

DEVELOPMENT OF A PROCEDURE TO DETERMINE INTERNAL STRESSES IN
CONCRETE BRIDGE MEMBERS

by

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Abstract

With aging and deterioration of bridges, evaluation of existing conditions of their structural elements becomes vital to engineers and public officials when deciding how to repair or replace the structures. The ability to obtain necessary information on these conditions is often expensive and time consuming, especially for concrete bridges where the reinforcement is not available for inspection. Employing the surface-strain relief method could allow for accurate evaluation of aged or damaged prestressed members.

The surface-strain relief method was developed to measure initial or pre-existing strains in a concrete member. It involves relieving the strain in the member and measuring the change in strain. Two methods were tested—one used a linear electrical-resistance strain gage and a three-inch-diameter diamond concrete core bit to cut around the gage, and the second method used a laser-speckle imaging device and a diamond cutting wheel to create notches perpendicular to the axis of maximum strain. Both methods measured the change in strain and related it to within 10 percent of the actual f_{se} . The method of cutting notches and the laser-speckle imaging device provided a simpler method to be implemented in the field, while the coring method achieved a higher level of accuracy and precision.

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Chapter 1 - Introduction

In North America, many prestressed concrete bridges have been built over the past five decades. Several of these bridges, including rural bridges on county roads, are approaching the end of their design life, or have been subjected to larger loads and heavier traffic demands, making them deficient and in need of repair. To preserve the structural integrity of the bridges and safety of the public, inspections need to be conducted. With prestressed members, visible inspections may not be sufficient to determine the condition of the structure due to environmental and time-dependent losses of the prestressing force. Therefore, engineers need a reliable method to determine the remaining prestress force in a member during routine inspections and rehabilitation, or when retrofitting the structure.

Current evaluation methods involve visual inspections and or instrumenting the structure with strain gages, applying a known load to the structure, and measuring the change in strain due to the applied load. The load is then varied and models are created from the gathered data, then strains in members can be extrapolated from the models. While these methods are accurate, they only capture strains induced by an applied load and not initial or residual stresses in the members. Two methods exist to determine the remaining prestress force in a member and each is semi-destructive and difficult to conduct in an existing structure. The first method involves applying a load to generate flexural cracks; instrumenting the cracks with displacement transducers, strain gages, or similar devices; loading the structure once more; and determining the moment needed to open the crack to produce zero concrete tension at the instrumented crack. The second method involves removing concrete from around the tendon, and cutting a wire and measuring the deflection of the wire after cutting it. This deflection can be related to the stress in the wire and assumes that all wires have similar stress. Each of these methods is semi-destructive and is conducted in laboratory settings, and would be difficult to employ in an existing structure.

With aging infrastructure, it becomes more important to calculate or measure the remaining prestress force in existing structures. Knowing the average prestress force in a member could allow analysis to be conducted to determine the stress in the prestress reinforcement at a more accurate strength of the member and more importantly, to calculate the

stress range of the member due to fatigue. The average prestress force provides valuable information when monitoring strength and durability of older or damaged structures. Bridge owners can make informed decisions about how to allocate maintenance funds and reduce the inherent risk associated with deteriorating infrastructure with this information.

Often times when trying to calculate the remaining prestress force, for older structures, limited information exists on actual design and/or construction and environmental conditions. Thus assumptions such as initial jacking force, ect., have to be made affecting the accuracy of the analysis. Insignificant initial flaws in the members can go unnoticed but due to time-dependent losses, over time these can become critical to the strength of the member. Prestress force is a time-dependent phenomena influenced by factors such as elastic shortening due to transfer, shrinkage, creep, and relaxation that occurs after transfer. These losses are calculated based on geometric and mix properties of the member, along with environmental conditions. Based on research, equations have been developed to enable the calculation of losses over time. These equations are not exact and are only estimates, and have been developed to provide estimates for many types of prestressed members.

With these factors in mind, a method of surface-strain relief was developed to accurately measure the remaining prestress force through relief of residual stresses, while being mostly non-destructive. The method allows bridge members to be checked over time to ensure they are still meeting the design assumptions. Calculation of the losses is only an estimate, so the surface-strain relief method could lengthen the life of a structure by providing a level of confidence that the structure can still perform as designed. The surface-strain relief method provides a cost-effective means to evaluate the condition of the structure, and places a higher level of certainty on decisions by owners and engineers in regard to the condition of the structure.

The surface-strain method was developed and tested on post-tensioned concrete members and compared to theoretical calculations and finite-element models (Peterman and Hammerschmidt 2010). The next phase, Phase II, focused on implementation in a laboratory setting, the method of surface-strain relief by dry-coring on prestressed concrete members, and determining the accuracy of the method. The prestress members had multiple strands with varying force, geometry, and production dates. Results of the surface-strain relief method were compared to the prestress force in the member, which had been found through the crack-opening

procedure. Effectiveness of the method was evaluated using prestress members with multiple-bonded strands.

Chapter 2 - Literature Review

Multiple methods similar to surface-strain relief, as proposed for this project, were researched to find limitations and difficulties encountered with each. Destructive and semi-destructive methods were researched to use as a basis of comparison and to accurately determine the average prestress force in each member.

2.1 Similar Methods to the Surface-Strain Relief Method

Many methods have been proposed to measure residual stresses on the surface of steel and concrete specimens. The standard to measure residual stresses in steel is found in ASTM E837. Measurement of residual stresses in concrete members have been researched by the Federal Aviation Administration's National Airport Pavement Test Facility (NAPTF) (Guo et al. 2008) and by David G. Marks at the University of Illinois at Urbana-Champaign by modifying the ASTM E837 hole-drilling method to be applicable for concrete members (Marks 2009). Others like Kesavan, Ravisankar, Parivallal, and Sreeshylam have created a method to measure the relaxation around a core or to core around the gage, theoretically relieving all the stress in the concrete (2005).

2.1.1 ASTM E837 Standard Test Method for Determining Residual Stresses by the Hole-Drilling Method

According to Vishay Micro-Measurements, residual stresses are developed from virtually all manufacturing processes, repairs, or modifications (2007). To quantify these residual stresses, ASTM E837 "*Standard Test Method for Determining Residual Stresses by the Hole-Drilling Method*" was developed to measure residual stresses in the critical residual stress region. The material must be isotropic linear-elastic with residual stresses not exceeding 60 percent of the material yield stress, can vary in thickness, and can have non-uniform stress (ASTM E837 2009). The stresses are measured near the surface of the material by mounting a rosette strain gage and drilling a small hole (2 mm in diameter) at the center of it. Residual stresses in the material surrounding the hole are partially relieved, and the associated relieved strains are measured at varying depths while drilling and recording the changes using a suitable strain-recording instrument (ASTM E837 2009). Based on the linear elasticity theory and finite-

element models, the residual stresses can be calculated from the difference in strain measurements and calibration constants found through finite-element models. Accuracy of the method depends on the operator skill and expertise with a precision of $\pm 10\%$, providing the stresses are uniform throughout the depth of the hole, as much larger errors result when non-uniform stresses are present.

2.1.2 National Airport Pavement Test Facility Core-Ring Strain Gage Test Procedure

NAPTF developed a procedure called the core-ring strain gage test, using ASTM E837 as a basis. The initial objective was to directly measure residual stresses in concrete beams and then to develop a procedure to measure residual stresses in concrete airport pavements. To complete these objectives, tests were conducted to determine the optimum core-ring size and depth, and the spacing between the strain gage center and the core-ring edge. The core-ring strain gage procedure used a single linear-resistance strain gage aligned along the axis of maximum strain. A core was then drilled at the end of the gage and the relaxation in strain was measured between the initial strain and the strain measurement after the coring was complete. Multiple tests were conducted to determine the size of strain gage, core-ring size, and depth of the core.

NAPTF used both finite-element analysis and experimental testing to develop the core-ring strain gage procedure. Experimental tests were conducted using six-by-six-inch beams, four feet long. Through loading the specimens and monitoring the strain, it was found that if each beam was rotated 90 degrees, the modulus of elasticity was uniform throughout the depth of the specimen when positioned in this direction. One end of the beam was fixed and the other end was loaded three inches from the end of the beam using a jack to the specified load of 400 lbs. Then the beam was cored adjacent to the strain gage (see figure 2.1), varying the depth and recording the change in strain at each depth. NAPTF concluded that strain gages with a gage length of 1.2 or 0.8 inches worked with a maximum aggregate size of one inch. Three- or-four inch core rings provided acceptable results with a one-inch core depth. Spacing between the strain gage and the core-ring edge should be 1 to 2.75 inches (Guo et al. 2008). Finite-element models were created and compared closely to the experimental results. The finite-element models showed larger strain changes when the core was on the fixed end rather than the end

where load was applied. Therefore, the core ring should be drilled between the gage and the fixed end.

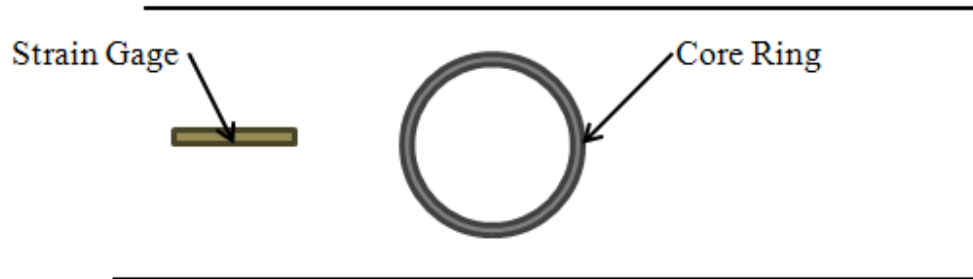


Figure 2.1 NAPTF Method

David G. Marks, from the University of Illinois at Urbana-Champaign, measured residual stresses in concrete pavements by either coring adjacent to a strain gage or sawing notches at each end of the strain gage. The project branched from the strain-relaxation technique developed by NAPTF. Both experimental tests and finite-element models were conducted to compare the results of core rings and saw notches.

Beams six by six inches and 40 inches long were cast, using a mix design from the Illinois Department of Transportation. Based on the findings of NAPTF, the beams were rotated 90 degrees for testing, making the side from casting the top side of the beam for testing. This was done to have a smooth surface for mounting strain gages and a more uniform stiffness in the beam, according to NAPTF. Both 20- and 30-mm strain gages were used, as suggested by NAPTF results, and these were positioned 13 inches from the fixed support. The procedure used a three-inch-diameter core with water to cool the core bit and reduce the effects of temperature on the strain readings. Using an NDT James Instruments, Inc. Kwikcore, the core bit was advanced in 0.25-inch increments to a total depth of 1.25 inches. During the coring process, the research team recorded strain measurements continuously and noticed a large change in strain appeared initially and generally stabilized after approximately 10 minutes. The increase in the strain measurements was due to a temperature increase caused by a difference in the water and environmental temperatures. To correct this error, water at the same temperature of the beam was used and produced the least amount of strain drift.

A second method was developed which implemented a diamond saw blade and cut a notch adjacent to the strain gage (see figure 2.2). A single notch adjacent to the strain gage on the fixed end of the test specimen, and two notches, one on each side of the strain gage, were tested. Notching provided a quicker method and eliminated issues with the cooling water affects. The testing procedure was the same, but instead of the core rings a circular saw fitted with a seven-inch masonry saw blade was used. Notches were cut in three passes starting with a depth of 0.5 inches, then to one inch, and to a final depth of 1.5 inches at a distance of 1.63 inches from the center of the gage. It was found that when sawing notches on each side of the strain gage, all the stresses were relieved. With both notches cut to a depth of one inch, the strain gage did not respond noticeably to the applied load, and the gage corresponded to the initial residual stresses in the beam (Marks 2009).

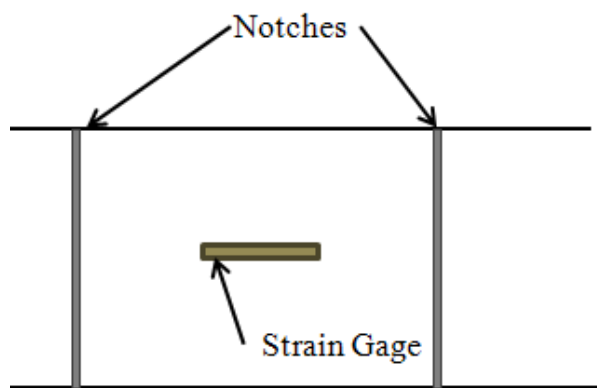


Figure 2.2 Notches Cut Next to Strain Gage

Marks used finite-element models to compare core-ring configurations and single- and double-notch configurations to the experimental results. Each model created a similar six-by-six-inch beam, cantilevered to induce stresses in it. Linear-strain triangle elements and linear-strain quadrilateral elements were used on the models, with a finer mesh around the notches and a less-fine mesh elsewhere to reduce the computationally run time. Use of core rings to a depth of one inch provided the same stress relief as a circular hole, similar to the ASTM E837 procedure. From the finite-element models, a coring ring of three inches at a depth of one inch was sufficient to relieve the stresses, full strain relief could be achieved with two notches, and a near-zero surface stress was found when the notches were at a depth of one inch (Marks 2009).

From the experimental and finite-element results, the saw notches provided a full strain relief and did not need additional calibration constants, and the residual stresses could be calculated using basic equations. Through finite-element modeling, full relaxation occurs when notch depths are 40% of the distance between the notches (Marks 2009).

2.1.3 Factors Affecting the Hole-Drilling Method

McGinnis (2006) researched three factors that affect the core-drilling method—water-induced swelling, proximity of steel reinforcement, and differential shrinkage. The core-drilling method is similar to the ASTM E837 procedure but instead of measuring strains, this method measures displacements around the core hole caused by relaxation of the core and relates them to the residual stresses in the structure.

The core-drilling process uses three points of known location outside of the core to measure the relieved displacements around the core hole. The relieved displacements are measured using the digital-image correlation system and calculate radial- and tangential-relieved displacements of the overall displacement with respect to the center of the core hole. Through a series of calculations, these displacements are related to in-situ stresses. The digital-image correlation system images an applied patterned surface to the concrete and then photographs the object with a pair of digital cameras before and after loading. Using photogrammetric triangulation principles, the sets of photos are compared and the displacements are calculated. The field of view is approximately 250 mm wide and has a displacement resolution of eight microns for out-of-plane displacements and better for in-plane displacements (McGinnis 2006).

McGinnis recorded an average error of 28.4% when effects of water-induced swelling, proximity of steel reinforcement, and differential shrinkage effects were neglected. When considered and accounted for, an average error in the experiments was 9.5%. It was found that the presence of reinforcement nearer than 35 mm to the core hole and with a concrete cover of less than 75 mm causes significant under-prediction in the calculated in-situ stress using the core-drilling method (2006). Water-induced swelling and differential shrinkage created additional tensile stresses and are added to the actual stresses measured. Using ABAQUS, models with similar geometry and material properties were created with and without reinforcement and the results were compared. An error of approximately 20% was found and the in-situ stress values were adjusted to account for this. Corrections of the water effects are much more complex and

depend on absorption, time of water exposure, porosity, and swelling strain. These are discussed thoroughly in McGinnis dissertation (2006). Differential shrinkage errors were determined through use of finite-element models and data from environmental curing conditions. From this differential shrinkage, stress profiles were created and an estimated stress of 2.55 MPa was found due to differential shrinkage (McGinnis 2006). Correction factors must be developed from finite-element models to account for the additional displacements caused by reinforcement, water-induced swelling, and differential shrinkage, making this procedure dependent on geometric and material properties of the member.

2.1.4 Core Trepanning Method

Kesavan, Ravisankar, Parivallal, and Sreeshylam developed a procedure, the core trepanning method, to simplify calculations of residual stress, and made it applicable to prestressed concrete members currently in service (2005). They accomplished this by coring around a strain gage positioned along the axis of maximum stress providing a full strain relief. Their method is unlike other methods where strain gages are positioned around the outer core hole and the relief around the hole is measured. The core trepanning method places the strain gage in the middle of the core and measures the relief of the core, which results in a larger change in strain. With this method, special procedures were developed to waterproof the gage and create connections to disconnect the lead wires to the strain gages. Through experimental testing a 50-mm-diameter core hole, in combination with a 30-mm electrical resistance strain gage at a depth of 20 to 30 mm, allowed maximum strain release to occur.

Kesavan, Ravisankar, Parivallal, and Sreeshylam conducted multiple experiments using both pre-tensioned and axially loaded members to determine the size of strain gage and also the depth of the core. Electrical-resistance strain gages of 10-, 20-, and, 30-mm lengths were tested on concrete cubes with no applied load. Each gage was cored to a total depth of 50 mm (diameter of the core) in 10-mm increments, recording strain measurements at each increment. The 30-mm gage provided consistent readings in comparison to the other gages and was found to be within ± 10 microstrain. A second set of tests on axially loaded specimens was run to determine the actual depth needed to fully release the residual stresses. From coring in 10-mm increments, it was concluded that maximum released strains occurred between 20 and 30 mm, and that cutting any deeper was not required (2005).

To further test the method and repeatability on prestress concrete members, the core trepanning method was used on prestress members by coring around gage positions along the top and bottom sides of a beam. The measured strains were compared to the recorded strain during prestressing and revealed that 92% of the applied strain was released through the core trepanning method (Kesavan et al. 2005). The method was also conducted on a seven-year-old prestressed T-section that had an initial prestressing force of 360 kN. On the surface of the T-beam, three cores were taken—one on the top flange and two below the neural axis. With these three cores, residual stresses were calculated and the residual stress at the neutral axis was interpolated. Stress at the neutral axis was used to calculate the prestress force in the member, because at the neutral axis, all bending stresses due to prestress force and gravity load disappear, leaving only the axial compression prestress force. An average prestress force of 285.3 kN was calculated and found to be in good agreement when taking losses into consideration (Kesavan et al. 2005).

2.1.5 Summary of Similar Residual Stress Measurement Procedures

Looking at the previous research conducted, many methods have been tested and have shown the feasibility of creating a method to measure residual stresses in a prestressed member. Measuring strain relief around the outside of a hole in steel has provided accurate and repeatable results. For concrete, this method has also shown that it can be effective, but due to the many steps involved, complex calculations, and the small strains that are measured, larger error results make it difficult for implementation outside a laboratory setting. Marks, Kesavan, Ravisankar, Parivallal, and Sreeshylam have developed two acceptable methods by coring or cutting notches around a strain gage, which increases the level of strain relief and greatly simplifies the analysis procedure. Each method uses water to cool the diamond coring bit, which can possibility damage the strain gage, and introduce swelling in the concrete as McGinnis has found. These strains due to swelling can be significant, affecting overall accuracy of the method (2005).

2.2 Destructive and Semi-Destructive Methods to Determine Average Prestress Force

Experimental procedures have been developed to accurately determine average prestress force in a prestress member. One method applies a load and measures the crack width to determine the load required to first open the crack. This method has proved to be accurate in

determining the average prestress force (f_{se}). Many researchers have used these methods with variations to determine f_{se} in members of different geometries and ages. Larson, Peterman, and Rasheed used the procedure to determine f_{se} in T-beams only a few months old (2005); while Pessiki, Kaczinski, and Wescott tested prestressed I-beams that were removed from an obsolete bridge (1996). Another method used by Czaderski and Motavalli (2006) removed the concrete surrounding the prestress tendons and measured displacement of the wire as the wires were cut, and the deformation was related to the stress in the wire.

