

AN EXPERIMENTAL INVESTIGATION OF THE CUTTING  
FORCES AND WEAR AREA OF A SINGLE DIAMOND

by

DON HELLAR

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Approved By:

F. C. Appl

Major Professor

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# SYMBOLS USED

$a$	Radius of Diamond
$h_w$	Depth of Cut
$h_{wd}$	Depth of Diamond Wear
$X$	Axial Cutting Force
$Y$	Tangential Cutting Force
$Z$	Normal Cutting Force
$R_{eq}$	Radius of Wear Area (Planimeter)
$R^*$	Radius of Wear Area (Profile)
$A_1$	Wear Area (Planimeter)
$A_2$	Wear Area (Profile)
$\lambda_w$	Diamond Wear Angle

## CHAPTER I

### INTRODUCTION

The use of diamonds as a cutting tool material has a long history. They have long been used in bits by the mining and oil industry for drilling and coring rock formations that are so hard that they cannot be economically drilled or cored by any other means.

Often the costs involved are high. For example, down-time on an offshore drilling rig can cost as much as \$1200 per hour and a large diamond drill bit may cost as much as \$20,000. With costs like this, even a small improvement in design and operation can result in large savings.

The use of diamonds has been rather limited due to the expense of natural diamonds. Only small crystals (suitable for abrasive tools only) have been capable of being produced by synthesis.<sup>1</sup> Thus, it is still necessary to use natural diamonds in some cutting tools, especially oil well drill bits. In general, the cost of diamonds (either natural or synthetic) is high and the supply somewhat limited. Therefore, it is important to learn more about the basic cutting action of diamond tools so that they may be designed and operated more efficiently.

Industry has acquired a certain level of experience in the design of diamond tools, but this has been based mainly on trial and error. Appl, et. al. [1], has developed a theory of diamond cutting action;

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<sup>1</sup>By altering the distance between atoms of a substance when it is under severe compression leads to significant changes in its properties. By using a polymorphic transformation of the crystal structure, the new properties are maintained.

but there is insufficient experimental work to verify the theory. Most previous experimental work deals primarily with metal cutting i.e., Loladze and Bokachava [4] and Keen and Grogan [3].

Reese [6] determined experimentally the cutting forces for a single spherical diamond while cutting Indiana Limestone. Limestone is not very abrasive, and so wear of the diamond was not a factor in these tests. In many applications, however, the life and hence the cutting cost is critically dependent on the wear of the diamonds during operation. Thus, it is important to learn more about the wear of diamonds during cutting.

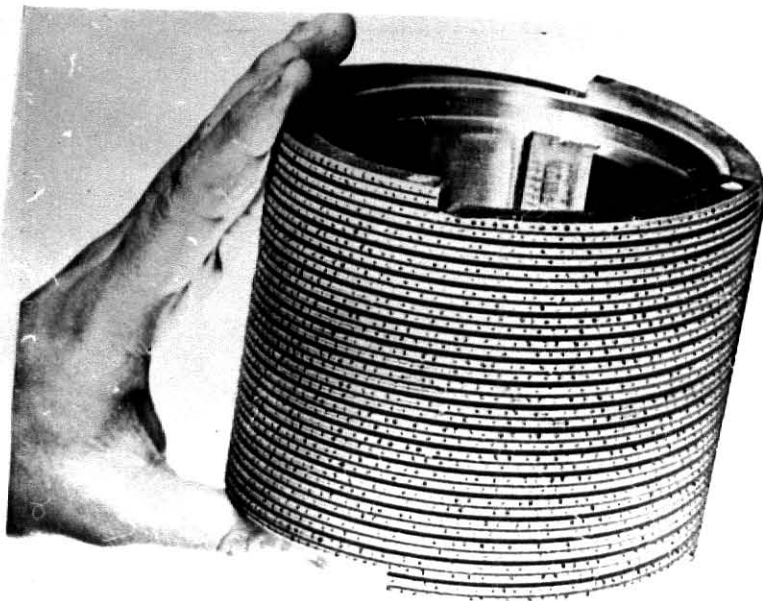
Most industrial tools consist of approximately spherical shaped diamonds held in a metal matrix. Fig.'s 1 and 2 show typical diamond tools. The diamonds usually protrude from the surface and are arranged in some pattern. The cutting action thus depends on the total action of all the individual diamonds. For this reason, a single-point diamond tool was selected to determine the effect of diamond wear on the cutting forces. The cutting action of a worn single-point diamond is shown in Fig. 3.

