophobic/hydrophilic surfaces. The area under the hard mask remained hydrophobic, while the Teflon coating was selectively removed, exposing the hydrophilic copper surface. Patterned surfaces were created for \( N = 1, 2, 3, \) and 7, as well as completely hydrophilic \( (N=0) \) and completely hydrophobic \( (N\to\infty) \), Fig. 5 and Fig. 6. Since the channels were 100 mm in length, silicon hard masks were fabricated from six-inch (0.15 m) wafers, and created using a lithography and deep reactive ion etching process. A method was successfully developed to create patterned surface, detailed in Derby [46].

**2.3 Test section design**

The condensation test section (Fig. 7) consisted of two parts: an interchangeable coupon which was joined to a heat flux measuring base; steam flowed through a 0.56 mm by 9.6 mm mini-gap channel (hydraulic diameter 1.06 mm) machined into the coupon’s top surface.; a large surface area was available for patterning. The mini-gap coupon was joined to the base with high thermal conductivity indium and indium-silver 0.05 mm thick solder ribbon preforms (Indium Corp. of America) and aligned with Teflon alignment pins.

The test section was designed to accurately measure heat flux, wall temperature, quality, and fluid temperature. Unlike boiling experiments, where heater power can be easily obtained, heat flux measurements in condensation are difficult [47]. “Heat flux was measured in three distinct measuring segments (Fig. 8), by five 0.8-mm diameter sheathed thermocouples in each
segment, installed in 1-mm diameter wholes with a thin layer of thermal grease. The
temperature gradient was calculated over a maximum transverse distance of 32 mm, and
Fourier’s law was utilized to measure heat flux [28, 48]. Wall temperatures were measured
directly via three thermocouples installed in the coupon itself. For single-phase flow, fluid
temperatures were determined indirectly through a series of energy balances on the test section;
in the same manner, quality was determined from a series of energy balances for two-phase flow.
For two-phase flows, the inlet pressure and pressure drop across the test section were measured;
pressure was determined at the center of each measuring segment using a linear pressure drop
model, and the fluid temperature was calculated to be the saturation temperature for that
pressure.

Steam entered and exited the mini-gap through a stainless steel cover plate at an angle of
35° from horizontal, to lessen heat transfer enhancement from impingement. An o-ring seal
joined the cover plate and coupon; additionally, the mating copper surface was coated with
Teflon to prevent galvanic corrosion. Cooling was provided at the heat flux measuring base by
an aluminum plate heat exchanger, and thermal grease was applied the interface. The entire test
section assembly was compressed by six bolts in order to seal and promote good thermal contact
between parts.

2.4 Apparatus

An open loop (Fig. 9) allowed for a wide range of test section qualities and mass fluxes.
Steam at 440 kPa was filtered by seven 40-μm parallel filters, and then passed through a
separation tank to ensure near-saturated steam. Exiting high quality steam was then superheated
30-50 °C, ensuring that enthalpy before the pre-condenser could be accurately calculated through
temperature and pressure measurements (Omega PX303-300A5V) after the pre-heater. A short
or long tube-in-tube counterflow pre-condenser was used, cooled via open loop city water, to set a wide variety of different test section inlet qualities; the pre-condenser outlet quality was calculated through a cooling water energy balance using measured water mass flow rates and temperature differences. To obtain the highest test section inlet qualities, the loop was used without a pre-condenser. A 4-kW heater was installed on the cooling water side to vary the cooling water inlet temperature from 10 °C to 50 °C to further adjust pre-condenser outlet/test section inlet quality. Cooling water mass flow rate and pressure (above atmospheric) were controlled to suppress undesirable sub-cooled boiling on the cooling water side.

Steam entered the test section with a known quality. Temperature and absolute pressure (Omega PX303-100A5V) were measured at the test section inlet (needed for calculating enthalpy for single-phase validation cases) and was used to check saturation temperature and pressure for two-phase cases. Exit pressure was obtained from a differential pressure transducer (Setra model 230), and the pressure drop set the fluid temperature inside the test section. Since small quality changes were set across the test section, a tube-in-tube, city water cooled post-condenser condensed the remaining steam fully, enabling the condensate mass flow rate to be measured downstream of the test section with a weigh tank and stopwatch. Additionally, a valve after the post-condenser and before the rotameter regulated the flow and suppressed flow instabilities, and the rotameter permitted the visualization of steady flow rates.