Larson, Peterman, and Rasheed determined f_{se} in T-beams before strengthening with carbon fiber reinforcement attached to the bottom of the beams. The researchers pre-cracked each section with four-point bending, applying an initial load greater than the calculated cracking moment so a visible crack could be seen, and location of the crack was marked before unloading the beam. Linear variable differential transducers (LVDTs) were then mounted spanning the base of the crack. The load was reapplied at the same load rate for an additional 25 cycles to determine an average cracking moment for the beam. When the crack was just opened, zero concrete tension resulted at the base of the beam, so the modulus of rupture was assumed to be zero for calculations of the prestress force. To determine the experimental load needed to just keep the crack closed and the concrete at zero tension, graphs of load versus deflection were created and the load was found at the point of end of linearity for cycles two through 10 (2005). Assuming tensile strength of the concrete as zero due to the pre-cracking, linear elastic analysis of the gross transformed section was used to calculate the average prestressing stress in the prestressing strands. Larson, Peterman and Rasheed found the experimental f_{se} in agreement with the calculated PCI losses (2005).

A similar method was conducted on two prestress I-beams taken out of the Shenango River Bridge on Interstate 80 in Mercer County, Pennsylvania. Pessiki, Kaczinski, and Wescott (1996) conducted experimental tests on two beams at Lehigh University. Each beam was loaded in three separate phases—phase I was to crack the beam, document the location of flexural cracks, and instrument the cracks with displacement transducers and strain gages. Next the beams were loaded to determine the decompression load, or cracking moment, based on displacement transducers and strain gage measurements. The final phase was to load the beam to failure. During the second phase, the beam was repeatedly loaded and unloaded in a quasistatic manner in order to determine the decompression load in the bottom of each beam. The

decompression load was determined by three methods—visible observation of the crack opening, measurement of the crack using LVDTs, and use of surface-mounted strain gages. Examining the load versus strain curves and the load versus crack width from the LVDTs and strain gages, a bilinear response was seen. The load versus strain curves showed a proportional increase in load compared to the strain in the first linear section of the bilinear curve. In the second linear portion, an increase in load was accompanied by no increase in strain. Once the crack was open strain was no longer transferred across the crack, therefore, no increase in strain. Linear lines were fitted to each linear segment and the point of intersection was determined to be the decompression load. The strain gage measurements were found to be repeatable and varied by no more than three to five percent (1996). The load versus crack width was analyzed in a similar manner, where the load versus crack width was plotted and typically showed an increased crack opening with an increasing load. The point when the rate of increasing load to crack opening changed was taken as the end of linearity and the decompression load. The decompression load found using the crack-width data was generally higher than the decompression load from the strain gages, and visual inspection resulted in the highest decompression load out of the three values. Pessiki, Kaczinski, and Wescott used the decompression load determined from the strain gages in the rest of its calculations due to their consistent and repeatable values (1996).

Czaderski and Motavalli (2006) investigated losses of a 38-year-old bridge being dismantled in southern Switzerland. Five I-beams were removed from the existing bridge, and each beam consisted of two prefabricated concrete I-beams connected using two post-tensioning tendons with a parallel wire bundle of 26 or 27 wires. The concrete was removed, exposing the tendons at five locations along the length of the beam. Once the tendon was visible, the duct and grouting material was removed, exposing the individual prestressing wires. Aluminum measurement points were glued on the wires with a spacing of eight inches. Several wires were instrumented, including removing some of the exterior wires to instrument the interior wires. Using a mechanical strain gage (deformeter), the initial strain measurement was recorded. The wires were cut, releasing the force in the wires, and the deformeter measured the change in displacement. Results from the 26 wires showed small deviations in the measured strains and also, when one wire was cut, strain increase in the other wires was minimal (Czaderski and Motavalli 2006). Calculated and measured tendon force was in good agreement and showed

cutting a few wires out of each tendon would be sufficient to determine the remaining post-tensioning force in the member.

Chapter 3 - Test Specimens

Prestressed beams of varying dimensions are used in bridges and structures, ideally the surface-strain relief method should be applicable to these various geometries. Steel reinforcement and the concrete mix designs will vary around the country due to state and local standards and availability of materials. To test the accuracy of the surface-strain relief method, two types of beams were used—T-beams' and rectangle beams' cross sections. A set of rectangle of beams designed and cast at Kansas State University (K-State) and a set of nine-year-old T-beams cast at a prestressed concrete plant were used. The beams were initially tested with the crack-opening procedure to determine f_{se} in each member, and then the surface-strain relief method was used to calculate f_{se} and compare it to the experimental determination of f_{se} . The beams were designed according to American Concrete Institute (ACI) and Precast Prestressed Concrete Institute (PCI) codes and standards. Four beams were cast at K-State with varying stress levels but similar concrete properties and dimensions. The beams cast at K-State were cast in the laboratory where many variables, including concrete mix, prestress force, and geometry of the member, could be controlled. Whereas the T-beams represented a member cast by a prestress plant and were approximately nine years old, this provided a member that had incurred losses over time due to environmental conditions.

3.1 Design and Casting of Rectangle Beams

Two sets of beams with rectangle cross sections were designed to simulate a beam to meet ACI and PCI code and standards. Each set was designed to contain two beams cast in series, enabling each beam to have identical prestress force. These beams were cast at K-State using a Kansas Department of Transportation (KDOT)-approved mix design. The purpose of these beams was to represent a control beam, limiting the amount of added reinforcement but still representing a beam with similar stress as a beam found in a structure. Since the beams were cast at K-State, multiple methods would be used to determine the prestress force in each beam and verify results of the surface-strain relief method.

Each beam had a cross section six inches wide by 12 inches tall and 120 inches long. Reinforcement in each beam consisted of two, ½-inch 270 kips per square inch (ksi) low-relaxation strand and two, ½-inch 50 ksi steel reinforcing bars. These were placed with two

inches of concrete cover surrounding the bar in accordance with ACI (ACI 318-08 2008) (see figure 3.1). To achieve strand stress that represented long-term losses in a member, each strand was initially stressed to approximately 160 ksi. No shear reinforcement was needed in the beam and added stiffness was introduced affecting the surface-strain relief method. Four, 3/8-inch steel stirrups were positioned throughout the beam, one at each end and at the third points to hold the top bars in place (see figure 3.2). The concrete mix design was a normal-weight mix designed for KDOT bridge girders. The mix used type III cement with 50% coarse aggregate and 50% fine aggregate by weight (see table 3.1 for mix proportions). The mix had a design 28-day strength of 6000 psi, a three-inch slump, and 5% air entrainment to meet KDOT specifications. A release strength of 4200 psi was needed before the beam could be de-tensioned.

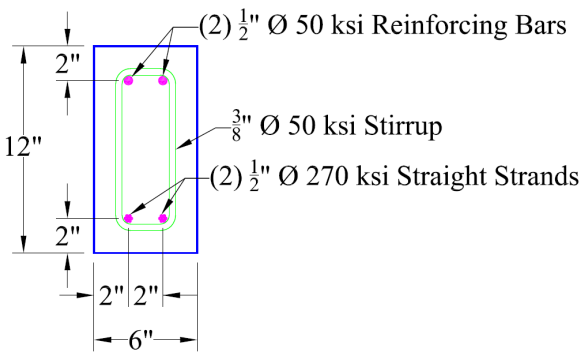


Figure 3.1 Cross Section of Rectangle Beam

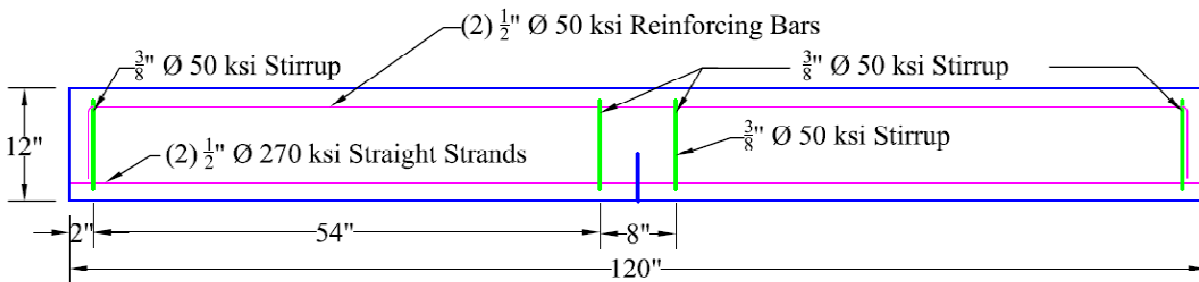
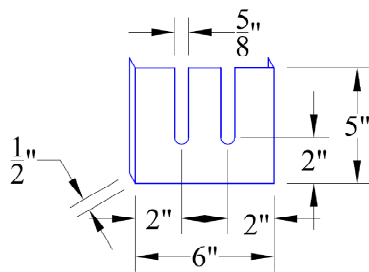


Figure 3.2 Longitudinal Section of Rectangle Beam

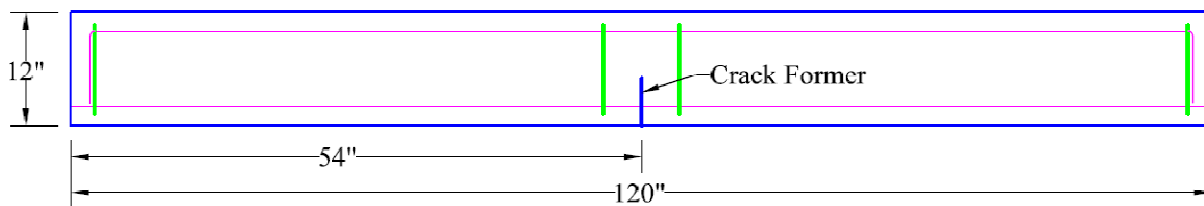
Table 3.1 Mix Proportions

Material	Design Quantity
Water	252 lb/yd ³
Cement	721 lb/yd ³
Large Aggregate	1442 lb/yd ³
Small Aggregate	1442 lb/yd ³
Daravair	21 mL/yd ³
AdvaFlow	450 mL/yd ³

At the midpoint of the beam, a crack former was embedded as shown in figure 3.3. The crack former was a 16-gauge stainless steel plate, five inches tall and six inches wide, with a ½-inch bend on each side to temporarily attach it to the form. One side was covered with duct tape to prevent the concrete from bonding to the steel. The crack former initiated and controlled the location of the crack for use with the crack-opening procedure to determine the prestress force in the beam. The crack former also allowed for the assumption that no concrete tensile stress could be transferred across the crack. Therefore, the modulus of rupture of the concrete could be assumed as zero at the midpoint. This would greatly simplify the calculation of the prestress force and reduce the amount of error and uncertainty in determining the prestress force.



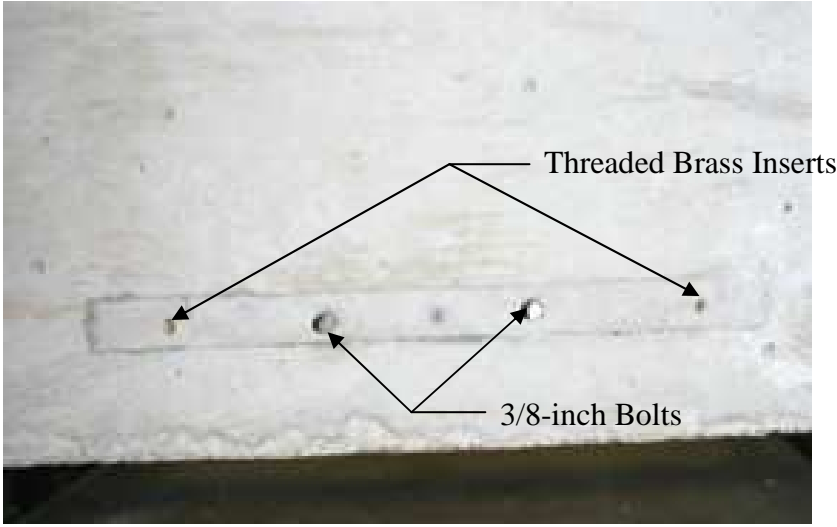
(a)



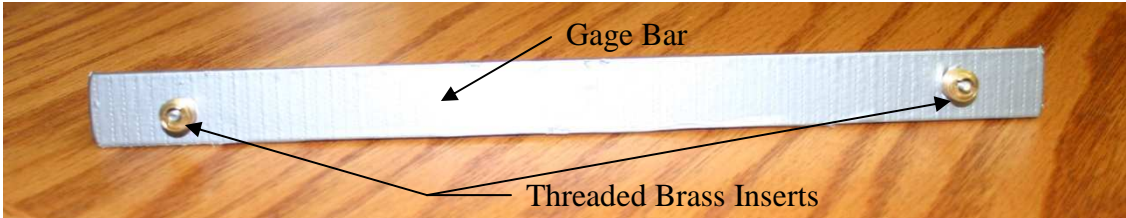
(b)

Figure 3.3 a) Crack Former, b) Location of Crack Former

Two 3/8-inch bolts were positioned two inches up from the bottom of the beam, and two inches from center, to aid in mounting LVDTs for measuring the crack opening at the strand height. In addition to the bolts at the height of the strand, two threaded brass inserts were embedded eight inches apart, as shown in figure 3.4. Quarter-inch by 3/8-inch, threaded brass inserts were attached to a gage bar which was then inserted into the forms to be cast into the beam. The bar was covered with duct tape to prevent it from adhering to the concrete. Using a Whittemore gage, initial distance between the points was measured and later related to the losses of the prestress force in the beam.



(a)



(b)

Figure 3.4 a) Inserts Cast into Beam, b) Inserts on Gage Bar

The two sets of beams were cast in series, so theoretically these would be the same prestress force in each beam. This allowed the testing of one beam initially and the testing of the

second beam after a majority of the creep and shrinkage losses had occurred. According to Dr. B.C. Punmia, Ashok K. Jain, and Arun K. Jain, 50% of shrinkage occurs within the first month after the start of curing and 75% takes place in the first six months. Fifty percent of creep occurs one month after loading and 75% occurs after six months from the initial loading (2003). A period of a minimum of six months elapsed before testing the second beam from each series to ensure a majority of the losses due to creep and shrinkage had occurred. A comparison between the two beams showed whether any residual stresses were not fully relieved on the core from creep or shrinkage of the concrete due to the prestress force. The beams were design for a maximum compression stress at the bottom of the beam, while staying within the maximum allowed stress ranges. This allowed for the assumption that the beams would behave elastically.

Wooden forms were built with inside dimensions of six inches by 12 inches. The forms were continuous with a total length of 21 feet. Two beams were cast end to end in the forms, leaving a six-inch space between the beams to allow for de-tensioning. Each strand was initially jacked to one kip to align the forms to the center of the strand, and place the stirrups and top bars in place. Once all the forms and steel were in place, each strand was jacked to 75 percent of the tensile strength of the strand, or 31 kips. Figure 3.5 shows the overall setup of the forms with all the steel placed in the forms and the strands tensioned to 31 kips. Each strand had a load cell on one end to verify the load in the strand. A bracket was designed to allow a load cell to be positioned on each end and not interfere with the other strand position two inches away (see figure 3.6). Using a post-tensioning jack with an electric hydraulic pump, each strand was stressed individually and then a chuck was seated to hold the force in the strand. The final stress in each strand was approximately 160 ksi after the seating losses of 15%.

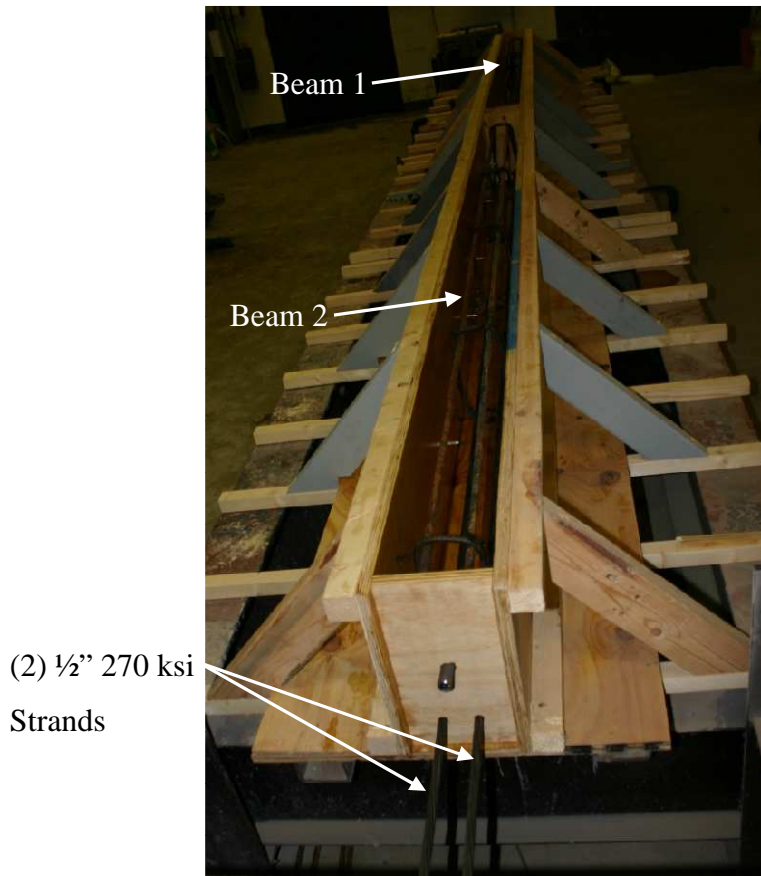


Figure 3.5 Completed Forms with Strand Tensioned

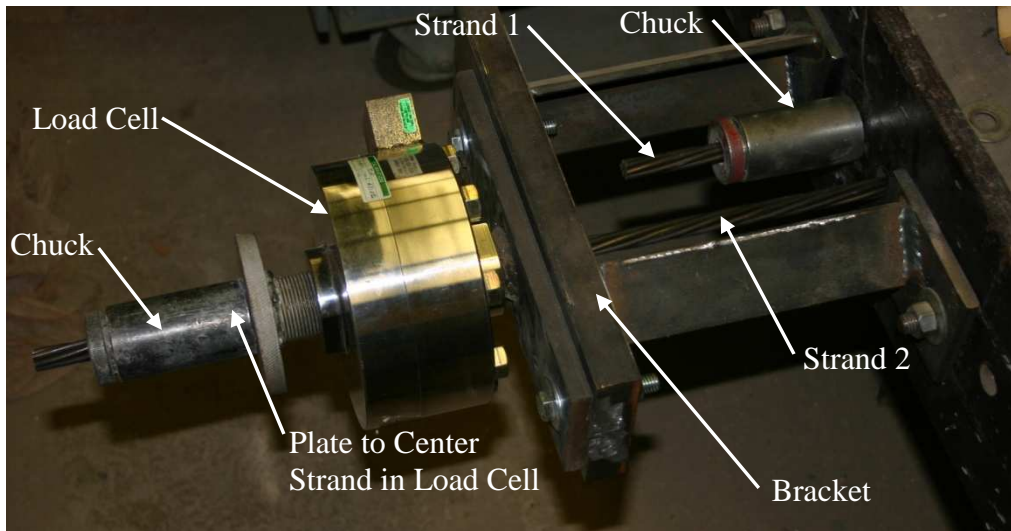


Figure 3.6 Load-Cell Bracket

The beams were cast using a trailer-mounted portable drum mix with a capacity of one cubic yard. Fifteen cubic feet of concrete was batched for each set of beams, which included taking a slump and air test, and making four 6x12 cylinders and nine 4x8 cylinders. All materials were weighed out into barrels using a 2,000-pound-capacity crane scale. Aggregates were weighed out the night before casting and sealed in 55-gallon barrels to prevent loss of moisture. Three samples were taken from the aggregate piles to calculate moisture content in the aggregates. Once the moisture content was known, corrections were made to the mass of the aggregates and to the amount of water needed for the mix. Aggregates were added to the mixer first by dumping them into a hopper that guided the materials into the mixer (see figure 3.7). Next, cementitious materials were added with the water and admixtures added last (see figure 3.8). The water was added using a pressurized water tank where the mass of the water could be measured.