Recent work by Keen and Grogan [3] has shown that the diamond life or amount of wear is affected considerably by the orientation of the diamond. This work has shown that when the tools were oriented so that the 111 or 110 planes were close to the top face, wear resistance was increased. A check with Sidley Diamond Tool Company, the manufacturer of the tools used, revealed that the 110 plane was oriented toward the top face so this factor was not considered.



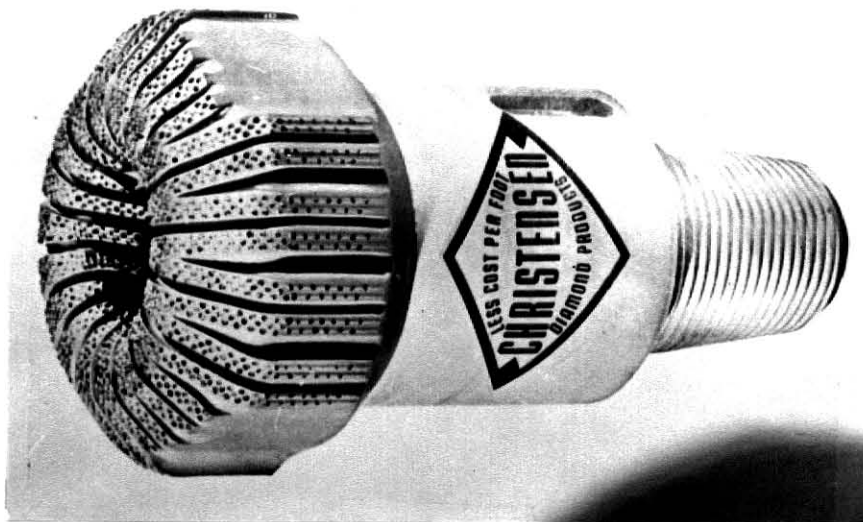
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Typical Diamond Mill Cutter