2.5 Experimental Procedures
Tests were run at steady state conditions. First, cooling water flow rates were set in the test section, post-condenser, and pre-condenser (if applicable). Once steady cooling water temperatures and flow rates were obtained, steam entered the system at a desired flow rate, and the two pre-heaters were switched on, superheating the steam 30-50°C above the supplied steam saturation temperature (142°C – 144°C). Data were recorded thirty to forty minutes after cooling.
water and steam flow rates were set and after the temperatures were steady for at least ten minutes. Temperature and voltage data were recorded via LabVIEW for three to five minutes and later averaged, while cooling water and steam condensate mass flow rates were measured with weigh tanks and stopwatches.

2.6 Data Reduction

For single-phase and two-phase flows, segment-averaged heat transfer coefficients were found using the expression

$$h_i = \frac{q_i^*}{(T_{F,i} - T_{W,i})}$$

Wall temperatures were measured in the coupon by thermocouples installed 1 mm below the channel. The heat transfer rate in each column was calculated assuming one-dimensional conduction (confirmed through numerical modeling of the copper block),

$$Q_i = -kWL_{seg,i} \frac{dT}{dy_i}$$

where $k$ was the conductivity of oxygen-free copper, $W$ was the width of the block, $L_{seg,i}$ was the length of the column segment, and $dT/dy_i$ was the temperature gradient in each measuring segment, with $i=1$ for the inlet segment, $i=2$ for the middle segment, and $i=3$ for the exit segment. The channel heat flux was

$$q_i^* = \frac{Q_i}{A_{ch,t}}$$

where $A_{ch,t}$ was the three-sided heat transfer surface area of the channel.
For single phase validation, the test section energy balance obtained using the copper heat flux sensors and the temperature gradient to calculate heat flux,

\[ q_g = q_1 + q_2 + q_3 \]

where \( q_g \) was the total heat transfer rate from the copper block through the gradient measurement method, including segment-averaged heat transfer rates \( q_1, q_2 \), and \( q_3 \); the first and third segment included the additional inlet and exit header areas, respectively. In single-phase validation, the total heat transfer rate from the copper block was compared to the enthalpy change of the cooled liquid water.

### 2.7 Uncertainties

A propagation of uncertainty analysis was conducted to estimate the uncertainty in condensation heat transfer coefficients [49], qualities, and other quantities.

The average quality across each measuring segment was obtained through a series of energy balances. Beginning with the pre-condenser, the steam cooling rate was determined from the cooling water energy balance, incorporating heat losses; validation experiments showed that the measured cooling water heat transfer rate underpredicted the steam-side heat transfer rate by an average of 2.9%. Cooling water and steam mass flow rates were obtained using a weigh tank and stopwatch, so the uncertainty in both mass flow rates depended on measured mass, \( m \), and time, \( t \), and was incorporated into the uncertainty analysis; the uncertainty in mass measurement was assumed to be ±1 g, larger than the accuracy of the scale (Citizen CT-8000H), and the uncertainty in time measurements was assumed to be ±1 s. Uncertainties in subsequent energy
balances were calculated, yet uncertainties in average test section qualities were low, of the range ± 0.01 to 0.03.

Uncertainties in condensation heat transfer coefficients were found using a propagation of uncertainty analysis [49] and are detailed in Derby [46]. The uncertainty of the thermal conductivity, wall temperature, and thermocouple location were ± 8 W/mK, ± 0.2 °C, and ± 0.13 mm, respectively. Fluid saturation temperature was determined by accurately measuring saturation pressure; an absolute pressure transducer at the test section inlet (range 0 to 690 kPa, uncertainty ±1.725 kPa) measured inlet pressure, combined with a differential pressure transducer (range of 0 to 69 kPa, uncertainty ±0.172 kPa) resulted in two-phase fluid temperatures with uncertainties of ± 0.2 °C. All pressure transducers were calibrated with a deadweight tester and mounted on pigtails. The uncertainties from measured areas were negligible. The uncertainty of the temperature gradient was obtained with the method of Kedzierski and Worthington [48],