Figure 3.7 Adding Aggregates to Mixer



Figure 3.8 Adding Water to Mixer

Once the concrete had been thoroughly mixed, it was dumped into wheelbarrows and samples were taken to determine slump and air entrainment. Following ASTM C143 (2000) and C138 (2001) a slump of three inches was found for each mix and an air entrainment of five percent was determined. Concrete cylinders were made for determining average compressive strength and modulus of elasticity of the mix, and these cylinders were created following ASTM C31 (2003). The cylinders were cured next to the beam to represent the beam properties and not the ultimate strength potential of the mix. When placing concrete in the beam, a concrete vibrator was used to consolidate the concrete around the reinforcement and to create a smooth surface for mounting gages on the sides of the beams. A wooden hand trowel was used to finish the top surface of each beam, and then the beams were covered with wet burlap followed by plastic until the next day when the beams were de-tensioned.

The forms were removed the next morning and three concrete cylinders were broken to determine an average strength of the concrete. For the first set of beams, the strength was 6350 psi and for the second set it was 5970 psi, well above the required 4200 psi. Before de-tensioning, the load at each load cell was recorded and represented the force in each strand. The Whittemore gage was used to measure the initial distance between the brass inserts. De-tensioning was done using an oxy-acetylene torch, cutting one wire in the first strand followed by a wire in the second strand and continuing this process until all wires were cut. This

prevented a sudden release which could spalling or other damage the beam. Next the beams were picked up and placed on blocks at each end. Using the Whittemore gage, readings were taken on the brass inserts to record initial losses in each beam and to find the average prestress stress in each strand. Stresses in each strand during casting and after de-tensioning are shown in table 3.2. Initial stress values are given for each strand from the load cell positioned on each strand. The post de-tensioning values are from the Whittemore measurements and represent the average prestressing force in each strand. The beams were then transported to a storage area where they were allowed to cure and be prepared for testing.

Table 3.2 Stress in Each Strand

	Average Stress (ksi)		
	Initial Pull	Before Casting	After De-tensioning
Beams 1a and 1b			
Strand 1	208.6	176	163.9
Strand 2	205.7	172.5	163.9
Beams 2a and 2b			
Strand 1	205.3	161.8	143.1
Strand 2	185.0	164.7	143.1

3.2 Rectangle Specimen Material Properties

The four rectangle beams were cast in two separate pours using the same materials and design mix. Each mix had a 28-day design strength of 6000 psi and a release strength of 4200 psi. Table 3.3 shows the average compressive strength at release and 28 days. Each mix had very similar average compressive strengths as shown in the table. The average modulus of elasticity was determined at the time of the surface-strain relief method and was found to be 3,528 ksi for the first pour and 3,750 ksi for the second pour. The prestressing steel had a tensile strength of 270 ksi and a modulus of elasticity of 28,500 ksi. Other steel, such as the top bars and stirrups, had a tensile strength of 50 ksi with a modulus of elasticity of 29,000 ksi.

Table 3.3 Compressive Strengths of the Concrete Mixes

Pour	Average Compressive Strength	
	At Release	28 Day
1	6350	7490
2	5970	7390
Design	4200	6000

3.3 T-Beam Specimen Geometries Properties

The prestressed concrete T-beams were cast at Prestressed Concrete, Inc. (PCI) in Newton, Kansas, in March of 2002. The T-beams had a top flange 18 inches wide and four inches deep, with a tapered web four inches wide at the bottom and a total depth of 14 inches (see figure 3.9). The T-beam had two straight 3/8-inch 270 ksi low-relaxation strands, one two inches up and another four inches up from the bottom and jacked to a stress of 202.5 ksi. Additional mild reinforcement of D4-welded-wire reinforcement was placed in the beam at 1.25, three, four, and seven inches from the top. Shear reinforcement was provided in the form of D4-welded-wire reinforcement placed four inches on center in the flange and D6-welded-wire reinforcement placed four inches on center in the web. Crack formers were embedded in the bottom of the beam to initiate a crack in the web of the beam at three locations—mid-span and 3.5 feet from each side of mid-span (see figure 3.10).

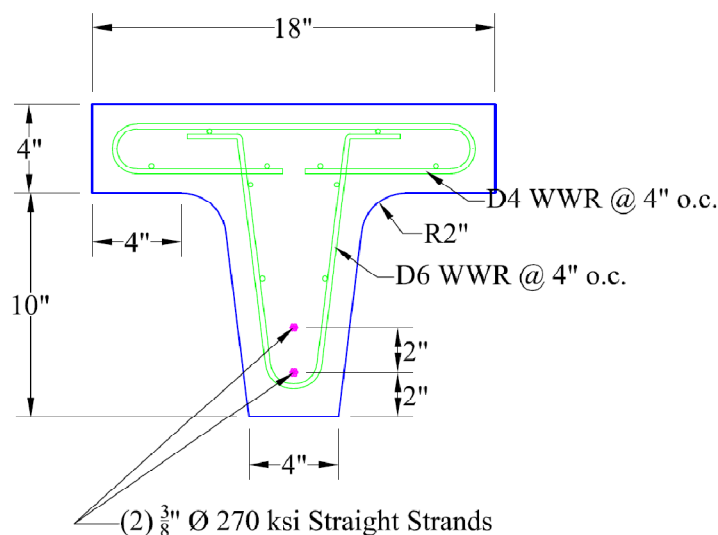


Figure 3.9 Cross Section of T-Beam

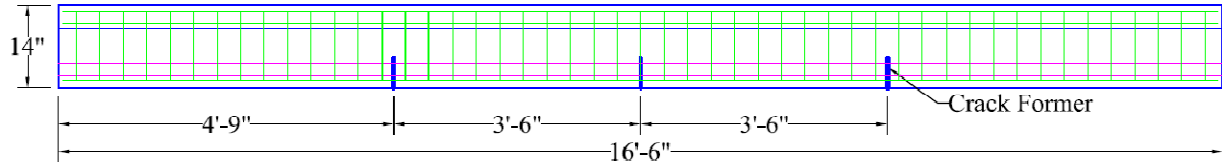


Figure 3.10 Locations of Crack Formers

3.4 T-Beam Specimen Material Properties

The T-beams were produced in 2002 at a prestressed plant in Kansas. The plant provided concrete strength measurements through standard cylinder testing. The average 28-day strength was measured at 7,040 psi. Average modulus of elasticity was obtained from the crack-opening procedure and found to be 3,285 ksi. The 3/8-inch strand used in the beams had a tensile strength of 270 ksi and an elastic modulus of 28,300 ksi. The additional mild steel reinforcement had a tensile strength of 80 ksi and an elastic modulus of 29,000 ksi (Larson 2002).

Chapter 4 - Surface-Strain Relief Method

The surface-strain relief method determines residual strain on the surface of a member and relates it to residual stresses in the member. For prestressed members, residual stress can be considered primarily due to prestressing force applied to the beam. The surface-strain relief method has four main steps:

- 1) Measuring initial strain,
- 2) Coring or cutting notches,
- 3) Measuring relaxation of the concrete, and
- 4) Relating relaxation of the concrete to the average prestress force.

Two methods were explored to measure surface strain—traditional linear electrical-resistance strain gages (ERSG) and a laser-speckle imaging (LSI) device. Initially, residual stresses on the surface were relieved by coring around the strain gage, but upon further research, a method of notching was used and showed promising results. The core and notches were cut to varying depths to determine optimal depth and were compared with finite-element models. The strain was measured after each incremental core or notch depth. Change in strain was assumed to be the relief of the residual stress and was used to calculate average prestress force in the member.

4.1 Measurement of Strain

Two methods were used to measure surface strain—the traditional linear electrical-resistance strain gage and the LSI device. The linear-resistance strain gages were used with a concrete diamond coring bit and with notches. Phase I showed minimal error with a strain gage and core, so the effectiveness of the notch procedure was compared to the coring process. The LSI device was not used with the core because it measures the strain over a larger area, requiring a larger core bit. A larger core would provide many disadvantages to the method, and limit possibilities and applications. With a larger core, location of the core would be affected. With a three-inch core, the center of the core must be approximately two inches up from the bottom in order to provide enough space to prevent the core bit from breaking out the concrete at the bottom of the beam, as well as provide the necessary space to mount the guide. With the larger

gage length and development of the notches, the LSI device provided an opportunity to simplify the method.

With either method, the linear-resistance strain gage or the LSI device, the strain is only measured in one direction. In order to get the least error and the largest change in strain, the strain gage or the optical device must be positioned parallel to the axis of maximum strain. For the interest of this project, the remaining prestress force was being investigated, so the gages were positioned along the centroid of the prestress strand.

4.1.1 Strain Measurements with Strain Gages

Linear-resistance strain gages from Vishay Micro-Measurements were used for the majority of the testing due to the reliability and known accuracy of the strain gages. Vishay EA-06-20CBW-120 strain gages were used with a gage length of two inches and a resistance of 120 ohms. Following Vishay Micro-Measurements Tech Note 505-4, two-inch strain gages were used due to the size of the aggregates in the concrete mix design (Vishay Micro-Measurements 2007).

To mount the strain gages, locations of the gages were marked on the surface of the beam and this area was lightly ground down to remove any laitance from the surface. Following Vishay Micro-Measurements Tech Note 611 (2010) for mounting strain gages on concrete surfaces, AE-10 epoxy was used to fill in any voids in the surface of the concrete and provide a smooth surface to mount the gages. Vishay Micro-Measurements Bulletin B-137 (2010) was followed to prepare the surface and to mount the gage to the AE-10. Once the gages were installed, short lead wires, approximately two inches in length, were soldered to the gage and a four-pin terminal block connector was soldered on the other end to allow the gage to be quickly connected and disconnected during the coring process. M-coat polyurethane coating was applied over the gages to prevent damage to the gage, and for further protection, microcrystalline wax was applied over the M-coat. Type I/II silicone was used to hold the terminal block in place and prevent movement during coring (see figure 4.1).



(a)



(b)



(c)

Figure 4.1 a) AE-10 Applied to Surface with Alignment Marks, b) Gage Applied and Clamped in Place, c) Completed Gage with Connection

4.1.2 Laser-Speckle Imaging (LSI) Device

The second method incorporates the LSI device, which was developed at K-State (Zhao 2011) (see figure 4.2). The device uses the surface of the beam to measure the change in displacement. It images the speckle pattern produced by a laser, reflecting off the surface as shown in figure 4.3. The speckle pattern produces a unique pattern from the member's surface, serving as a fingerprint of the location. Two locations are imaged simultaneously, initially, to serve as the reference point. Subsequent measurements are correlated to the reference images to find the amount of displacement.

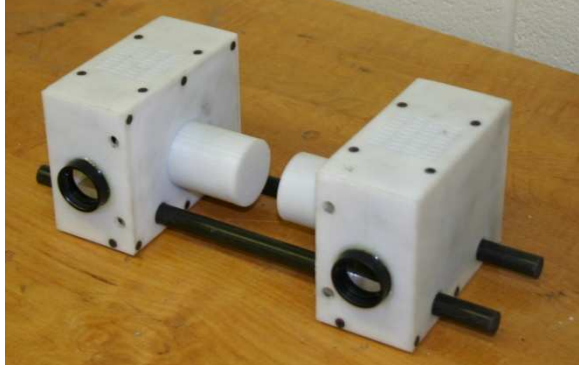
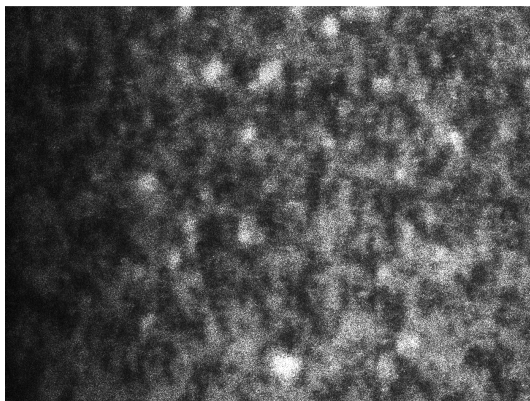
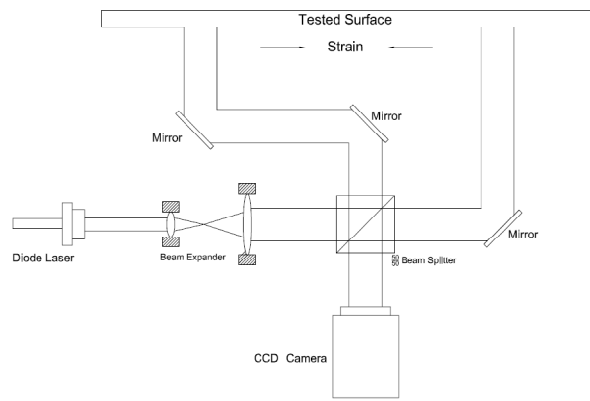


Figure 4.2 Laser-Speckle Imaging Device



(a)



(b)

Figure 4.3 a) Laser-Speckle Imaging from the Concrete Surface, b) Schematic of Laser Speckle Strain Measurement System

The LSI device consists of two modular units allowing for varying gage lengths and multiple applications. To make the LSI device applicable to the surface-strain relief method, the gage length need to be shortened from eight inches, a similar gage length to the Whittemore gage, to approximately two inches. This gage length was much too large to be able to core around or to cut notches on either side. Each modular unit was positioned back to back, as seen in figure 4.4, on two carbon rods for a gage length of approximately two inches. The LSI device can accurately measure displacement due to an applied stress by correlating a reference image with the image captured due to the applied stress. For determining the change in strain due to residual stresses, a gage length had to be accurately determined and checked to minimize errors in the data. The determination of the gage length is described in the following paragraphs.

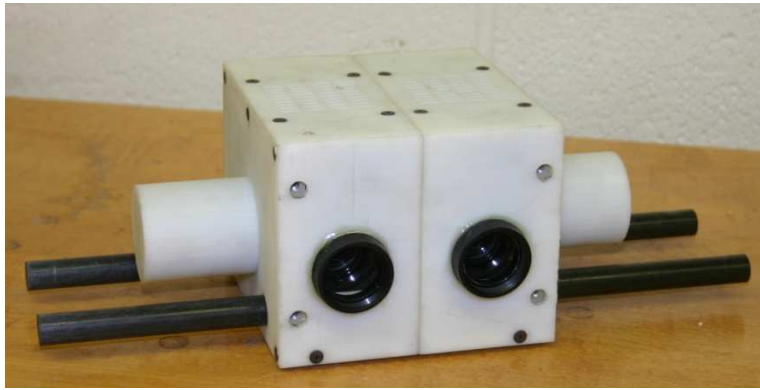


Figure 4.4 Laser-Speckle Imaging Device with Two-inch Gage Length

First the approximate gage length was measured by placing a ruler divided into 1/32-inch marks down on a flat surface and viewing each image produced by the camera. The ruler was positioned so zero was at the center of the left camera's viewing area, and then the distance was recorded from the right camera's viewing area. This gave an initial gage length estimate of 2.1875 inches.

An experiment was developed using a simply supported beam setup in four-point bending with a clear span of 10 feet. The four-point bending setup was used to create a constant moment region at the center of the beam. To achieve larger strains with applying minimal force, an aluminum c-channel was chosen due to its relative small modulus of elasticity when compared to steel, to calibrate the device. A c-channel C6x10.5 was used as the beam to calibrate the LSI device, using its weak axis moment of inertia to develop large strains in the channel. In the constant-moment region, the strains could easily be calculated by determining the stress developed by the bending moment and converting the stress by dividing it by the modulus of elasticity of the aluminum. To measure the strain on the c-channel, two strain gages were mounted on the top surface of the channel at the mid-span and one inch from the center as shown in figure 4.5. The LSI device then was used to measure the strain between the two strain gages. Initially each strain gage was zeroed and an initial reading was taken using the LSI device. To determine the accuracy and precision of removing the device, a series of five readings was taken at each strain level, removing the device in between each reading. At zero strain, the device provided consistent readings within 10 microstrains. Next, known masses were hung from two load straps one foot from center as shown in figure 4.6. Another series of five readings was

taken and compared to the two strain gages. These values were recorded and the masses were increased, and the procedure was repeated. Once the measurements were complete, all the mass was removed and a zero reading was taken to confirm that the device would measure zero strain and that no error had been introduced. The first trial saw a shift when the mass was removed, and it was determined that the internal temperature of the device had increased. So one hour was used to allow the device to reach its operating temperature and the shift was not noticed in the following tests.

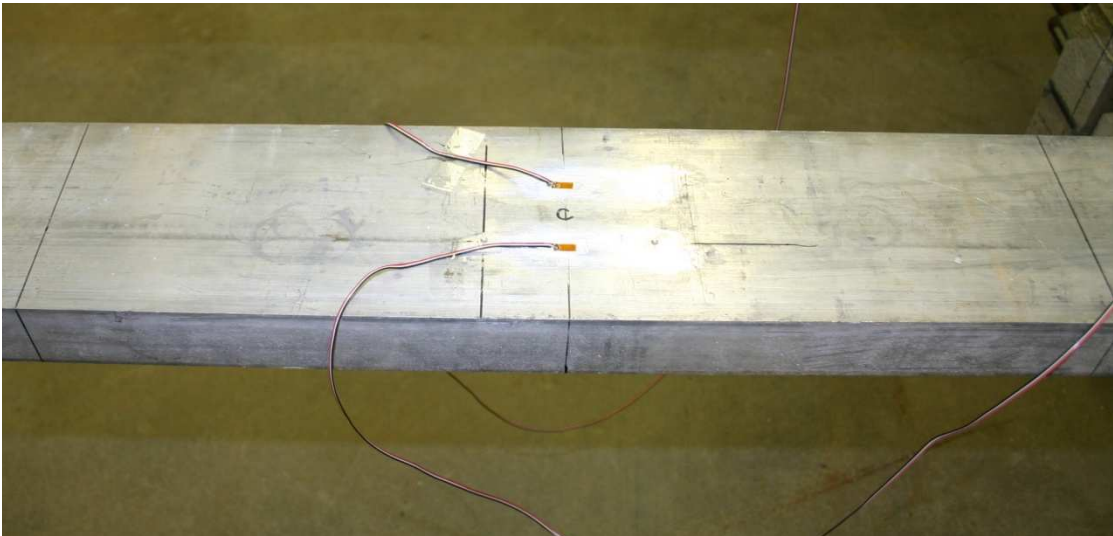


Figure 4.5 Strain Gages Mounted on Channel

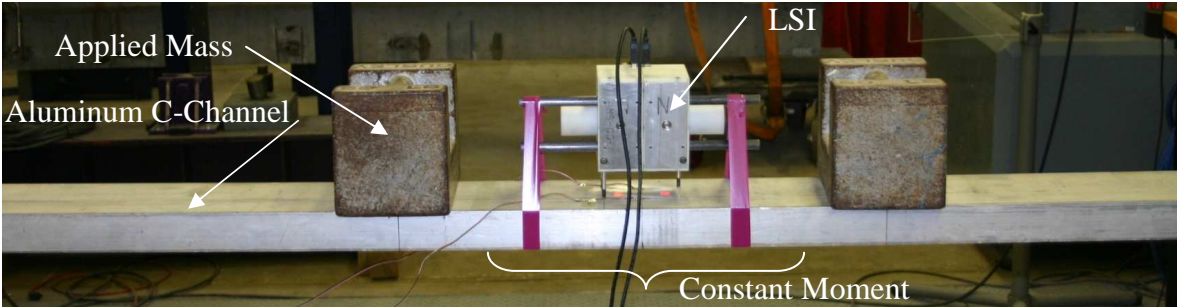


Figure 4.6 Channel Loaded

To calculate gage length of the device, the change in displacement data taken by the device was averaged from the five readings taken at each applied load. With the two strain gages used as the real strain, the change in displacement measured by the device was divided by the

average strain reading from the linear-resistance strain gage. This was done for each applied load and then the calculated gage factors were averaged to get a gage factor. Five trials were conducted and an average gage factor of 2.05 inches was obtained. Each calibration trail was plotted versus the applied moment, along with the measured strain from the two strain gages to ensure both were providing linear measurement. Figure 4.7 shows an example of the measurements as well as a very linear response of both the strain gages and the non-contact optical sensor.