Figure 1



Typical Petroleum Diamond Bit

Figure 2

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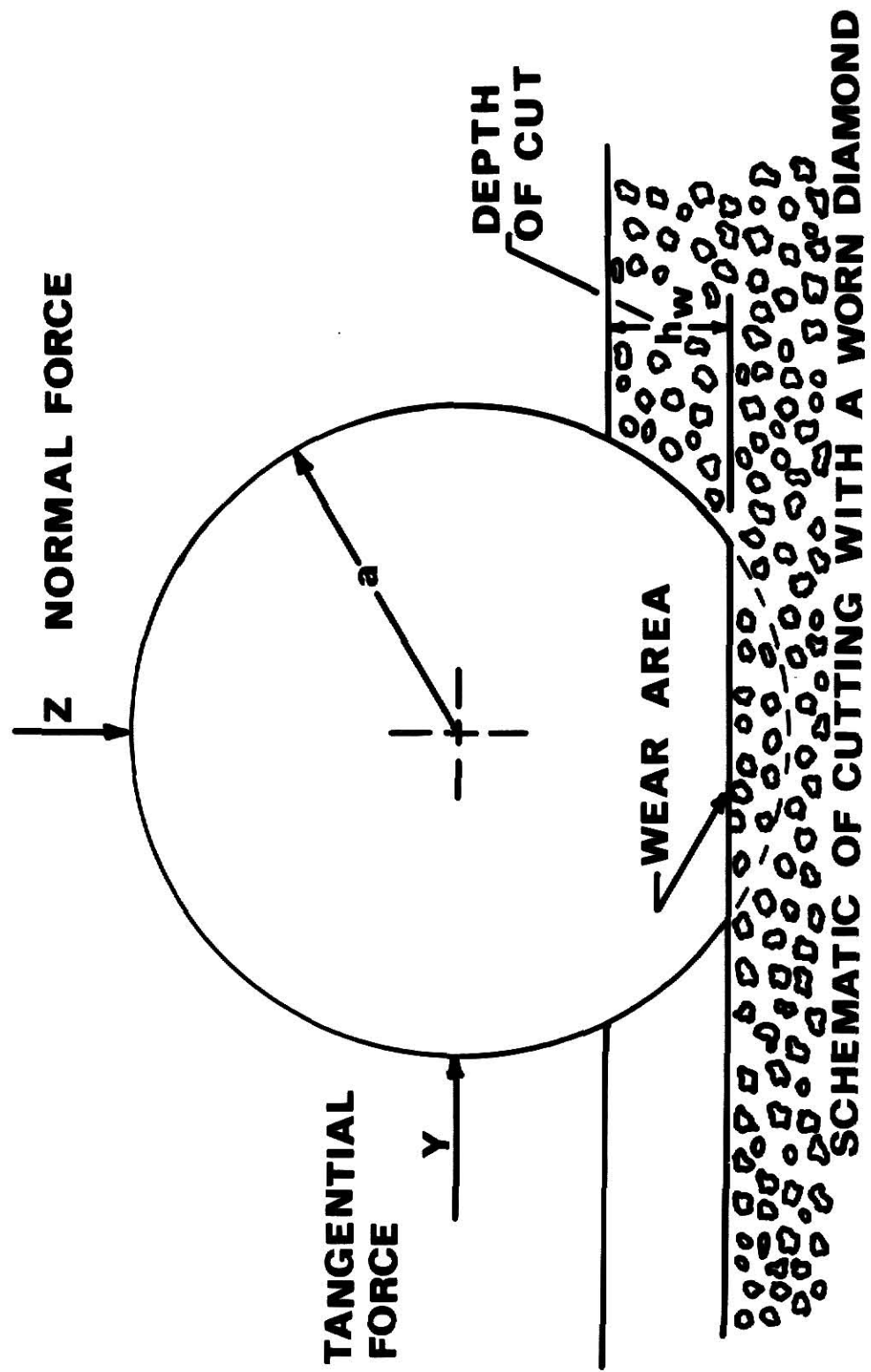


Figure 3

The mechanism which causes the cutting surface of diamonds to wear is not entirely understood. However, those studying wear believe that the principle cause of wear is mechanical in nature. With that assumption, Appl, et. al. [1], has developed a theory for a single diamond. The purpose of this work was to obtain basic experimental data to check the validity of the theory and to obtain information relating to the rate of diamond wear. The experiment consisted of cutting on a cylindrical rock (Georgia granite) mounted in a lathe with a single spherical diamond and measuring the cutting forces.

Periodically the cutting tool was removed and photographed through a microscope to determine the nature and extent of diamond wear.

## CHAPTER II

## DESCRIPTION OF EXPERIMENT

The test set-up consisted of rotating a cylindrical piece of rock in a lathe. A single-point diamond tool was used to cut the rock with the forces acting on the diamond being measured with a specially built dynamometer (Fig. 4). The forces were then recorded on two Sanborn recorders. A constant flow of water was provided to keep the diamond cool and to remove the cuttings.