$$w_2 = \sqrt{\frac{w_{T_i}^2}{\sum \left( \frac{y_i - \bar{y}}{G_e} \right)^2} \left( \frac{1}{\sum y_i (y_i - \bar{y})^2} \right)}$$

where $w_{T_i}$ was the temperature sensor uncertainty of ± 0.2 °C, $y_i$ was the position of the $i$th thermocouple, and $\bar{y}$ was the average position of the thermocouples. For single-phase cases, the heat flux uncertainty was dominant. For two-phase flow, especially the Teflon coated surfaces, low fluid-wall temperature differences were the largest contributor to condensation heat transfer coefficient uncertainty. Temperature measurements were critical for accurate condensation heat transfer and quality measurement. For this reason, all type T thermocouple probes were calibrated carefully using a LabVIEW calibration wizard over a wide range of temperatures,
including ice point, 10 °C to 80 °C in increments of 5 °C, and boiling point. Measured temperatures were compared to a reference thermometer with an accuracy of ±0.05 °C.

3. Results and Discussion

3.1 Single-phase validation

Single-phase experiments, conducted to validate the experimental apparatus for subsequent condensation results, compared test section energy balances from the gradient method to overall fluid energy balances, and evaluated Nusselt numbers for known, laminar flow conditions. Subcooled liquid entered the test section and was further cooled. The decrease in sensible heat on the fluid side was compared to the total heat transfer rate measured through using Fourier’s Law. Good agreement, with differences of less than 10%, was found between the two energy balances (Fig. 10), yielding confidence in the test section heat flux measurement method.

Because the length of the first measuring segment was 33 mm, values in the second measuring segment were fully developed. The reported data were for the second measuring segment, as exit and entrance effects, from impinging flow due to the angled inlet and exit, affected the heat transfer coefficients in the first and third measuring segments (but not the energy balances).

Laminar Nusselt numbers were measured with respect to Reynolds number and were compared to laminar flow between parallel plates, as the mini-gap offered a high aspect ratio (width/height=17 (Fig. 11). Additionally, the cover plate was not actively cooled and well insulated from the environment, similar to the case of parallel plates with one side insulated ($Nu=4.86$ [50]). Excellent agreement was achieved between the measured and predicted Nusselt numbers for laminar flow. Combined with the good agreement in overall energy balance, these
single-phase validation tests demonstrated that heat transfer coefficients could be accurately measured for condensation heat transfer.

3.2 Condensation data

Condensation studies examined the effects of mass flux, quality, and surface characteristics on flow condensation heat transfer behavior in a single channel, without flow instabilities associated with parallel channels. Condensation heat transfer coefficient data were reported from the second measuring segment, which, unlike the first and third measuring segments, was not affected by inlet and exit effects.

3.2.1 Hydrophilic copper mini-gap

Condensation heat transfer coefficients were observed to be a strong function of quality and lesser function of mass flux in the hydrophilic mini-gap, commensurate with the findings in the literature [3, 4, 17, 27, 51]. Condensation heat transfer coefficients were measured with uncertainties ranging from ±5% to ±29%, over a mass flux range of 50 to 200 kg/m²s and a wide range of qualities. Measuring segment quality changes were typically less than 5%, except at the lowest mass flux of 50 kg/m²s when quality changes of 12% were observed; uncertainties in average quality were very low, typically ±0.01 to ±0.03.

Higher heat transfer coefficients were observed at high qualities in the copper mini-gap (Fig. 12); less liquid at high qualities yielded a thinner liquid film, and consequently higher heat transfer coefficients, which varied by as much as a factor of three based on quality alone. Additionally, there was also an observable increase in heat transfer coefficients with respect to mass flux at higher qualities, especially apparent at mass fluxes of 100 and 150 kg/m²s, for
which the tested range of quality was largest. A dependence on mass flux was expected and observed, since the heat transfer coefficient typically scales with increasing velocity. Zhang et al. [19] studied laminar steam condensation between parallel plates (gaps spacing = 3 mm) using FLUENT, and observed shear thinning of the liquid film at higher vapor velocities. The mass flux dependence observed in the copper mini-gap agreed with the findings in the literature [3, 4, 17, 18], demonstrating that higher shear forces found at higher mass fluxes served to thin the liquid film, thus increasing the heat transfer coefficient.