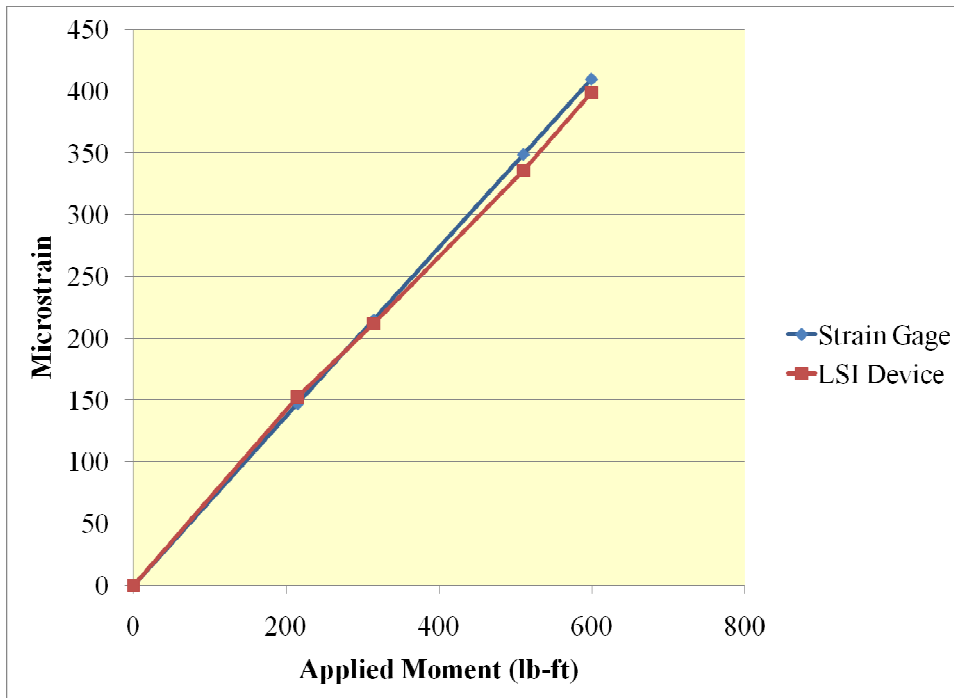


Figure 4.7 Laser Speckle Compared to Strain Gage

With the gage length determined, the next step was to test the method on concrete. Using rectangular specimens with dimensions of 3.75 by 3.75 inches and 18 inches long, the device measured the initial condition using similar methods as when calibrating it by taking five measurement at each load. Next, using a hydraulic jack and small movable load frame, an axial load was applied to the test specimen and the device was used to measure the change in strain as shown in figure 4.8. The measured strain was then compared to the calculated theoretical strain. The measured strains were within 5% of the theoretical strains, which shows an acceptable error. Some of the error could be a result in small eccentricities in the loading of the specimen due to

the ends of the member not being square with the load frame and the hydraulic jack. The modulus of elasticity was determined from cylinders cast when the specimen was casted, and variations can occur in the modulus of elasticity from member to member, introducing another source of error. Initial testing of the LSI device on concrete provided acceptable results.

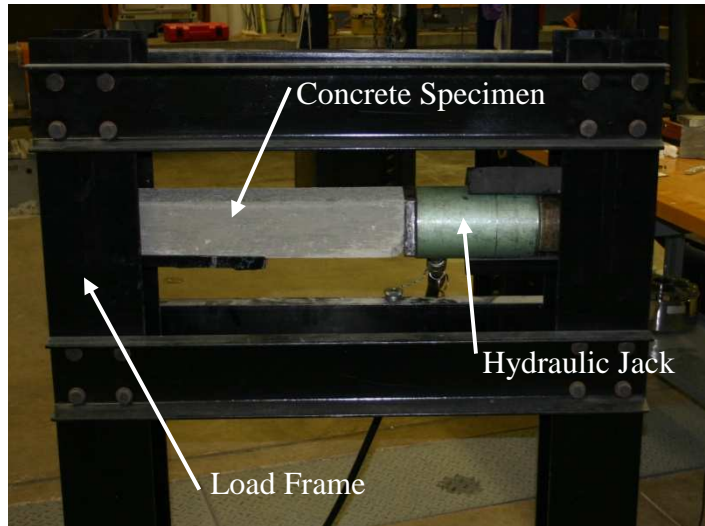
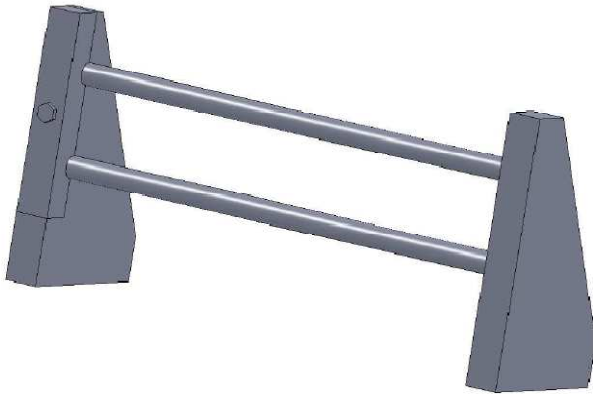
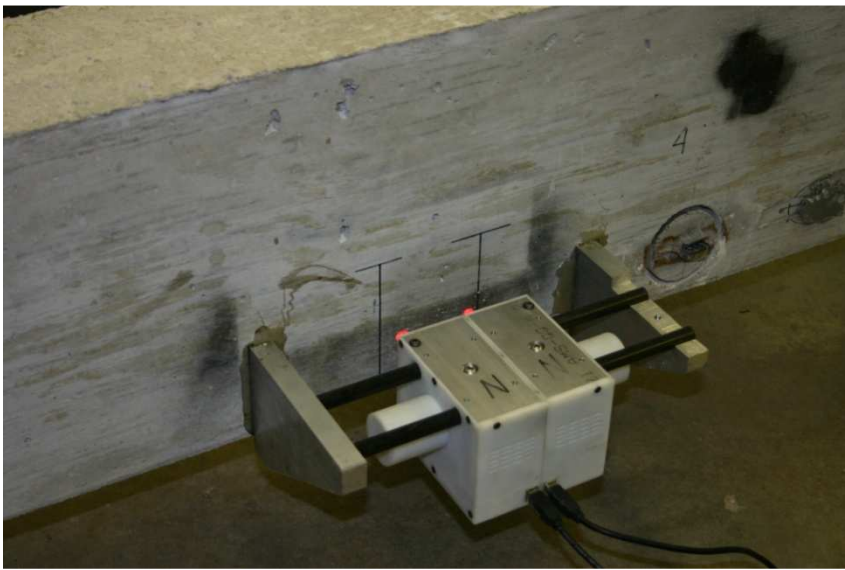


Figure 4.8 Concrete Specimen in Load Frame

Unlike the strain gages, the LSI device must be removed from the surface of the beam so the area can be notched. Accuracy of the LSI device is determined by the ability to reposition the device in the same spot each time. To aid in placement of the device and maintain the distance away from the surface, two brackets were fabricated to be attached to any surface while remaining out of the way for the notch-cutting process. The brackets, shown in figure 4.9, positioned the two carbon rods that each module was mounted on in the same location each time. To secure each bracket, a five-minute epoxy was used along with concrete screws to temporarily hold the bracket in place while the epoxy cured.



(a)



(b)

Figure 4.9 (a) Laser-Speckle Imaging Device Mounting Brackets, (b) Laser-Speckle Imaging Device Mounted to Beam

The device uses the surface of the concrete to determine the displacement. Extra care had to be taken to preserve the surface and not damage it to prevent introducing large errors or losing correlation and losing the data point. The surface was cleaned using a wire brush and compressed air before imaging the reference reading. Tape and plastic were used to cover the surface, making sure to only have the tape touch the surface of the beam near the notch and not where the surface would be imaged, to protect it while cutting notches in the concrete. Using the same specimens to verify the strain readings, the method of surface-strain relief was tested. The

developed brackets were attached to the concrete surface using a five-minute, quick-setting epoxy. Next initial readings were taken with the test specimen under an applied stress, and then the procedure for notching was followed.

4.2 Coring Process

The coring process relieves the stress surrounding the strain gage, allowing for the measure of residual stresses. Relief stresses on the surface are a function of the depth of the core. From the findings and conclusions of phase I, a depth of $\frac{3}{4}$ to one inch was determined to fully relieve the stress on the surface of the core. Depth of the core was checked on prestressed members by coring to varying depths and recording the changes in strain. Phase I used a one-inch strain gage and a 2.5-inch-diameter diamond dry-coring bit, but with a two-inch strain gage, a three-inch-diameter diamond dry-coring bit was used. Michael McGinnis (2006) and David Marks (2009) noted that water was used to cool the core bit, preventing fluctuation in strain readings due to increase in temperature caused by the coring of the concrete. McGinnis also determined that water used during coring induced swelling in the core and increased the measured strain on the surface. A dry-coring method was used to prevent stresses due to water-induced swelling. To correct for the temperature increase, a non-contact thermometer was used to measure the temperature in and around the core.

The first step of the coring process was to record the initial strain values, which were set to zero microstrain. All gages were excited with two volts through a strain indicator used in conjunction with a switch-and-balance unit to monitor the multiple-strain gages. Once the gages had been zeroed with the switch-and-balance unit, the terminal block was disconnected from the gage and then reattached to record any difference in strain from the connection. An error of ± 1 microstrain was recorded as the maximum error observed from the terminal block connection. Next, the lead wires were disconnected and checked to ensure they were securely attached to the center of the core. Layout marks from positioning of the strain gage were extended in order to position a guide for the diamond core bit. A wooden guide was built using $\frac{3}{4}$ -inch particle board, with a stop on the bottom to help in locating the center of the core. Using the provided layout marks, the guide was next mounted on the surface of the beam and centered on the strain gage. A hole was cut slightly larger than the diameter of the core bit to allow it to spin freely within the guide. The guide prevented the bit from moving on the surface of the beam as the

coring process started and prevented the possibility of damaging the gage. To prevent excess friction and keep the amount of concrete dust to a minimum, a vacuum was used near the core hole to remove the concrete dust. When a depth of $\frac{1}{2}$ inch was reached, a caliper was used to measure the depth of the core in multiple locations. This ensured the core was being cored at a uniform depth and perpendicular to the surface. The coring was then continued to $\frac{3}{4}$ inch where the depth was checked again and a strain reading was taken. After 10 minutes, another strain reading was taken and then the coring process was resumed. Ten minutes were allowed between coring increments to minimize temperature effects on the strain readings. After the final depth of one inch was reached, a final reading was taken 10 minutes after the coring was complete.

To investigate effects of temperature and the error induced in the strain measurements, a non-contact thermometer was used to measure the temperature of the surrounding environment and the beam throughout the coring process. Temperature measurements of the beam, core, and ambient temperature were taken initially after each coring increment, and then 10 minutes after each coring increment. To calculate the error caused by the thermal increase, thermal output coefficients from the strain-gage package were used in a regression-fitted polynomial equation (Vishay Micro-Measurements 2007). Using the supplied polynomial curve for the thermal output, the change in strain reading was calculated due to the increase in the temperature. This increase change in strain was then compared to the drift during the 10-minute period to explain the drift in the strain-gage measurement and to correct for any error caused by the temperature increase.

Phase I recommended that each core be fractured at the base of the core, removing the entire core intact. This was done to remove any errors induced by over-coring or strains induced from the surrounding area. Phase II tried to remove the core but difficulty was encountered when trying to do this. The concrete mix used in the test specimens had higher strengths than the mortar mix used in Phase I and used coarse aggregates. When the core was removed, the core fractured at multiple locations, damaging the strain gage on the surface. The coarse aggregate caused an aggregate interlock at the base of the core, which prevented the core from being removed intact. Many methods were tried to remove the entire core with few successful results. Then only successful method was to create a notch next to the core to insert a chisel at an angle and break the core out. Two cores were successfully removed and a change in strain of 10 microstrain was recorded, showing minimal error at the one-inch depth. Removal of the core left

a larger hole in the beam and resulted in more damage to the surface of the beam than just the core, as shown in figure 4.10, when compared to when the core was not removed. The change of 10 microstrain was considered insignificant and caused a minimal error, and it was unable to be determined if the change in strain was caused by removal of the core or from over-coring.

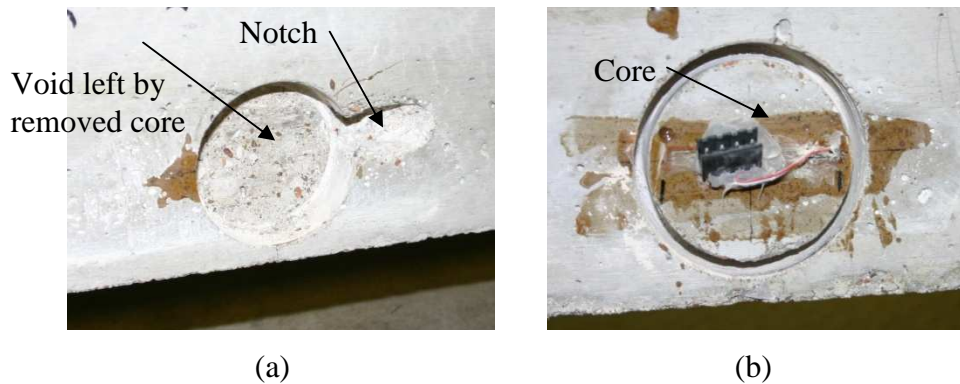


Figure 4.10 a) After the Core Has Been Removed, b) Core Intact

4.3 Notching Process

The notching process provided a simpler and quicker method of relieving the stress at the surface. It was similar to the coring process for measuring the strain at different increments. Multiple depths were tried to determine the optimum depth with a spacing of 3.5 inches between notches. According to David Marks, a ratio of 0.4 of the notch spacing to the depth of the notch provides the maximum strain relief (2009). The notches were cut using a five-inch diamond wheel designed for dry-cutting applications and to be used with a handheld grinder. A variable-depth and dust-extraction guard were used on the grinder to control the depth of the cut and to minimize the dust created. The guide also maintained the blade perpendicular to the surface of the concrete.

Initial balancing of the strain gage was the same as the core procedure, with the gage balanced to zero. Unlike the core procedure, a terminal block connection on the lead wires was not needed. The wires could remain connected to the strain gage at all times but needed to be secured out of the way to prevent the wires from being cut. Spacing between the two notches was set at 3.5 inches. This allowed ample room between the notch and the edge of the strain gage to prevent the possibility of the edge of the cut chipping out and damaging the gage. This

spacing was also used with the LSI device and a direct comparison was made between the two methods. With the LSI device, initial readings had to be taken once mounting brackets and the surface were prepared. A set of 10 reference readings were taken and an average of all 10 was used in calculating the prestressing force. To ensure high-quality reference readings were taken, another set of measurements was taken after the reference readings. To take the second set of readings, the device was removed from the mounting brackets and then repositioned. Once repositioned, another 10 measurements were taken. This ensured no false readings had been taken and the device was working properly.

From the center of the gage, a line was drawn 1.75 inches from each side of the center and five inches up. The line served as a reference for where to cut. Total length of the line was five inches, which allowed for a full-depth cut three inches up from the bottom of the beam or one inch past the center of the top strand. The total cut of five inches represented the curvature of the blade and the intersection on the surface at a cut depth of one inch. For the first two sets of notches, depths of from $\frac{1}{2}$ inch to 1.25 inches in $\frac{1}{4}$ -inch increments were cut around a linear-resistance strain gage, with measurements taken at each depth. For the rest of the notches, depths of $\frac{3}{4}$, one, and 1.25 inches were cut. Five minutes elapsed between each notch depth to allow the gage to stabilize.

To investigate effects of temperature on the notching procedure, a noncontact thermometer was used. With this, initial temperatures of the beam, location of the notches, and ambient temperatures were measured. After the notching was complete, a maximum temperature increase of five degrees Fahrenheit was observed. Within a few minutes, the temperature around the notches was found to be in equilibrium with the surrounding beam. This temperature was much lower than the coring temperature increase, and the temperature increase of five degrees provided minimal strain drift.

4.4 Calculation of the Average Prestress Force

To find the average prestress force in the beam, the measured relaxation of strain had to be converted to the change in stress, which was then related to the stress in the concrete. Using the calculated modulus of elasticity, the strain relief was converted by equation 4.1, Hooke's Law, assuming the concrete is linear elastic.

$$\sigma = E\varepsilon \quad (4.1)$$

where

σ = relieved stress (psi),

E = concrete modulus of elasticity (psi), and

ε = relieve strain (in/in).

The prestress force was then solved from the known stress by the following equation:

$$\sigma = -\frac{P}{A} - \frac{Pe y}{I} + \frac{My}{I} \quad (4.2)$$

where

σ = relieved stress (psi),

P = prestress force (lbs),

A = cross sectional area (in²),

e = prestress force eccentricity (in),

y = distance from the neutral axis (in),

I = moment of inertia (in⁴), and

M = moment due to mass of beam (lb-in).

The moment was calculated from the mass of the beam, but if additional dead load was on the beam at the time of testing such as a bridge deck or floor, the moment due to the dead load would be taken into account within the moment term. The distance from the neutral axis was measured as the distance from the neutral axis to the center of the strain gage. This was done to relate the calculated prestress force to the measured strain at the location where the strain gage was mounted.

4.5 Determining the Modulus of Elasticity of the Concrete

Two methods were used to determine the modulus of elasticity of the concrete—calculating the modulus from the beam during the crack-open procedure, and in accordance with ASTM C 469. Calculating the modulus from the crack-opening procedure will be discussed in section 6.3.2, *Analysis of Crack-Opening Data*.

To determine the modulus of elasticity based on ASTM C 469, four-by-eight-inch concrete cylinders were used from the casting of the beam. Multiple cylinders were made during the casting of the beam to represent a sample of the beam to be used to test the compression and modulus of the concrete. Each cylinder was cured in a similar method as the beam, to represent the properties of the beam and not the ultimate strength of the concrete. The cylinders were tested during the method of surface-strain relief to determine the modulus of elasticity of the concrete at the time of testing. The moduli of concrete changes as strength of the concrete changes, and since the beams were tested at approximately 28 days, and after six months of curing, the modulus could vary significantly. Two samples were tested for each beam, with each sample cycled three times. The samples were tested using a servo-controlled hydraulic actuator to apply the load, and a compressometer was used to measure the strain on the concrete. Using a 16-bit data acquisition system, the load and displacement, measured by the compressometer, were sampled at two hertz. The first cycle was not used in the calculation of the modulus due to possible errors in the installation of the compressometer and of the compression caps used to even out any irregularities, and to allow for the cylinder to be loaded uniformly. The chord modulus was determined using the procedure in ASTM C 469 (2002).