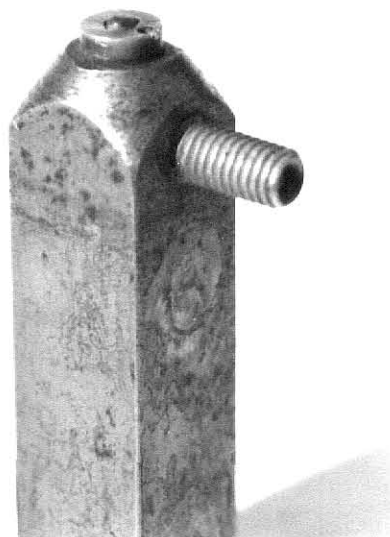
The rock used was Georgia granite. Mandrels were centered and cemented to each end for mounting in the lathe. The rock was cut to a cylinder before any tests were made.

The diamond used was initially spherical, .092 inch in diameter (8 per carat). It was mounted in a metal matrix (Fig. 5) with .040 inch protruding. This matrix was then mounted in the dynamometer.

The dynamometer used was especially designed and built for Reese [6] by Lebow and was used for this experiment with no modifications.

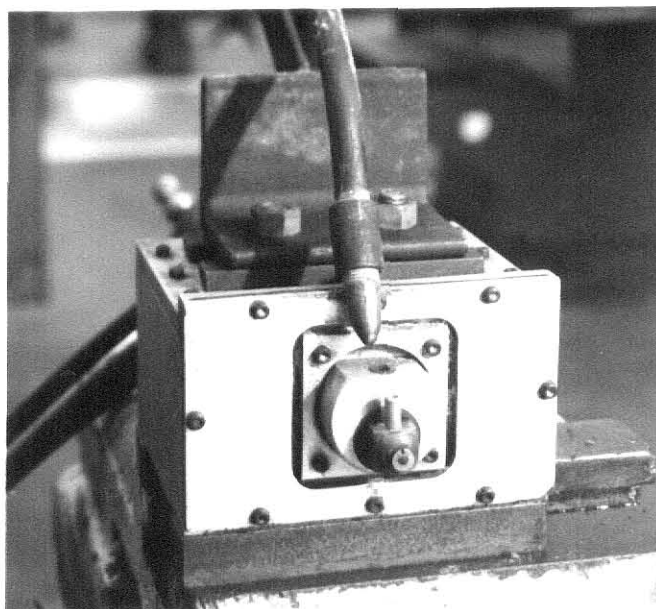
It had a range of 100 pounds in the normal direction and a 50-pound range in the axial and tangential directions. Calibrated resistors could be switched into the strain gage bridge of each direction. These resistors corresponded to a known force. By doing this, the recorders could easily be calibrated. Two channels of one recorder were used to record the normal and tangential forces. The axial force was recorded on a second Sanborn recorder. The test set-up is shown in Fig. 6.

A continuous cut was taken with the forces recorded during the entire cut. In order to find an average force for the entire cut,