3.2.2 Comparison with Correlations

Condensation data from the copper mini-gap was compared to correlations by Shah [52] and Kim et al. [53] (Fig. 13). The Shah [52] correlation utilized a database containing 22 working fluids, pipe diameters ranging from 2 mm to 49 mm, mass fluxes of 4 to 820 kg/m²s, and was based on the author’s previous boiling correlation. Mean average error was used to assess correlations, where MAE was defined as

\[
MAE = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{h_{\text{pred}} - h_{\text{exp}}}{h_{\text{exp}}} \right|
\]

where \( h_{\text{pred}} \) was the heat transfer coefficient predicted by the correlation, \( h_{\text{exp}} \) was the experimentally determined heat transfer coefficient, and \( n \) was the number of data points in a given set. This macro-scale correlation under-predicted the mini-gap data, with a mean average error (MAE) of 27.8% Kim et al. [53] developed a two-phase multiplier correlation for mini- and micro-scale condensation, including seventeen working fluids, hydraulic diameters of 0.424-mm to 6.22-mm, and mass fluxes of 53 to 1403 kg/m²s. The correlation utilized the modified Weber number criteria, developed by Soliman [54], to determine whether the flow was annular or slug-bubbly; the majority of the present data were within the annular flow regime, and just
one out of 26 data points were in the slug-bubbly flow regime. There was excellent agreement between the measured data and predicted values from the Kim et al. [53] correlation, with a MAE of 8.9% and without a significant bias, despite the absence of steam from the data set used to develop the correlation. Comparisons with the Shah [52] and Kim et al. [53] correlations demonstrated that the measured condensation heat transfer values were reasonable, and, based on the resulted obtained in this study, the Kim et al. [53] correlation is recommended for future predictions of steam in mini-channels

3.2.3 Comparison with Teflon-coated surface

Condensation behavior on a Teflon-coated surface differed from the plain copper surface in several notable ways: the heat transfer coefficients were substantially higher, generally in the 300,000 to 400,000 W/m²K range, and there was no discernible dependence on mass flux or quality (Fig. 14). While heat transfer in the copper mini-gap was very sensitive to quality, the Teflon mini-gap appeared insensitive to quality, which suggested that the condensing liquid was forming droplets as in dropwise condensation, instead of a liquid film that would act as a barrier to condensation; combined with the order of magnitude increase in heat transfer coefficient as compared to the hydrophilic copper mini-gap, the data strongly suggested that dropwise condensation occurred on the Teflon-coated surface. It should be noted that there was a clear difference between the performance of the copper and Teflon mini-gaps, although firm conclusions about the effects of quality on the Teflon surface were difficult to draw due to the uncertainties in heat transfer coefficients; higher condensation heat transfer coefficient uncertainties were a consequence of low fluid-wall temperature differences (< 1.0 °C).

3.2.4 Comparison with hydrophobic/hydrophilic patterned surfaces
Condensation heat transfer coefficients were measured for a range of mass fluxes and qualities in each of the hydrophobic/hydrophilic patterns and compared to condensation results for the hydrophilic copper and hydrophobic Teflon-coated surfaces (Fig. 15). Heat transfer coefficients from the Teflon and all patterned mini-gaps exceeded those found in the copper mini-gap and did not exhibit a strong dependence on quality, unlike the dependence observed with the plain copper surface. The uncertainties for these condensation heat transfer measurements were high as a result of low fluid-wall temperature differences, so differences in heat transfer coefficients between patterned surfaces were on the order of the uncertainties.

With some reservations due to the uncertainties, it appeared that the patterns with the lowest ($N=1$) and highest ($N=7$) number of hydrophilic areas yielded the best heat transfer performance. Three of the patterns ($N=2$, 3, 7) had comparable percent hydrophilic area coverage (Table 1), and, yet, the results indicated, but did not conclude, that the performance of the $N=7$ surface was superior. All of these patterns had hydrophilic areas in the corners of the mini-gap, but different widths: 1.10 mm for $N=2$, 0.91 mm for $N=3$, and 0.43 mm for $N=7$. One hypothesis on this difference in condensation heat transfer coefficient behavior is that the surfaces with the larger hydrophilic areas in the corners ($N=2$, 3) formed growing liquid films in the corners due to surface tension, covering some Teflon coated areas and reducing overall heat transfer rates. Another difference between the surfaces was the lack of branched “on-ramps” in the $N=7$ case (Fig. 6), which could have influenced the condensation heat transfer physics. The results indicated, however, that the condensation phenomenon is not merely a function of hydrophilic area coverage, and there were other factors influencing the condensation process.