Chapter 5 - Finite-Element Models

To visualize the stress distribution and test many different combinations of core depths and notch configurations, finite-element models were created using Abaqus CAE software. The models represented the prestress members used for the laboratory experiments. Similar dimensions and material properties were used in the model and each model was created without a core and stresses, compared to the theoretical stress calculated in the prestress member, determining that the model was built accurately, and then adding either a core or two notches at the mid-span of the beam.

5.1 Rectangle Beam Models

Initially a base model was created with the same cross-sectional properties as the laboratory specimens. The models did not include information on the transfer length, so high-stress concentrations existed at each of the beams. For determining stresses on the model, the midpoint of the beam was used, which did not include the stress concentrations due to the disregard of the transfer length in the model.

5.1.1 Model Parameters

Each model started with the base model that consisted of a beam six inches wide by 12 inches deep, and a total length of 120 inches. Beams were restrained in the model similar to a simply supported beam, as shown in figure 5.1, with one end pinned and the other end supported on a roller. Two ½-inch strands were positioned in the bottom of the beam, represented as a stringer, and an initial stress of 150 ksi was applied to each stringer representing the prestressing force. An elastic modulus of 3,100 ksi for the concrete, with a Poisson's ratio of 0.2 and 28,500 ksi for the prestress steel elastic modulus and a Poisson's ratio of 0.3, were the only material properties entered into Abaqus. Tensile and compressive strengths were not included into the models due to the fact that no stress exceeded yield or fracture points, and it was assumed that all materials behaved with linear elastically. The top bars were omitted from the model for simplicity because they provided limited stiffness to the model. The top bars were placed in the research specimens to limit the tensile stress in the top of the beam, to satisfy ACI requirements and to prevent cracking of the top portion of the beam.

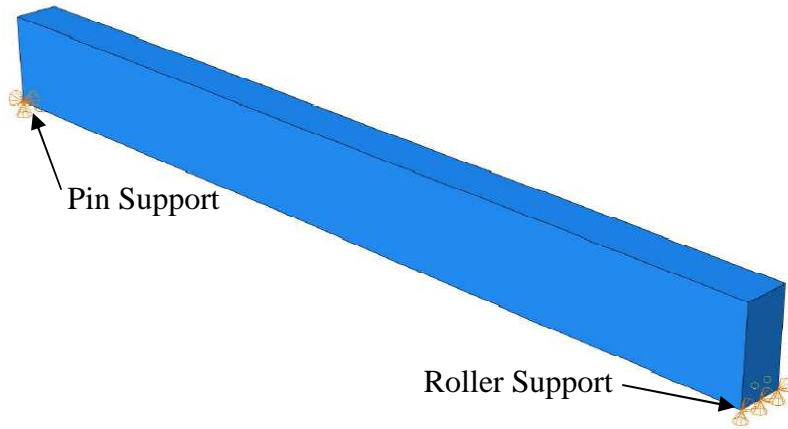


Figure 5.1 Finite-Element Model Restraint

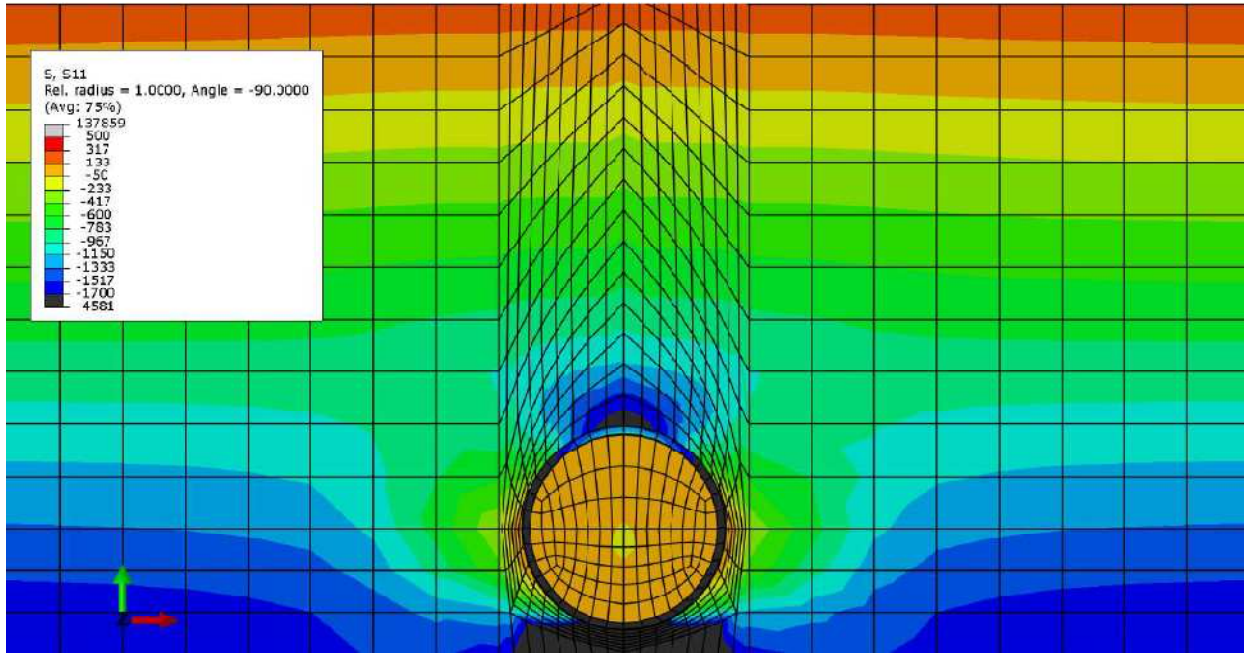
The mesh for each model consisted of beam elements for the prestressed strand and structural hex elements for the rest of the model. Partitions were created around the core or notch to create a finer mesh in this area of interest at the mid-span. This refinement was used also to reduce the computational time of each model. Each model had approximately 8,000 elements, with the finer mesh having an approximate element size of $\frac{1}{4}$ inch and the rest of the model having an approximate mesh size of one inch.

Multiple models were created using the base model, with varying depths of cores and notches. The first three models had cores in the side of the beam with three varying depths— $\frac{3}{4}$, 1, and 1.25 inches. The cores were represented by removing the material between the inner and outer diameter of the core bit, leaving a cylindrical ring cut out. A spacing of 3.5 inches was set as the distance between the notches. Marks determined that a ratio of depth versus the spacing of the notches to be 0.4 (2009), so this was used as a starting point for the first model. The first model created had a notch depth of 1.25 inches with spacing between notches of 3.5 inches. The notch was modeled as a cut three inches long at the bottom of the notch, creating the total length on the surface to be approximately five inches. This model seemed to overestimate the residual stress in the member and a significant tensile stress was seen on the surface. The depth of the core was reduced to one inch, with everything else staying the same, and full relaxation was not achieved. The depth was then increased to 1.125 inches and a full relaxation was shown with no significant tensile stresses present. For the prestress beams, a ratio of depth versus spacing of 0.33 results in full relaxation. To test this hypothesis, the depth was changed to one inch and the

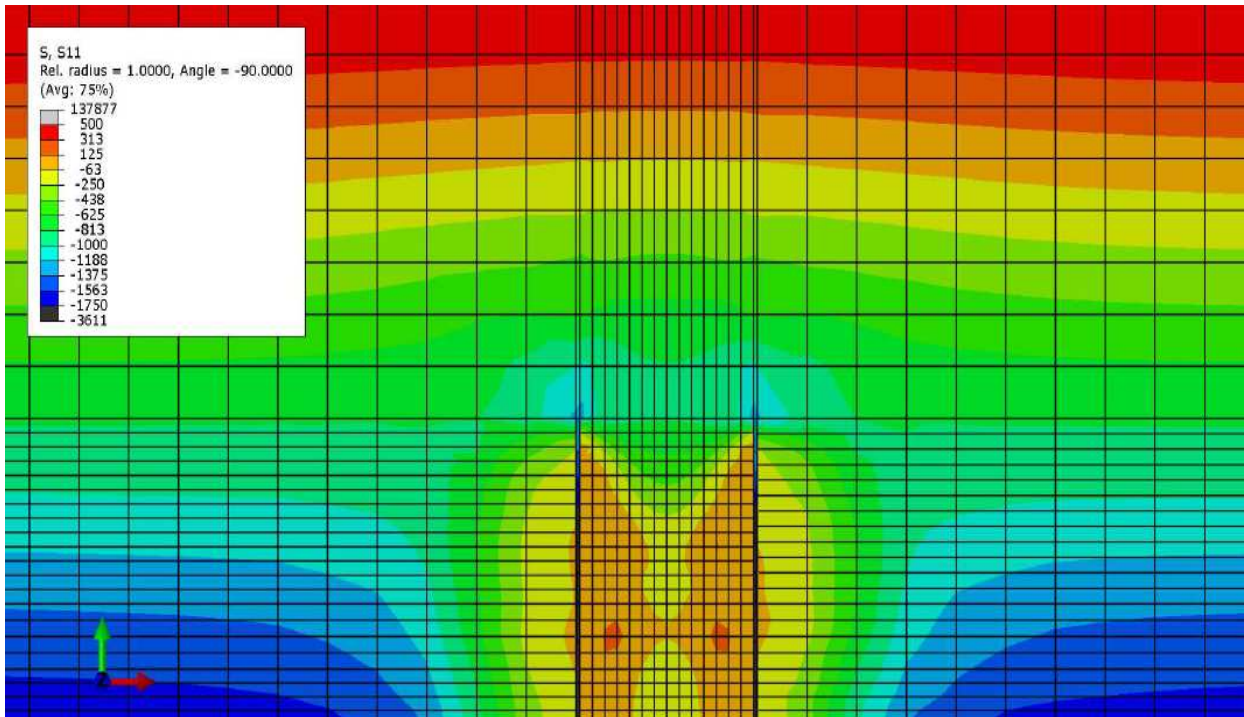
space was reduced to three inches, which resulted in a similar full relaxation. Total length of the notch was also varied but was not found to affect the results significantly.

5.1.2 Results

All models started from the same base model and contained the same parameters. Thus they could be compared directly to one another. To compare the models, stresses were measured at each node location along the center of the core or notch as shown in figure 5.2, showing the stress distribution. This area along the center of the core or notch would also be where the strain measurement would be taken with a strain gage or LSI device. To determine the residual stress that would be measured by a strain gage or the LSI device, the stress values were plotted as in figure 5.3, and Simpson's rule was used to calculate the area under the curve where the strain gage would be positioned. Stress near the edges was near zero as expected, but a tensile stress increase followed with a decrease in stress to the midpoint. To get a full relaxation, the tensile stress needed to be balanced out by the compressive stress towards the midpoint of the core.



(a)



(b)

Figure 5.2 (a) Stress Distribution Across Core, (b) Stress Distribution Across Notch

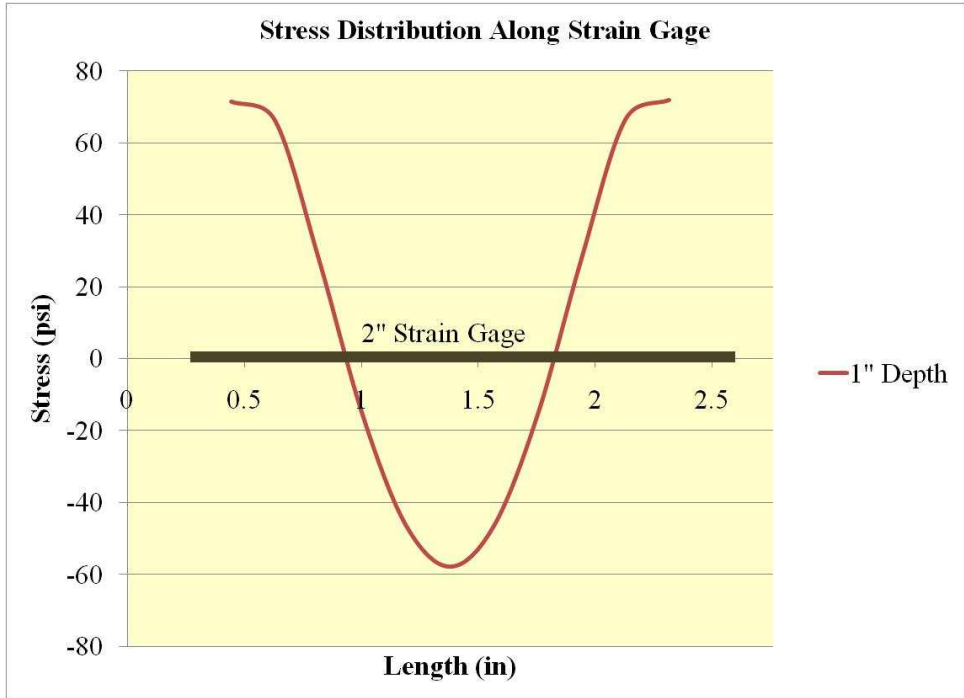


Figure 5.3 Plot of Stress along Length of Strain Gage

Table 5.1 shows the depth of the core and the calculated stress using Simpson’s Rule, along with the percent of relieved stress. The percent of relieved stress was calculated from the prestressing stress of -1490 psi, which was found on the non-cored beam two inches up at mid-span of the beam. Both table 5.1 and figure 5.4 show that ¾-inch core depth does not provide a full relaxation of the stress and that the 1.25-inch core depth provides a full relaxation. But some induced bending stresses resulted causing a tensile stress, which over-predicts the amount of applied prestress force. The one-inch core depth balanced out the compressive stresses and tensile stresses, providing a near 100% relief of stress, just slightly overestimating the prestressing stress.

Table 5.1 Calculated Stresses and Percent Relieved Across Cores

Core Depth (in)	Simpson's Rule Calculated Stress (psi)	% Relieved Stress
0.75	-266	82%
1.00	15	101%
1.25	174	112%

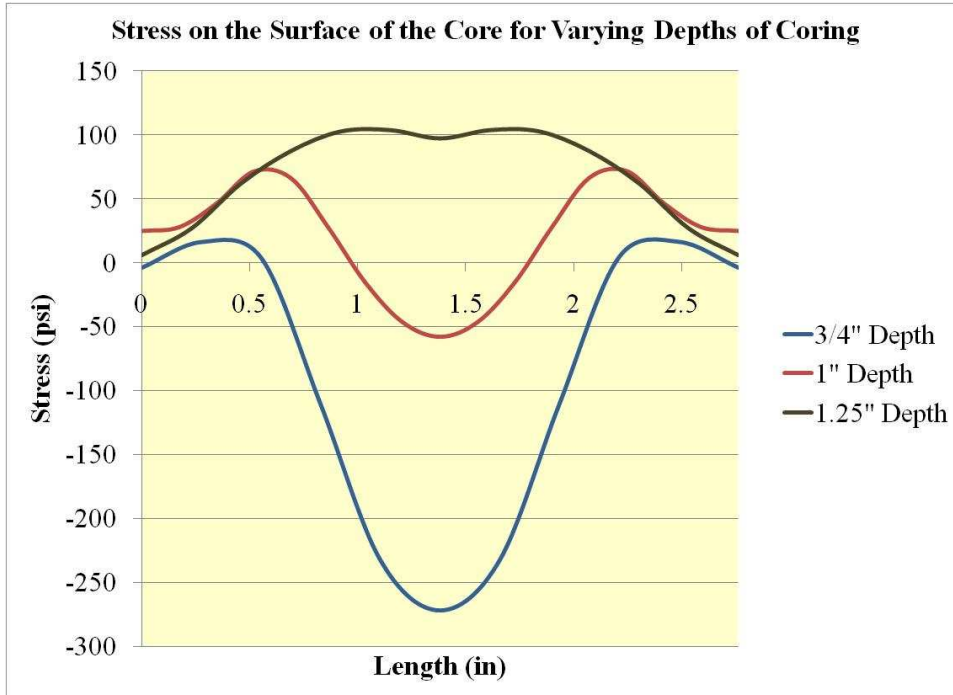


Figure 5.4 Plot of Stress on Surface of Cores

Stresses relieved by the notches were more dependent on depth than on the cores. Figure 5.5 shows the plots of the varying depths of notches, while keeping the spacing and length of the notch constant. A depth of 1.125 inches was found to represent a full stress relief as seen in table 5.2. A change in depth of ± 0.125 inch results in a large change in relieved stresses, either under- or over-estimating the residual stresses.

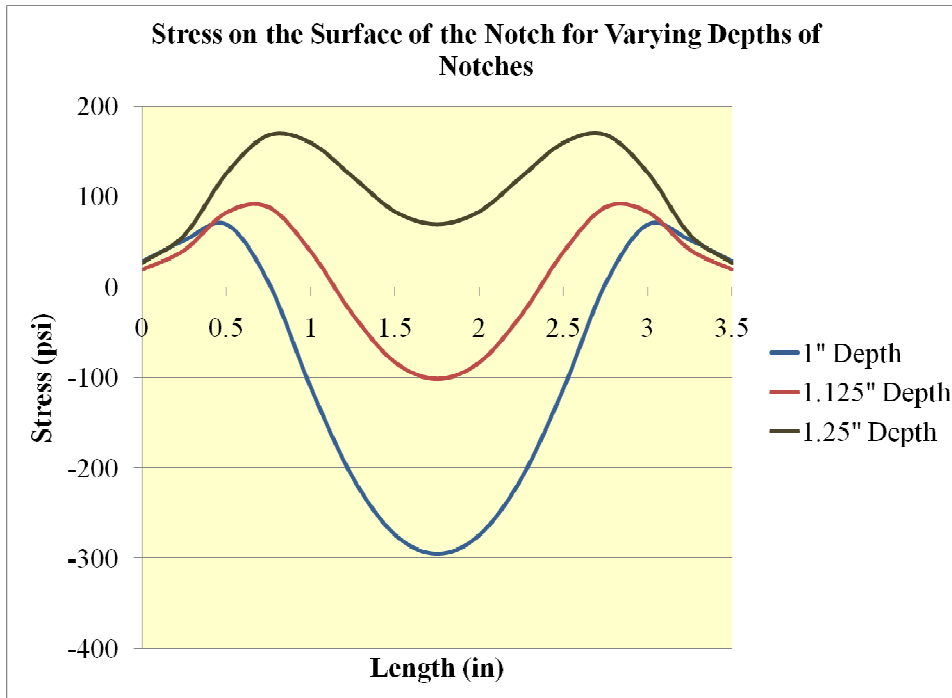


Figure 5.5 Plot of Stress between Notches

Table 5.2 Calculated Stresses at a Spacing of 3.5", Length of 3", and Varying Depth

Notch Depth (in)	Simpson's Rule Calculated Stress (psi)	% Relieved Stress
1.00	-352.85	76%
1.13	3.97	100%
1.25	317.93	121%

There are more variables to the notching procedure to relieve the stress than just the depth of the notch. To look at these, three models were created to examine the spacing of the notches and three models to view the length of the notches. The three models varied the total length of the notch that was cut to the full depth of one inch. The lengths looked at were two inches, which is up to the strand height, and three and four inches, while keeping the spacing at 3.5 inches and a depth of one inch. Figure 5.6 shows lengths of two and three inches are very similar, with a length of four inches relieving the least amount of stress. Table 5.3 reinforces that the relief of stress between a length of two and three inches is similar at 76% but still not full relaxation. Next, the spacing between the notches was modified to see its effects on the relieved stress. Three spaces of 2.5, 3, and 3.5 inches were compared using a constant depth of one inch

and a length of three inches. Figure 5.7 shows the plots of the three varying lengths, with each spacing aligned with the center of the others. As the spacing got closer together, the amount of relieved stress increased. At a spacing of 2.5 inches, influences of each notch seemed to influence the relieved stress, creating a positive tensile residual stress between the notches. Table 5.4 shows the calculated stresses and the percent of relieved stresses. A spacing of three inches seems acceptable, with a 5% error.