Test Diamond in Holder

Figure 5



Test Dynamometer

Figure 4



Test Set-Up

Figure 6

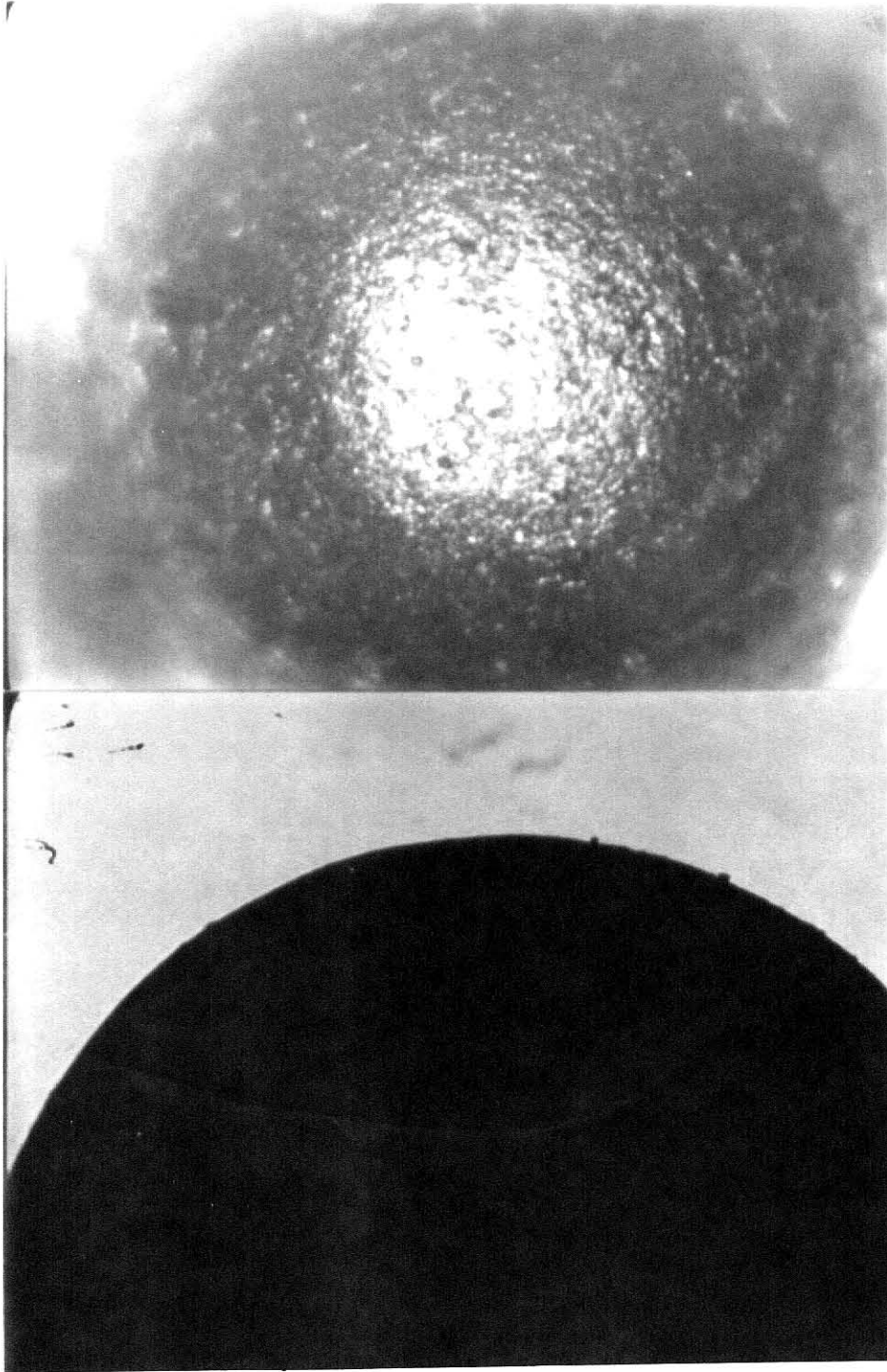


readings were taken in three places from the recordings. One reading was taken at each end and one in the center. The end readings were taken about one inch from the end of the stone so that the measured loads were unaffected by end conditions. These readings were then averaged to give a single reading for each run. After each eight runs, the diamond was removed from the dynamometer and photographed through a microscope. Typical photos are shown in Fig.'s 7, 8 and 9. Finding the area of the diamond flat spot was accomplished by two methods, yielding different areas but following similar trends.

From Fig. 8a, the area of the flat spot could be measured using a planimeter. It was assumed that the flat spots were flat. Otherwise, the entire area would not be in focus at one time. From this reading, the radius of a circle with the same area was determined. By using identities, (appendix 1) the volume of diamond worn away could be determined.

From Fig. 8b, the diameter of the flat spot could be measured. Again, by using identities, the volume of the diamond worn away could be computed.

Computer programs were written for each method and the different measurements were inserted to yield the desired information.