To facilitate and quantify the heat transfer enhancement of the patterned and Teflon surfaces, the Teflon and patterned mini-gap data were compared to the copper mini-gap baseline data (Fig. 16). However, since it was shown that quality was the strongest variable governing
condensation for the copper mini-gap, the data were normalized to account for this effect. Simple equations were curve fit to relate heat transfer coefficients and average qualities for each mass flux in the copper mini-gap. For each surface, every data point was compared to the predicted value of the copper surface from the appropriate curve fit, yielding an enhancement factor of \( \frac{h_{\text{measured}}}{h_{\text{predicted,Cu}}} \) (Fig. 16). As expected, the copper enhancement factors ranged from 0.95 to 1.02, and centered around 1, which indicated the goodness of the predicted baseline values from the curve fits. The Teflon and patterned surfaces enhanced condensation heat transfer for all cases, and the results indicated that performance improved at decreasing quality; at qualities above 0.5, typical heat transfer enhancements ranged from 3 to 6. Previous modeling (section 3) suggested that the maximum heat transfer enhancement would be found at lower qualities, and experimentally, enhancements of 4 to 13 were seen at qualities below 0.5. The large condensation heat transfer coefficients observed with the Teflon and patterned mini-gaps further supported the hypothesis that dropwise condensation occurred on these surfaces, mirroring the enhancements found in the literature that dropwise condensation offered enhancements of 5 to 20 that of filmwise condensation [5-13].

In contrast to gravity driven external flows, this study examined the effects of hydrophobic and hydrophilic patterns in internal flow where shear forces mattered. Pattern performance would have been superior to that of a fully Teflon coated surface if thick, liquid films accumulated on the entire Teflon surface, but those liquid films could gather on the hydrophilic areas in the hydrophobic/hydrophilic surfaces. Droplet sweeping via shear forces may be affecting the condensation process, hindering liquid film development on the Teflon coated surface. An analytical [40] and experimental study [41] demonstrated the benefit of droplet sweeping in condensation. The presence of droplets, and the absence of a constant liquid film on the condensing surface, is required in order for droplet sweeping to be an important
condensing mechanism. Droplet formation, and thus droplet formation, would play a more significant role at higher void fractions were the liquid volume was small relative to the vapor volume, as liquid would not flood or fill the channel. Consequently, void fraction was estimated for the quality range tested using the homogeneous equilibrium model [5] and Lockhart Martinelli model [2]. The formulation of the homogeneous equilibrium model assumed equal liquid and vapor velocities in order to determine the void fraction. Alternatively, using an approach developed by Lockhart and Martinelli [2], Butterworth [43] developed a simple correlation for void fraction, Equation 3, which did not assume equal liquid and vapor velocities, where the Lockhart Martinelli parameter, $X$, was selected for viscous liquid-viscous gas and viscous liquid-turbulent gas flows at mass fluxes of 50 and 200 kg/m$^2$s, respectively.

Using these models, void fraction was estimated for the lowest and highest mass fluxes tested (Fig. 17). Since the density of liquid water is three orders of magnitude higher than that of water vapor, void fraction remained high even as quality decreased for all mass fluxes. For all cases, void fraction was above 0.8 for qualities above 0.1, and declined rapidly as quality approached zero. Condensation heat transfer coefficients were measured experimentally from qualities nearing 1 to qualities of around 0.15, and the heat transfer coefficients on Teflon/patterned surfaces did not vary with quality. Over this quality range, the void fraction was high, signifying that the majority of the channel cross sectional area was occupied by vapor, not liquid, and thus it was reasonable to assume that droplet sweeping was occurring.

4. Conclusions

Flow condensation of steam was studied inside a mini-gap, including the effects of hydrophobicity on promoting dropwise condensation; a hydrophilic copper 1.06-diameter mini-
gap was compared to a hydrophobic Teflon coated mini-gap and patterned hydrophobic/hydrophilic mini-gaps were explored over a range of mass fluxes and qualities.