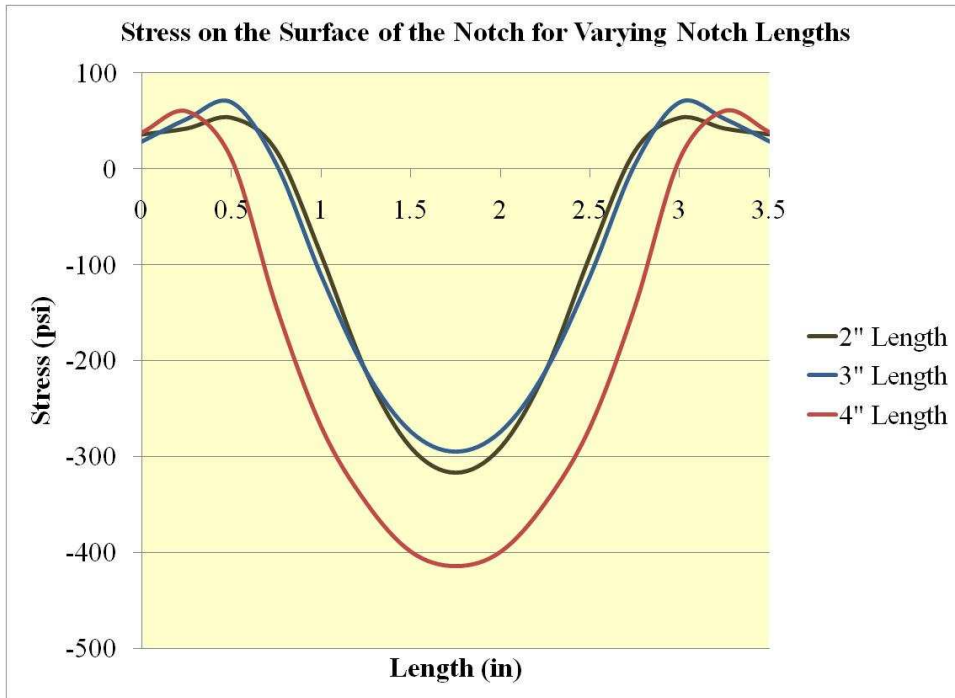


Figure 5.6 Plot of Varying Length of Notches

Table 5.3 Calculated Stresses At a Notch Depth 1”, Spacing of 3.5”, and Varying Length

Notch Length (in)	Simpson's Rule Calculated Stress (psi)	% Relieved Stress
2.00	-351.47	76%
3.00	-352.85	76%
4.00	-689.35	54%

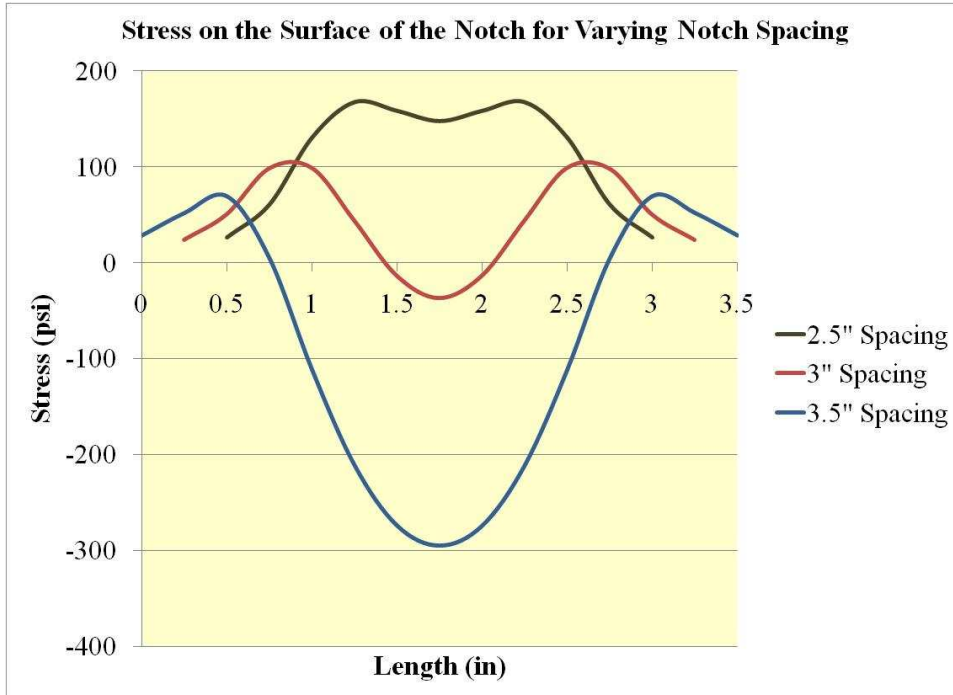


Figure 5.7 Plot of Varying the Spacing of Notches

Table 5.4 Calculated Stresses at a Depth of 1", Length of 3", and Various Spaces

Notch Spacing (in)	Simpson's Rule Calculated Stress (psi)	% Relieved Stress
2.50	283.18	119%
3.00	81.45	105%
3.50	-352.85	76%

According to Marks, the ratio of depth to spacing should be around 0.4 (2009). The two combinations of notches seem to be a depth of one inch and a spacing of three inches, or a depth of 1.125 inches and a spacing of 3.5 inches, each having a ratio of approximately 0.33. For the surface-strain relief method, a spacing of 3.5 inches was chosen to allow ample space around the strain gage and to allow for use of the LSI device, which had a larger gage length.

5.2 T-beam Models

T-beam models were made to represent the T-beams' specimens tested with the surface-strain relief method. The models looked at the core depth and notch depth found from the

rectangle beam models. These models were similar to the rectangle beams, not including transfer length or shear reinforcement placed in the member.

5.2.1 Model Parameters

The models had the same cross-section properties as the T-beam described in section 3.3. Simply supported beam restraints were applied with a pin end on one end and a roller support on the other. Each T-beam had two 3/8-inch strands represented by stringers with equal area to a 3/8-inch prestressing strand, and an initial stress of 150 ksi was applied to each stringer. Concrete and prestressing steel properties remained the same as the rectangle beams, due to limited information on the properties of the beams at the time of creating the models. The T-beam was partitioned to have a finer mesh around the notches and core with an approximate size of 1/4 inch, with an approximate mesh size of one inch for the rest of the model. Each model contained around 64,000 elements, which consisted of beam elements representing the prestressing steel and structural hex sweep elements for the concrete T-beam. An initial model was created and then three different models were made, one to represent a core perpendicular to the surface of the beam at a depth of one inch, a core that was parallel to the bottom surface with a depth of one inch at the bottom of the core, and a final model consisting of two notches 1.125 inches in depth. Figure 5.8 shows a cross-section of the T-beam with either a notch or core cut into the side and the dimensions.

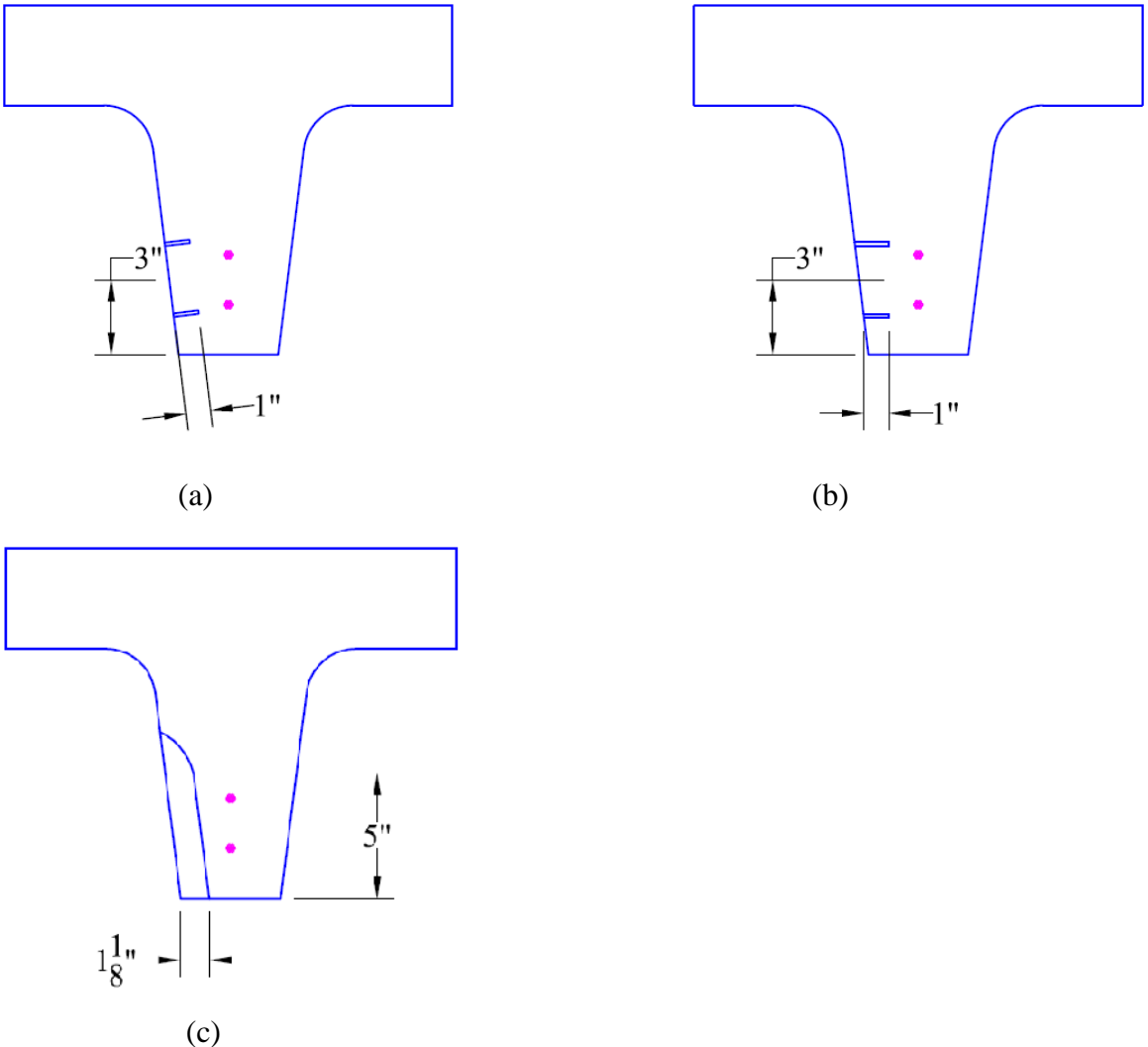


Figure 5.8 a) Core Parallel to Bottom of Beam, b) Core Perpendicular to Web, c) Notch

5.2.2 Results

From results of the finite-element models of the T-beams, it can be seen that optimal depths and notch configurations determined from the other finite-element models will also apply to the T-beam and provide an acceptable relief stresses. Table 5.5 shows the stresses that remain on the surface of the core or notch, and what percentage of stress is relieved compared to the applied prestressing force. Two core models compared effects of the direction of the core, one core being parallel to the base of the beam or perpendicular to the prestressing plane, and the second core perpendicular to the web of the beam. The core parallel to the bottom of the beam showed that 103% of the stress had been relieved, which was very close to the rectangle beam

model of a core to a depth of one inch. The core parallel to the base had a complete relief of stress and introduced some bending stress into the surface of the core. The core perpendicular to the web had a similar relief of stress as the parallel core, as shown in figure 5.9, showing that the direction of the core is not as important as the depth of the core. The notch model provided similar results as the other models, with slight over-prediction of the relieved stress. In order to create one method acceptable to all shapes and configurations, the depths and notch configurations developed for the rectangle beams are within 10% of the full relaxation on the surface of the T-beam.

Table 5.5 T-Beam Calculated Stresses

Method	Simpson's Rule Calculated Stress (psi)	% Relieved Stress
Core Parallel	20.53	103%
Core Perpendicular	-23.22	97%
Notch	64.85	109%

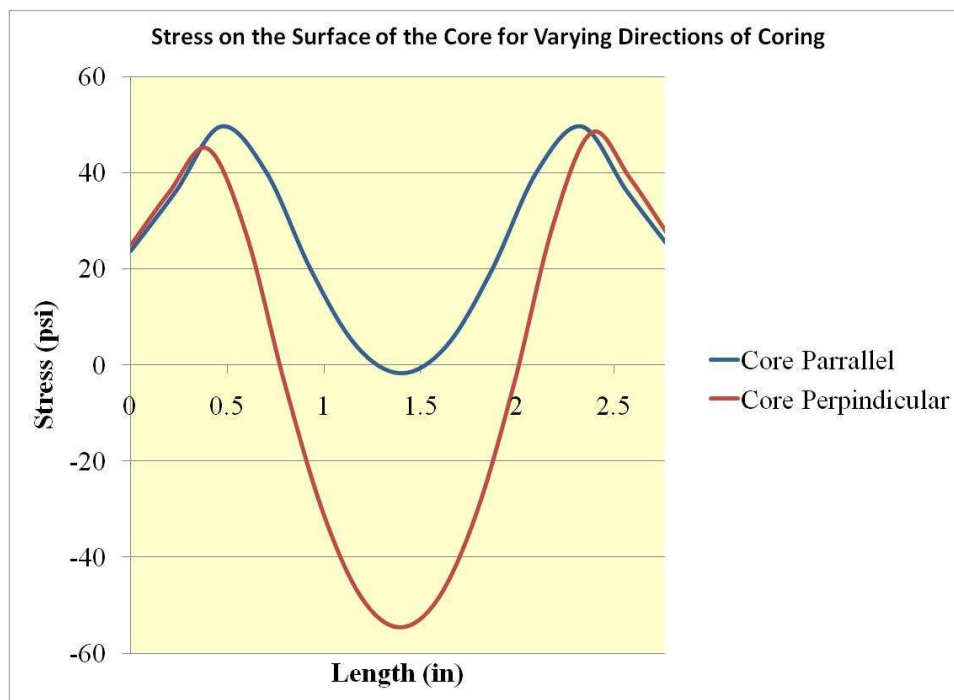


Figure 5.9 Surface Stress Comparing Direction of Core

Chapter 6 - Determining the Average Prestress Force

The surface-strain relief method calculates average prestress force from the change in surface strain. To determine accuracy of the method, average prestress force must be known. Multiple methods were used to calculate average prestress force, including calculation of losses, measuring losses, and a crack-opening procedure. First a series of calculations were used to estimate prestress losses based on the PCI Design Handbook and ACI 318-08. Calculation of losses is a conservative estimate and serves as a reference to determine an approximate prestress force after losses. To get an accurate measurement, average prestress force was calculated from experimental results, using a method similar to a method used by Larson, Peterman, and Rasheed (2005) and also by Pessiki, Kaczinski, and Wescott (1996). Losses were also measured through use of a Whittemore gage at the mid-span of the beams cast at K-State. This was determined to be the most accurate way to measure losses of the rectangle beams.

6.1 ACI Loss Calculations

The purpose of this research project was not to measure the losses of prestress members but to determine the remaining prestress force in a member for comparison purposes to the method of surface-strain relief. Losses were calculated based on ACI 318-08 and the PCI Handbook only to serve as a check that average prestress force (f_{se}) calculated from experimental procedures was in the expected range based on the expected losses. Losses due to creep, shrinkage, relaxation of the tendons, and elastic shorting were all considered and individual losses for each beam were calculated. Effective stress in the prestressing steel after losses for the first set of beams was 130 ksi and for the second set of beams was 122 ksi. The T-beam average prestressing stress after losses was determined to be 167 ksi.

6.2 Use of Whittemore Gage to Determine Losses

To measure the losses of the beam, a Whittemore gage was used. The gage measures the deviation between two points from its set gage length of eight inches. The deviation distance is measured by a dial gage with an accuracy of 0.0001 inch. For the rectangle beams cast at K-State, two brass points were cast into the side of each beam eight inches apart. Initial measurements were taken before de-tensioning the beam and once again immediately after de-

tensioning. Comparing the initial measurement to the de-tensioning measurement, the initial losses can be calculated by computing the change in length between the two measurements and dividing by the gage length to convert to a strain. Due to the nature of concrete, the modulus of elasticity is not linear during the curing process; therefore the strain measured by the Whittemore gage is compared to the relaxation of the strand which has a constant modulus of elasticity up to the point of yield. The prestressing steel was tensioned to 75% of the ultimate strength, therefore the prestressing steel can be assumed to have a constant modulus. To determine the long-term losses and total losses at the time of testing the surface-strain relief method, measurements were taken before coring to calculate the losses at the time of coring.

The surface-strain relief method calculates the prestressing force and not the losses. So in order to calculate prestressing force, initial stresses of each strand were needed. Load cells were positioned on each strand throughout the casting process to measure the stresses in each strand. Before de-tensioning, the load in each strand was recorded and assumed as the initial force in each strand. Losses measured from the Whittemore gage were then subtracted from this initial stress in the strand. For the beams cast in the laboratory, this was assumed to be the most accurate method of determining average prestressing force in each beam and was used as a benchmark when determining the accuracy of the crack-opening method.

6.3 Crack-Opening Method to Determine the Average Prestress Force

To accurately calculate f_{se} of each beam tested using the surface-strain relief method, a combination of procedures used by Larson, Peterman, and Rasheed (2005), and Pessiki, Kaczinski, and Wescott (1996) was used. Each beam was initially loaded past the calculated mid-span cracking moment, instrumented with displacement transducers, and then loaded past the cracking moment for an additional 25 cycles. Unlike the two methods researched, the displacement transducers were positioned at the height of the strand and mounted on the side of the beam. This allowed the crack width to be measured at the level of the strand rather than the base of the beam. With the displacement transducers mounted on the side, the force required to open the crack and produce zero concrete tension near the strand could be found.

6.3.1 Crack-Opening Method Setup

The beams were loaded in a three-point bending setup using a hydraulic servo-controlled actuator shown in figure 6.1. At each end of the beam, a steel-bearing plate was positioned on a concrete-bearing block and one was positioned on the bottom side of the beam using a high-strength gypsum cement to fill in any voids between the bearing plate and the concrete surface. Between the two bearing plates, a 1.5-inch roller was used to prevent the horizontal restraint at the beams ends. At mid-span, a four-inch-wide bearing plate was attached to the top surface of the beam using high-strength gypsum cement to fill in the voids on the rough concrete surface. A one-inch steel roller was positioned between the bearing plate and the hydraulic actuator. Two, LVDTs were positioned at the mid-span, mounted above the beam, and attached to the top bearing plate to measure the deflection of the beam shown in figure 6.2. Two additional ½-inch LVDTs were mounted on the side of beam, see figure 6.3, at mid-span using the 3/8-inch bolts cast into the beam to measure the crack width. Each beam was initially loaded to 40% past the calculated cracking moment to create a visible crack. The load was held for one minute to mark the location of the crack, and the beam was unloaded to 100 pounds. The beam was then loaded to the same maximum applied load as initially, at a rate of 3500 pounds per minute, and unloaded at the same rate for a total of 25 cycles. For the rectangle beams, each was loaded to the maximum applied load of 14,000 lbs and the T-beam was loaded to 9000 lbs. Deflection, load, actuator displacement, crack width, and time data were collected at two hertz throughout all cycles.

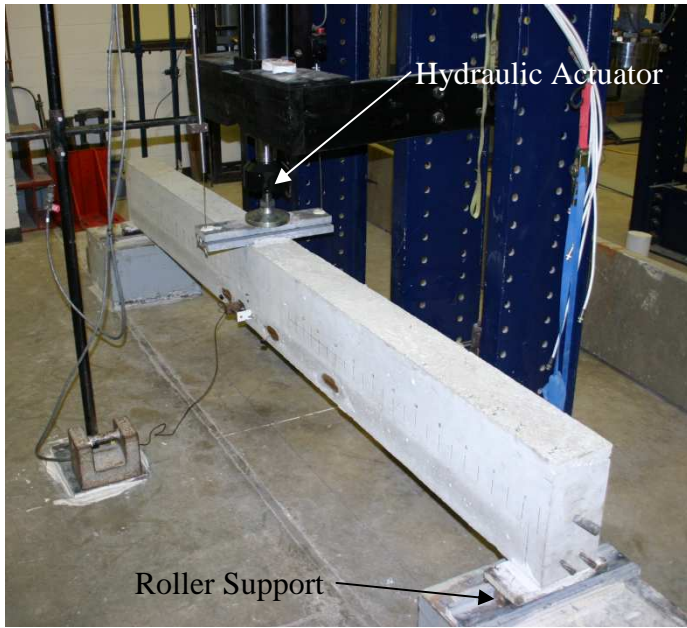


Figure 6.1 Beam Setup

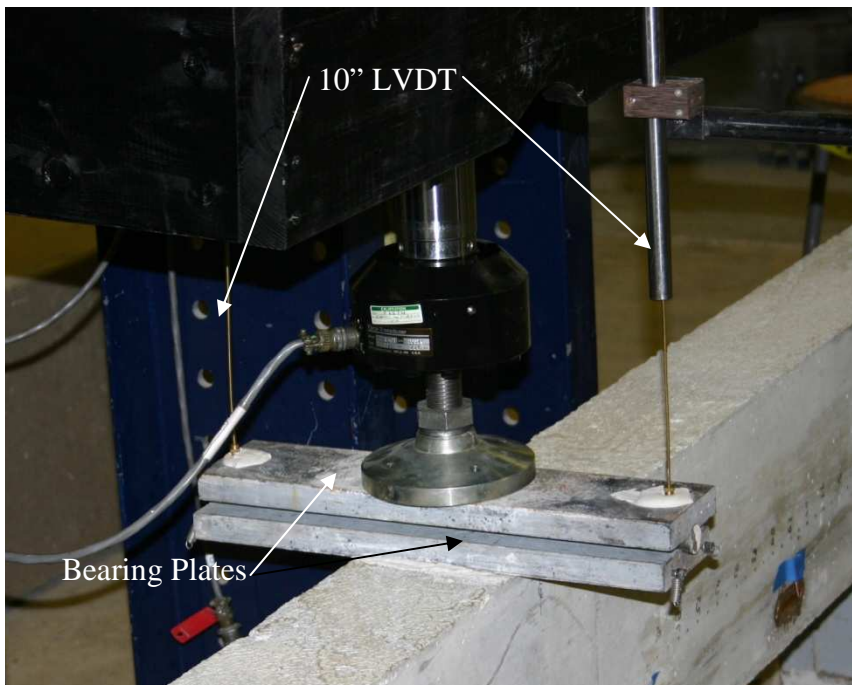


Figure 6.2 Deflection Measurement Setup



Figure 6.3 LVDT mounted to measure crack width

6.3.2 Analysis of Crack-Opening Data

Data from each beam was separated into individual cycles so the cracking moment for each cycle could be found. From the data, the modulus of elasticity was calculated using load versus deflection for relating relief strains to stresses. To find the crack opening or decompression load, multiple methods were analyzed including the end of linearity and a double line method. The double-line method takes into consideration the bilinear response of the load versus crack opening.

Using the initial loading, which cracked the beam, and the first cycle data, the modulus of elasticity was calculated using the applied load and mid-span deflection. The data was examined up to 50% of the cracking moment to insure the crack had not yet formed, which would reduce the cross section and would create a crack section and a varying moment of inertia. Assuming the load is applied similar to a point load, the modulus of elasticity can be found by solving for the modulus of elasticity in the following equation for the deflection of a simply supported beam:

$$\delta = \frac{-PL^3}{48EI} \tag{6.1}$$

where

δ = mid-span deflection (in),

P = applied load (lbs),

L = clear span between supports (in),

E = modulus of elasticity (ksi), and

I = moment of inertia (in^4).

Using the average measured deflection and the applied load, the modulus of elasticity was solved for each load and averaged throughout the cycle to find the modulus of the beam. Initial loading and the first cycle were used because once the beam has been repeatedly cracked it loses some stiffness, resulting in a smaller modulus of elasticity. When using the applied load and deflection to find the modulus of elasticity, the modulus of the entire beam is found and not the modulus of the concrete, so the cyclic loading on the beam reduces the overall stiffness of the beam resulting in a lower measured beam modulus of elasticity. The initial loading of the beam had not been cracked, so the beam can be considered a representation for the concrete modulus of elasticity. The modulus was calculated to be used in conjunction with the surface-strain relief method, to relate the measured strain to the residual stress.

The data, applied load versus the crack width, was plotted for each cycle, and a bilinear response was seen, as in figure 6.4. To calculate the average prestress force, the cycles were each evaluated using two methods—looking at both the bilinear response and at the end of linearity. The double-line method uses the bilinear response to fit two linear regression lines before the crack opens, and then after the crack is fully open. The point where these two lines cross is equal to the load that is required to first open the crack. Pessiki, Kaczinski, and Wescott used this method to determine the decompression load when strain gages were used as the displacement measurement device. The decompression results were found to be repeatable and vary no more than three to 5% (1996).

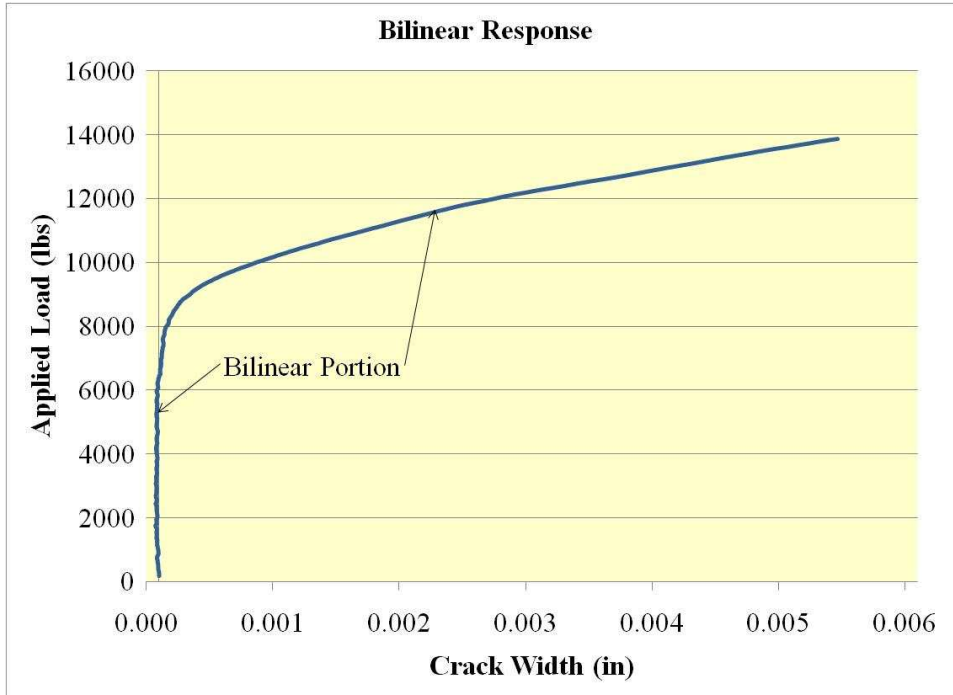


Figure 6.4 Graph of Bilinear Response

Two bilinear portions of the graph were looked at—zero to 7,000 lbs and 11,000 to 14,000 lbs for the rectangle beams, and zero to 3,000 lbs and 5,000 to 9,000 lbs for the T-beams. The initial portion of the graph was linear up until the crack opened, and the second portion was linear once that crack was fully opened. To fit a line of best fit to these linear portions, the slope and the y-intercept were calculated using the following linear regression equations:

$$m = \frac{n \sum(xy) - \sum x \sum y}{n \sum(x^2) - (\sum x)^2} \quad (6.2)$$

$$b = \frac{\sum y - m \sum x}{n} \quad (6.3)$$

where

m = slope of the line,

b = y-intercept,

n = number of data elements considered,

x = crack width data, and

y = applied load data

Figure 6.5 shows the plot of each linear line and the point of intersection, which was examined to be the point of the decompression load. To ensure the portions were linear, the correlation coefficient was calculated for each portion.

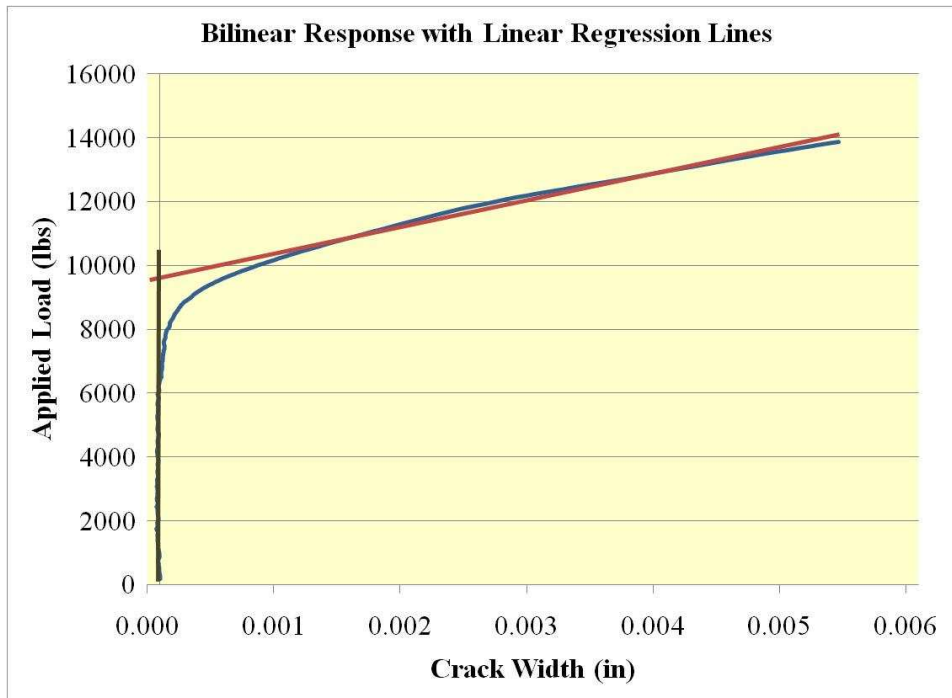


Figure 6.5 Linear Regression Lines Plotted on Graph

The next method was to determine the end of linearity; the same procedure was followed to create the linear regression line from zero to 7,000 lbs for the rectangle beams and from zero to 3,000 lbs for the T-beams. Using the equation of the regression line, a predicted crack width was calculated based on the applied load. To determine the end of linearity, multiple methods were evaluated. One way was to determine a range when the end of linearity occurred. A visible inspection was used to give a rough value of where the end of linearity occurred. The second method looked at the amount of deviation between the predicted crack width based on the regression line and the actual measured crack width. The point when the predicted crack width differed from the actual crack width by more than 0.0002 inches was considered to be the end of

linearity. This difference was well within the resolution of the 16-bit data acquisition system and the ¼-inch LVDT that was measuring the crack width.

Both methods showed similar decompression loads for all cycles, with the maximum decompression load occurring on the first cycle and the least decompression load occurring on the 25th cycle. The decrease in load can be attributed to the bond being broken around the strand at the location of the crack. With the bond broken, the friction between the strand and the concrete was reduced, therefore requiring less force to open the crack. Following Larson, cycles one through 10 were considered for determining the crack-opening moment (2002). Table 6.1 shows the decompression loads for both the double-line method and the end of linearity with the first 10 cycles recorded, and then every five cycles after that. After the tenth cycle, minimal change can be seen in the applied load required to open the crack. Once all the data were plotted, the load at the intersection point was recorded along with the load at which the end of linearity occurs. Once all the data were analyzed, the extreme values were excluded and an average applied load was determined. An average load was determined for each method and then the average prestressing force was calculated.

Table 6.1 Applied Loads to Open Crack

Cycle	Applied Load (lbs)	
	Double Line Method	End of Linearity
1	10000	9200
2	10000	9000
3	10000	9000
4	9800	8800
5	9800	8750
6	9800	8700
7	9750	8650
8	9700	8650
9	9650	8600
10	9650	8600
15	9600	8600
20	9500	8600
25	9500	8550
Average	9729	8535

To calculate average prestress force for each beam, the cracking moment was first calculated from the average applied load, which resulted in zero concrete tension across the crack. Average prestress force was calculated from the cracking moment of each beam as follows, by solving for the average prestress force:

$$M_{CR} = \frac{I}{y} \left[\frac{P}{A} + \frac{Pe y}{I} + f_r \right] \tag{6.4}$$

where

M_{CR} = cracking moment (lb –in),

I = section moment of inertia (in⁴),

P = average prestress force (lbs),

A = area of concrete (in²),

y = distance from neutral axis (in),

e = eccentricity (in), and

f_r = modulus of rupture (psi).

The LVDT measured the width of the crack two inches from the bottom of the beam, or at the height of the strand, so once the crack started to open at the LVDT, a crack was already present from the bottom of the beam. To account for this crack, cracked transformed section properties were used. The modulus of rupture was assumed to be zero since a crack former was embedded at mid-span in each beam and prevented the transfer of any tensile stress in the concrete. Once the average prestress force was calculated, the f_{se} was calculated, to be compared to the other methods that were used to find f_{se} .

6.4 Results

Data gathered from measuring the losses using the Whittemore gage employed the most direct method to determine f_{se} in each of the rectangle beams. Average prestress stress measured from the Whittemore gage can be found in table 6.2. Beams 1 and 2 were cast in series along with beams 3 and 4, which show similar values when compared to each other. These values were used as a benchmark to determine the accuracy of the crack-opening procedure, and to determine a method to increase the accuracy of the method so f_{se} could be found for the T-beams. Table 6.3 shows the results from finding f_{se} based on the two different methods, the double-line method and the end of linearity for the first 10 cycles of beam 2. For the other three beams, table 6.4 summarizes f_{se} for each method.

Table 6.2 f_{se} Based on Losses

Beam	f_{se} (ksi)
1a	134.8
1b	135.0
2a	114.5
2b	98.0

Table 6.3 Results of Crack-Opening Procedure for Beam 2

Cycle	End of Linearity Method					Double Line Method			
	P _{co-End} * (lbs)	M _L (k-in)	P _e (lbs)	f _{se} (ksi)		P _{co-End} * (lbs)	M _L (k-in)	P _e (lbs)	f _{se} (ksi)
1	9200	276.0	41084	134.3		10000	300.0	44657	145.9
2	9000	270.0	40191	131.3		10000	300.0	44657	145.9
3	9000	270.0	40191	131.3		10000	300.0	44657	145.9
4	8800	264.0	39298	128.4		9800	294.0	43764	143.0
5	8750	262.5	39075	127.7		9800	294.0	43764	143.0
6	8700	261.0	38851	127.0		9800	294.0	43764	143.0
7	8650	259.5	38628	126.2		9750	292.5	43540	142.3
8	8650	259.5	38628	126.2		9700	291.0	43317	141.6
9	8600	258.0	38405	125.5		9650	289.5	43094	140.8
10	8600	258.0	38405	125.5		9650	289.5	43094	140.8
Average	8750	262.5	39075	127.7		9794	293.8	43739	142.9

*P_{co-End} = Applied load to initiate a crack

Table 6.4 Summary of Crack-Opening Procedure

Beam	Average of End of Linearity Method				Average Double Line Method		
	P _{co-End} * (lbs)	M _L (k-in)	f _{se} (ksi)		P _{co-End} * (lbs)	M _L (k-in)	f _{se} (ksi)
1a	9150	274.5	135.4		10300	309.0	152.0
1b	8750	262.5	127.7		9800	294.0	142.9
2a	7600	228.0	111.6		9200	276.0	133.8
2b	6200	186.0	92.6		8250	247.5	120.7

*P_{co-End} = Applied load to initiate a crack

To compare all the methods, table 6.5 was created. Beams 1a and 1b were cast together along with beams 2a and 2b. Beams 1a and 1b were almost identical in terms of f_{se} , whereas beams 2a and 2b showed some differences. The reason for the discrepancy was not determined, but was determined that it was not in the measurement of losses due to all methods showing this discrepancy. The measured losses were within the ACI calculated losses, providing confidence that the measured losses were accurate. All beams tested were within 4% of the calculated losses, except beam 2b where the measured losses were significantly lower than the calculated losses. When looking at the crack-opening procedure methods, the end of linearity, and the double-line method, the end of linearity was within 6% and usually under-predicted, with beam

1a being the only beam that calculated a greater stress than the measured losses. The double-line method consistently found f_{se} to be greater than the actual stress by an average of 15%.

Table 6.5 Summary of All Stress Determination Methods

	Calculated f_{se} base on (ksi):			
Beam	Measured Losses	ACI Calculated Losses	End of Linearity	Double Line
1a	134.8	130.0	135.4	152.0
1b	135.0	130.0	127.7	142.9
2a	114.5	117.0	111.6	133.8
2b	98.0	117.0	92.6	120.7
	Percent Error Based on Measured Losses			
1a		3.6%	-0.4%	-12.8%
1b		3.7%	5.4%	-5.9%
2a		-2.2%	2.5%	-16.9%
2b		-19.4%	5.5%	-23.2%

The end of linearity served as reasonable method to determine f_{se} from the crack-opening procedure. This method would be used on the T-beams to determine the average prestressing force in the two beams tested. Table 6.6 shows f_{se} from the calculated losses based on ACI for each T-beam, and based on the end of linearity and the crack-opening procedure. A larger error is shown between the losses and the crack-opening procedure, but the calculated losses were calculated based off of limited information, the age of the beams was approximately nine years old, and information was not available about whether the beams had been damaged or tested before.

Table 6.6 T-Beam Calculated f_{se}

	Calculated f_{se} base on (ksi):	
T-beam	ACI Calculated Losses	End of Linearity
1	165	129.3
2	165	146

Chapter 7 - Surface-Strain Relief Method Results

Multiple methods were tried on different beams and were related to the calculated average prestress force determined from the measured losses and the crack-opening procedure. Factors influencing the residual stress were also monitored, such as the increase of temperature due to coring, determining the modulus of elasticity, and depth of the notches and core. The results were also compared to the finite-element models to determine if the models represented the specimens so that different beams could easily be modeled to determine the optimum core depth or notch configuration.

7.1 Modulus of Elasticity of the Concrete Beams

The modulus of elasticity calculated from the ASTM C 469 specification was used in all calculations to determine average prestressing force from the method of surface-strain relief with the rectangle beams. Following ASTM C 469 (2002), the modulus of the concrete was found and not the modulus of the entire beam. The modulus determined from the load versus deflection curve showed a lower modulus than ASTM C 469. Determining the modulus from a cylinder is much more feasible, and for a prestress member, the ability to obtain a core from the member would be simpler than loading the member and measuring the deflection over varying loads. For the surface-strain method to be feasible, not only must the method be feasible, but also the method of determining the modulus of elasticity. For an existing structure, the modulus could be determined from a core sample, which would follow the ASTM specification giving similar results to the research conducted for this phase. For the T-beams, the only modulus determined was from the crack-opening procedure. The web of the member was too narrow, along with the mesh reinforcement providing difficulty in obtaining a sample. With the calculated modulus of elasticity from ASTM and the load versus deflection on the rectangle beams, a high level of confidence was found between the two methods. Table 7.1 shows the modulus determined following ASTM and from the load versus deflection. When comparing the ASTM E-chord method and the load versus deflection method, a maximum difference of 300 ksi is seen. ASTM standard rounds the calculated modulus of elasticity to the nearest 50 ksi, so a variance of 300 ksi is fairly insignificant.