Condensation heat transfer coefficients were measured accurately in a hydrophilic copper mini-gap, 9.6 mm by 0.56 mm, with uncertainties between 5% and 15% at qualities below 0.5, and around 15-25% at higher qualities. It was found that the condensing heat transfer coefficient was a strong function of quality, which signified that a liquid film developed on the condensing surface as vapor was condensed. The heat transfer coefficient was a lesser function of mass flux, especially at high qualities, which denoted the effects of shear forces to thin the liquid film. The micro- and mini-scale Kim et al. [53] correlation predicted the data very well, with a mean average error of 8.9%.

Dropwise condensation of steam was promoted on hydrophobic Teflon AF™ coated copper surfaces. Extremely high condensation heat transfer coefficients were observed, ranging from 280,000 to 425,000W/m²K; higher uncertainties in these measurements were a result of low wall-fluid temperature differences (<1 °C). There was no discernible dependence on quality or mass flux, which suggested that a liquid film was not developing on the Teflon surface, since condensation heat transfer coefficients remained high even at qualities below 0.5. Heat transfer enhancements of 3.2 to 13.4 times that of the copper mini-gap were commensurate with the behavior of dropwise condensation.

Patterned geometries were selected for testing using a simple analytical model, with a range of hydrophilic strips (N=1,2,3,7). The data suggested, but did not conclude, that the best pattern performance was exhibited by two patterns with N=1 and 7, yet the patterned surfaces did not perform as well as the Teflon coated surface. It was posited that the shear forces that led to droplet sweeping and removal were more significant than liquid film development at these tested
mass fluxes. The Teflon coated mini-gap offered the most condensation heat transfer enhancement.

Several areas of future study emerged from this work. First, further understandings of the flow condensation mechanisms are needed, especially relating to the formation of droplets on a hydrophobic surface in shear driven flow. It was hypothesized that the effects of droplet sweeping from shear forces were the dominant means of heat transfer enhancement in any Teflon coated surface. This hypothesis should be analyzed further, analytically and experimentally, and the flow visualized at lower mass fluxes, where the effects of shear lessen and those of surface tension increase. In addition, future experiments could reduce condensing heat transfer coefficient uncertainties.

Acknowledgments

The authors acknowledge the financial support of Office of Naval Research through a MURI grant, Grant No. N00014-07-1-0723 entitled "System-Level Approach for Multi-Phase, Nanotechnology-Enhanced Cooling of High-Power Microelectronic Systems," and a graduate fellowship from the NSF GK12 program, “Building Bridges from High School to Grad School Through Discovery-Based Activities in Energy and the Environment.”
**Nomenclature**

\[ A \] Area \([\text{m}^2]\)

\[ d \] Gap depth, \([\text{m}]\)

\[ D \] Diameter, \([\text{m}]\)

\[ G \] Mass flux, \([\text{kg/m}^2\text{s}]\)

\[ h \] Heat transfer coefficient, \([\text{W/m}^2\text{K}]\)

\[ k \] Thermal conductivity \([\text{W/mK}]\)

\[ L \] Length, \([\text{m}]\)

\[ \dot{m} \] Mass flow rate, \([\text{kg/s}]\)

\[ MAE \] Mean average error

\[ n \] Number of samples

\[ N \] Number of hydrophilic areas in patterned surfaces

\[ q'' \] Heat flux, \([\text{W/m}^2]\)

\[ Q \] Heat transfer rate, \([\text{W}]\)

\[ t \] Time, \([\text{s}]\)

\[ T \] Temperature, \([\text{°C}]\)

\[ w \] Uncertainty

\[ W \] Width, \([\text{m}]\)
$x$ Quality

$X$ Lockhart Martinelli parameter

$y$ Transverse coordinate, [m]

$\alpha$ Void fraction

$\beta$ Contact angle

$\mu$ Viscosity, [kg/ms]

$\rho$ Density, [kg/m$^3$]