Table 7.1 Modulus of Elasticity

	Modulus of Elasticity (ksi)	
Beam	E-Chord Method	Load versus Deflection
1a	3750	3500
1b	3300	3000
2a	3950	3800
2b	3550	3350
T-beam 1	-	3550
T-beam 2	-	3000

7.2 Rectangle Beam Results

To compare multiple methods of coring, notching, and measuring strain, multiple methods were used on each beam. The first set of beams tested, which included beams 1a and 2a, were initially tested with the method of coring around a strain gage. Each beam had multiple cores and/or notches made at different locations along both sides of the beam. Each location was offset from the location on the opposite of the beam so two test locations would not line up, which would reduce the cross-sectional area at that location. A reduced cross-sectional area would result in an increase in measured strain and affect the accuracy of the measurement. Beam 1a only used the coring method and was tested three month after the beam was cast. Beams 1b, 2a, and 2b used a combination of both methods, cores and notches, and also used both strain gages and the LSI device. Beam 2a was tested one month after casting, while beams 1b and 2b were tested about 10 months after the beam was cast. Overall, the cores showed a larger release of strain without measuring a tensile stress across the core, which over-calculates the amount of prestressing force in the beam.

7.2.1 Core Results

The first beam cored was beam 1a, and four gages were successfully cored. Due to tight tolerances between the strain gage and edge of the core, one gage was damaged while coring and another gage experienced substantial drift during the process. Table 7.2 shows the measured strains on beam 1a at a 0.75-inch depth and one-inch depth, along with the percent error when compared to the theoretical strain measurement calculated from the measured losses and the experimental decompression load. The cores were taken at various locations along each side of

the beam. The surface-strain relief method gave consistent results on beam 1a at the varying depths, as with the other beams. Two cores were cored in the side of beam 1b and showed similar results as with beam 1a; the remaining locations on the beam were used to test other methods of relieving strain. Table 7.3 shows the relieved strain at a depth of 0.75 and one inch for beam 1b.

Table 7.2 Measured Strains on Beam 1a Using the Coring Procedure

Core	Theoretical ($\mu\epsilon$)	3/4" Depth ($\mu\epsilon$)	3/4" Percent Error	1" Depth ($\mu\epsilon$)	1" Percent Error
1	330	301	8.8%	314	4.8%
2	331	298	10.0%	328	0.9%
3	329	325	1.2%	361	-9.7%
4	331	297	10.3%	332	-0.3%

Table 7.3 Measured Strains on Beam 1b Using the Coring Procedure

Core	Theoretical ($\mu\epsilon$)	3/4" Depth ($\mu\epsilon$)	3/4" Percent Error	1" Depth ($\mu\epsilon$)	1" Percent Error
1	381	279	26.8%	351	7.9%
2	381	309	18.9%	390	-2.4%

The next set of beams, 2a and 2b, had similar amounts of cores taken out of each. The first beam in the set cored was beam 2a and it had three cores tested on one side and two on the other. Table 7.4 shows results from the coring procedure. Similar results were found when compared to the first set of beams cored. Four cores were taken from beam 2b, shown in table 7.5, with the second core being damaged during the incremental depth increase from 0.75 to one inch.

Table 7.4 Measured Strains on Beam 2a Using the Core Procedure

Core	Theoretical ($\mu\epsilon$)	3/4" Depth ($\mu\epsilon$)	3/4" Percent Error	1" Depth ($\mu\epsilon$)	1" Percent Error
1	269	240	10.8%	290	-7.8%
2	268	220	17.9%	254	5.2%
3	268	250	6.7%	300	-11.9%
4	268	261	2.6%	290	-8.2%
5	269	224	16.7%	247	8.2%

Table 7.5 Measured Strains on Beam 2b Using the Core Procedure

Core	Theoretical ($\mu\epsilon$)	3/4" Depth ($\mu\epsilon$)	3/4" Percent Error	1" Depth ($\mu\epsilon$)	1" Percent Error
1	266	184	30.8%	235	11.7%
2	268	236	11.9%	-	-
3	266	197	25.9%	219	17.7%
4	268	273	-1.9%	278	-3.7%

As shown in the previous tables, the measured strains were all consistent with the theoretical strains. Next, relieved strains were used to find the average prestress force at each core location, then an average was taken for each beam. Average prestress force calculated from the surface-strain relief method was then compared to the average prestress force determined from the measurement of losses and or the decompression load. Table 7.6 shows results of the coring method on all four beams. At a core depth of 0.75 inch, larger errors are present and vary from 7% to 24%. At a depth of core of one inch, much less error exists with all the beams having an error of less than 10% when compared to the experimentally determined f_{se} .

Table 7.6 Calculated f_{se} and Percent Error for the Core Method

Beam	Experimentally Determined f_{se} (ksi)	3/4" Core Depth Calculated f_{se} (ksi)	Percent Error	1" Core Depth Calculated f_{se} (ksi)	Percent Error
1a	134.8	125.1	7.2%	136.4	-1.2%
1b	135.0	103.2	23.6%	128.9	4.5%
2a	114.0	101	11.4%	116.4	-2.1%
2b	98.0	83.1	15.2%	90.4	7.8%

Beams 1a and 1b were cast together in the same prestressing bed, along with beams 2a and 2b. Theoretically beams 1a and 1b, and 2a and 2b should have the same average prestressing force, so by testing one beam within the first three months after casting, and then testing the second beam at a minimum of six months after casting, the effects of creep and shrinkage on the relieved strain could be examined. When comparing beams 1a and 1b and beams 2a and 2b, the average error varies from initially measuring a larger relief strain to measuring less than a full relief. Beams 1b and 2b show a larger error than beams 1a and 2a, suggesting that some time-dependent losses such as creep and shrinkage of the concrete may not be easily measured using the surface-strain relief method.

7.2.2 Notch Results

Beams 1b, 2a, and 2b tested the method of the nothing procedure to compare the results to the finite-element models and compare the LSI device to the linear electrical-resistance strain gage. Beams 1b and 2b tested both the LSI device and strain gages on each beam, and results are shown in tables 7.7 and 7.8. Results for both methods are much more varied than the core method. When comparing the strain gage to the LSI device, the LSI device provided more accurate results. One explanation for this is the LSI device measured over a larger surface and measured close to the edge of the notch, which captured both tensile and compressive stresses between the notches, as seen with the finite-element models. The strain gage had a smaller gage length and did not capture the strain over the entire surface. Beam 2a only used the LSI device to measure the strain relief from the notching procedure, as shown in table 7.9. Overall, the LSI device showed that 1.25 inches generally measures a resultant tensile strain on average 20% larger than the theoretical strain. The one-inch-depth errors were much closer to a full relaxation, with errors around 10 to 15% less than the actual prestress force.

Table 7.7 Measured Strains on Beam 1b Using the Notch Procedure

Notch	Theoretical ($\mu\epsilon$)	1" Depth ($\mu\epsilon$)	1" Percent Error	1.25" Depth ($\mu\epsilon$)	1.25" Percent Error
1	383	236	38.4%	323	15.7%
2	383	200	47.8%	248	35.2%
*3	382	310	18.8%	369	3.4%
*4	384	293	23.7%	311	19.0%

* Used LSI device to measure strain

Table 7.8 Measured Strains on Beam 2b Using the Notch Procedure

Notch	Theoretical ($\mu\epsilon$)	1" Depth ($\mu\epsilon$)	1" Percent Error	1.25" Depth ($\mu\epsilon$)	1.25" Percent Error
1	266	283	-6.4%	305	-14.7%
2	266	327	-22.9%	352	-32.3%
*3	268	240	10.4%	302	-12.7%

* Used LSI device to measure strain

Table 7.9 Measured Strains on Beam 2a Using the Notch Procedure

Notch	Theoretical ($\mu\epsilon$)	1" Depth ($\mu\epsilon$)	1" Percent Error	1.25" Depth ($\mu\epsilon$)	1.25" Percent Error
*1	268	288	-7.5%	316	-17.9%
*2	268	303	-13.1%	323	-20.5%

* Used LSI device to measure strain

To calculate the average error for the strain gage and the LSI device, at the two depths of one and 1.25 inches, each notch location of the average prestress force was calculated and compared to the experimental prestress force as shown in table 7.10. Results varied from beam to beam, but overall the strain gages had larger errors at the depth of one and 1.25 inches when compared to the results obtained from the LSI device.

Table 7.10 Calculated f_{se} and Percent Error for the Notching Method

Beam	Experimentally Determined f_{se} (ksi)	1" Notch Depth Calculated f_{se} (ksi)	Percent Error	1.25" Notch Depth Calculated f_{se} (ksi)	Percent Error
1b	134.8	79.2	41.2%	101.8	24.5%
*1b	134.8	107.6	20.2%	120.6	10.5%
*2a	114.0	125.6	-10.2%	135.4	-18.8%
2b	98.0	106.4	-8.6%	119.1	-21.5%
*2b	98.0	89.8	8.4%	109.7	-11.9%

*Used LSI device to measure strain

7.3 T-Beam Results

Two T-beams were tested, T-beam 1 and 2, and were approximately nine years old at the time of testing. Similar to the rectangle beams tested, the initial beam (T-beam 1) was tested using the coring method, and then with T-beam 2, both methods were used, coring and notching. T-beam 1 was successfully cored at four various locations, and at two locations the gages were damaged while trying to core around them due to the tapered web, causing the core bit to shift and tear the edge of the strain gage. T-beam 2 successfully cored around four strain gages and tested the notching procedure at five locations. As with the rectangle beams, the cores provided more precise and accurate results on the T-beams.

7.3.1 Core Results

Tables 7.11 and 7.12 show results of each core and incremental depth. A depth of 0.75 inches shows a full relaxation of the core is not achieved, but at a depth of one inch, the error is less than 10%. On T-beam 2, larger errors existed on cores three and four, showing errors of 50% at a depth of one inch. No other core showed this kind of error, so each core was broken out to investigate the reason behind the error and to see if any reinforcement was running through the core. Reinforcement was found running through the core at a depth of one inch from the surface of the web. The reinforcement ran vertically through the core as shown in figure 7.1. It was concluded that the presence of the reinforcement significantly affected the relief of strain on the surface of the member. The reinforcement allowed for less than 50% of the strain relief, so neither of these cores were considered in the calculations of the prestressing force as shown in table 7.13.

Table 7.11 Measured Strains on T-Beam 1 Using the Coring Procedure

Core	Theoretical ($\mu\epsilon$)	3/4" Depth ($\mu\epsilon$)	3/4" Percent Error	1" Depth ($\mu\epsilon$)	1" Percent Error
1	118	104	11.9%	123	-4.2%
2	118	101	14.4%	126	-6.8%
3	122	103	15.6%	108	11.5%
4	118	111	5.9%	113	4.2%

Table 7.12 Measured Strains on T-Beam 2 Using the Coring Procedure

Core	Theoretical ($\mu\epsilon$)	3/4" Depth ($\mu\epsilon$)	3/4" Percent Error	1" Depth ($\mu\epsilon$)	1" Percent Error
1	184	171	7.1%	180	2.2%
2	186	117	37.1%	149	19.9%
3	189	58	69.3%	71	62.4%
4	188	61	67.6%	78	58.5%



Figure 7.1 Reinforcement Affecting Strain Relief on the Surface of the Core

Table 7.13 Calculated f_{se} and Percent Error for the Coring Method

Beam	Experimentally Determined f_{se} (ksi)	3/4" Core Depth Calculated f_{se} (ksi)	Percent Error	1" Core Depth Calculated f_{se} (ksi)	Percent Error
T-beam 1	129.3	110.6	14.5%	119.2	7.8%
T-beam 2	146	122.7	16.0%	133.5	8.6%

7.3.2 Notch Results

T-beam 2 was the only beam notched, and both a strain gage and the LSI device were used to measure the relaxation of strain on the surface between the notches. Table 7.14 shows results of the five notch locations. Notches four and five show larger errors than expected at a depth of 1.25 inches, and it is believed the surface was disturbed and the false readings were taken with the LSI device. At a depth of one inch, all gages measuring a relief were within 10% of each other. Average prestress stress is calculated for each method in table 7.15, and excludes notches four and five at a depth on 1.25 inches due to the large error in the measurement. With the LSI device, a notch depth of 1.25 inches and a spacing of 3.5 inches produced a measured relief strain on the surface of 90% of the theoretical value.

Table 7.14 Measured Strains on T-Beam 2 Using the Notching Procedure

Notch	Theoretical ($\mu\epsilon$)	1" Depth ($\mu\epsilon$)	1" Percent Error	1.25" Depth ($\mu\epsilon$)	1.25" Percent Error
1	182	162	11.2%	206	-13.0%
*2	182	144	20.7%	157	13.6%
*3	188	142	24.5%	163	13.4%
*4	183	162	11.5%	328	-79.2%
*5	183	131	28.4%	321	-75.4%

* Used LSI device to measure strain

Table 7.15 Calculated f_{se} and Percent Error for the Coring Method

Beam	Experimentally Determined f_{se} (ksi)	1" Notch Depth Calculated f_{se} (ksi)	Percent Error	1.25" Notch Depth Calculated f_{se} (ksi)	Percent Error
T-beam 2	146	133.1	8.8%	160.9	-10.2%
*T-beam 2	146	122.7	16.0%	131.9	9.7%

* Used LSI device to measure strain

7.4 Summary of Results

The core data shows a greater accuracy and precision when compared to the experimentally determined f_{se} . The coring process reduces stress influences from the surrounding concrete and creates an almost full stress relief with a core depth of one inch. At a depth of one inch, the core always measured a relief strain less than the actual strain, except on the two members tested before a majority of the losses occurred, which showed an average error of 1.7% larger than the actual strain. The T-beam core results are similar to beams 1b and 2b, which were tested after a majority of losses had occurred. When comparing beam sets 1a and 1b, and 2a and 2b, an error exists suggesting that losses due to creep and shrinkage may not be fully relieved. The T-beams shows about a 7% error from the theoretical calculated f_{se} , which is very similar to beams 1b and 2b, which shows an approximate error of 6%.

When comparing the notching procedure between the rectangle beams and the T-beams, a depth of one inch provided the highest level of strain relief without measuring a complete tensile stress between the notches on the rectangle beams. With the T-beam, a depth of 1.25 inches provided the most relaxation between the two notches but still did not create a full relaxation between the two notches. Differences between the two beam results were also seen on the finite-element models, which showed a 10% difference in the relieved stress. Unlike the

coring method, the geometry and prestressing steel configuration affected the relieved stress on the surface between the notches. A core is isolated from the beam on all sides except at the base, where with the notches, only two sides are relieved from the surrounding beam.

The notches provided much more varied results due to the many variables of the method, including notch length, spacing, and depth. For this research, the only variable tested was depth of the notch. From the finite-element models, changing the length or spacing of the notch changed the measured strain significantly. The finite-element models also showed at a given spacing a 0.125-inch increase in depth increased the released strain by 24%, whereas an increase in core depth of 0.25 inches resulted in an 18% increase in released strain. When using the coring method, a slight error in depth of the core will not significantly affect the measured strain and will not introduce a large error, as with the notching method. Using the notching method, the errors were larger than that of the cores, and also much more varied, ranging from -9% to 22%.

7.5 Temperature Effects

When cutting the core, heat was generated from the friction of the diamond coring bit, which caused an increase in temperature. To monitor effects of temperature on the surface-strain relief method, the temperature before and during the process was monitored on multiple trials. The amount of strain drift due to the temperature increase was also calculated based on the supplied data of each packet of strain gages. Table 7.16 shows the average temperature of a core as the surface-strain relief method is used. Initially the temperature was taken, then immediately after each depth, and then again after waiting 10 minute to allow to core to cool. Maximum temperature increase occurred during the initial coring process with a 30 °F increase. This increase was due to the friction between the diamond core bit and the concrete. A maximum temperature was seen during the first core depth because it is the largest continuous incremental depth in the process. Water could be used to minimize the effects, but as other researchers have found, water can induce swelling of the concrete which influences the strain reading. As table 7.17 shows, very minimal strain drift occurs due to temperature. A period of 10 minutes allowed the temperature to decrease and reach equilibrium with the surrounding beam. The strain drift due to temperature was minimal and it took a few minutes for the gage to stabilize due to the

release of strain. Waiting 10 minutes to take the final reading corrected for the temperature error and allowed the gage to stabilize.

Table 7.16 Core Temperatures

Time	Temperature (°F)
Initial	74
3/4" Depth	104
After 10 minute wait	83
1" Depth	94
After 10 minute wait	77

Table 7.17 Increase in Strain Due to Temperature Fluctuations

Temperature Increase (°F)	40	30	20	10
Batch 1 (µε)	10.3	12.3	11.5	7.6
Batch 2 (µε)	24.8	22.5	17.8	10.4

Two different batches of strain gages were purchased, each having different batch numbers, and therefore having different thermal output coefficients. The first batch received had very minimal strain drift occurring due to a thermal change, with a 12 microstrain change due to a 30°F change. With the second batch, a 30°F change resulted in a 22.5 microstrain change. While the strain change was not very large, if unaccounted for, it can cause approximate an error of 10%, which would over-calculate the average prestress force.

Chapter 8 - Conclusions and Further Recommendations

8.1 Conclusions

From data collected from this experimental and analytical study, the following conclusions can be drawn:

- A three-inch core bit paired with a two-inch linear electrical-resistance strain gage provided an almost complete relaxation on the core with errors less than 10%. This method provided the most precision and accuracy among all methods.
- The notching procedure paired with the LSI device provided the quickest and most efficient method to measure residual stresses, and eliminated the need to mount strain gages, which is a time-consuming and tedious task. The notching procedure also produced the most variance in the readings and the notch spacing, depth, and length seemed dependent on member geometry and strand configuration.
- A spacing of 3.5 inches between notches—a depth of one inch, and one inch past the upper-most prestressing steel—was the optimal configuration for the rectangle beams, producing acceptable results with the T-beam geometry.
- With either method, multiple locations need to be tested and averaged to minimize errors with the method. The core or notch should also be placed in a region of high stress to minimize the effects of errors
- Strain drift due to temperature increase needs to be accounted for, due to the heat generated from the coring process. Allowing the core to reach equilibrium with the surrounding beam, which was found to take 10 minutes, was determined the optimal method to account for the temperature increase. Ten minutes also allowed the strain gage to fully respond and stabilize due to the sudden release of strain.
- Finite-element models predicted the amount of relieved stress within a few percent when compared to the experimental results, showing that finite-element models could be used to determine the optimal method for various geometries and strand configurations.
- When shear reinforcement is used in the construction of the member, precautions must be taken not to measure the relief strain directly over any reinforcement. The reinforcement causes significant errors when encountered in a core or notch, and can affect the measured relief strain by as much as 50%.

8.2 Recommendations

To further this research, the following recommendations are made:

- Develop the LSI device with a shorter gage length to allow the measurement of relief strain inside a three-inch core. This would allow for the elimination of mounting strain gages to the surface, which is time-consuming and tedious. It would also allow for a simple and quick procedure, while still achieving a near full relaxation in the core.
- To achieve a higher level of accuracy with the notching procedure, more finite-element models and laboratory specimens need to be tested to determine depth, spacing, and length that are not so sensitive to small changes in any one or all of these three factors.
- To accurately determine the average prestress force, core or notch one location from each side of the member, and preferable core or notch three locations from each side.
- Test a bridge member in which the losses can be easily calculated through the use of vibrating wire strain gages positioned in the member to monitor long-term losses, and evaluate the procedure for field testing.

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