**Subscripts**

$1,2,3$ Corresponding to first, second, third measuring segment

$ch$ Channel

$DWC$ Dropwise condensation

$exp$ Experimental

$f$ Fluid

$FWC$ Filmwise condensation

$g$ Gradient

$i$ Index

$l$ Liquid

$LM$ Lockhart Martinelli

$pred$ Predicted

$seg$ Segment

$tot$ Total

$v$ Vapor

$vv$ Viscous liquid and vapor

$vtt$ Viscous liquid and turbulent vapor

$w$ Wall
References


[18] S. Chowdhury, E. Al-Hajri, S. Dessiatoun, A. Shooshtari, M. Ohadi, An experimental study of condensation heat transfer and pressure drop in a single high aspect ratio micro-channel for


**Figure Captions**

Fig. 1: Basic minigap geometry

Fig. 2: Dependence of heat transfer coefficients on number of hydrophilic areas for specified qualities

Fig. 3: SEM micrograph used for measurement of Teflon AF™ coating thickness

Fig. 4 Goniometer images of heat transfer surfaces a) hydrophilic copper surface and b) hydrophobic Teflon AF™ coated surface

Fig. 5: Schematic detailing hydrophobic/hydrophilic patterned surfaces

Fig. 6: Completed hydrophobic/hydrophilic patterned Teflon/copper surfaces

Fig. 7: Test section design

Fig. 8: Detailed test section geometry

Fig. 9: Open loop steam experimental apparatus

Fig. 10: Single-phase comparison of gradient and fluid test section heat transfer rates

Fig. 11: Validation tests using single-phase Nusselt numbers

Fig. 12: Condensation heat transfer coefficients versus average quality for the copper mini-gap

Fig. 13: Comparison of measured copper mini-gap data to predictions with macro-scale Shah [52] and mini-scale Kim et al. [53] correlations

Fig. 14: Comparison of data from Teflon and copper surfaces

Fig. 15: Comparison of all surfaces at mass flux G=150 kg/m²s

Fig. 16 Condensation heat transfer coefficients on hydrophobic/hydrophilic surfaces as compared to copper hydrophilic surface

Fig. 17: Void fraction estimation using Lockhart Martinelli [2] and Homogeneous equilibrium models [5] for mass fluxes of 50 and 200 kg/m²s
Figures

**Fig. 1:** Basic minigap geometry

**Fig. 2:** Dependence of heat transfer coefficients on number of hydrophilic areas for specified qualities
Fig. 3: SEM micrograph used for measurement of Teflon AF™ coating thickness

Fig. 4 Goniometer images of heat transfer surfaces a) hydrophilic copper surface and b) hydrophobic Teflon AF™ coated surface
Fig. 5: Schematic detailing hydrophobic/hydrophilic patterned surfaces

Fig. 6: Completed hydrophobic/hydrophilic patterned Teflon/copper surfaces
Fig. 7: Test section design

Fig. 8: Detailed test section geometry

Fig. 9: Open loop steam experimental apparatus
Fig. 10: Single-phase comparison of gradient and fluid test section heat transfer rates
Fig. 11: Validation tests using single-phase Nusselt numbers
Fig. 12: Condensation heat transfer coefficients versus average quality for the copper mini-gap
Fig. 13: Comparison of measured copper mini-gap data to predictions with macro-scale Shah [52] and mini-scale Kim et al. [53] correlations
Fig. 14: Comparison of data from Teflon and copper surfaces

Fig. 15: Comparison of all surfaces at mass flux $G=150 \text{ kg/m}^2\text{s}$
Fig. 16 Condensation heat transfer coefficients on hydrophobic/hydrophilic surfaces as compared to copper hydrophilic surface
Fig. 17: Void fraction estimation using Lockhart Martinelli [2] and Homogeneous equilibrium models [5] for mass fluxes of 50 and 200 kg/m²s
List of Tables

Table 1: Percent hydrophilic area for different surfaces

<table>
<thead>
<tr>
<th>Surface</th>
<th>Hydrophilic area</th>
</tr>
</thead>
<tbody>
<tr>
<td>Copper, N=0</td>
<td>100%</td>
</tr>
<tr>
<td>N=7</td>
<td>33%</td>
</tr>
<tr>
<td>N=3</td>
<td>33%</td>
</tr>
<tr>
<td>N=2</td>
<td>31%</td>
</tr>
<tr>
<td>N=1</td>
<td>13%</td>
</tr>
<tr>
<td>Teflon, N→∞</td>
<td>0%</td>
</tr>
</tbody>
</table>