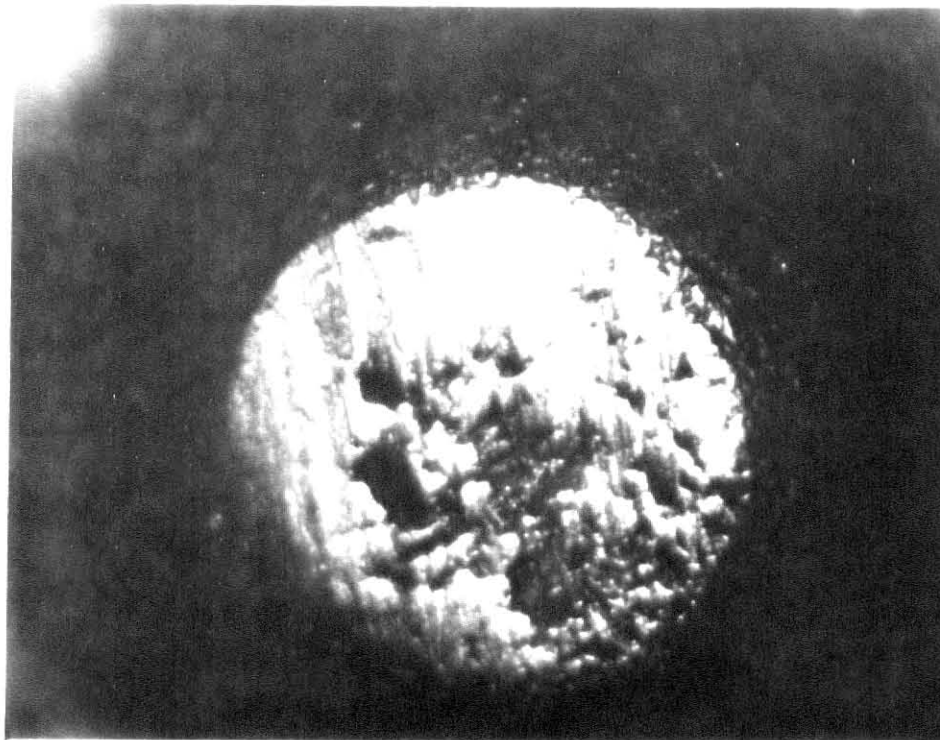


New Test Diamond (X58.6)

Figure 7a

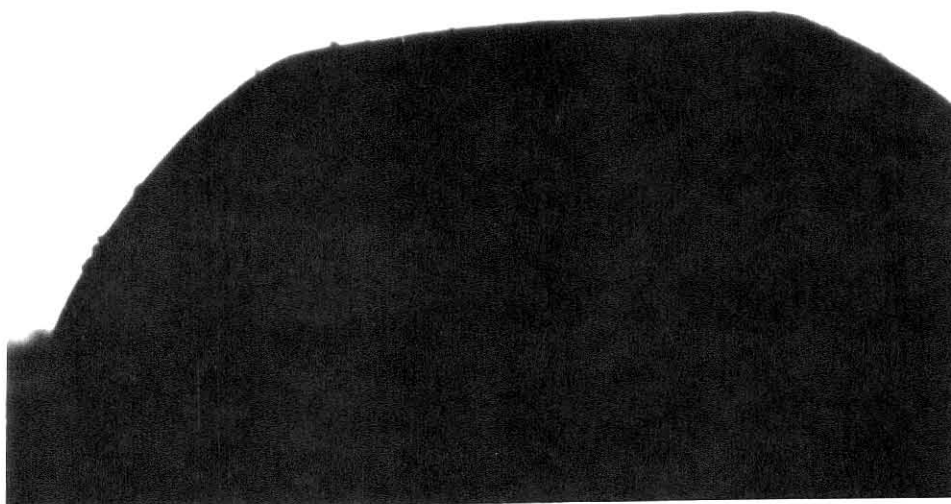
Profile of New Test Diamond (X58.6)

Figure 7b



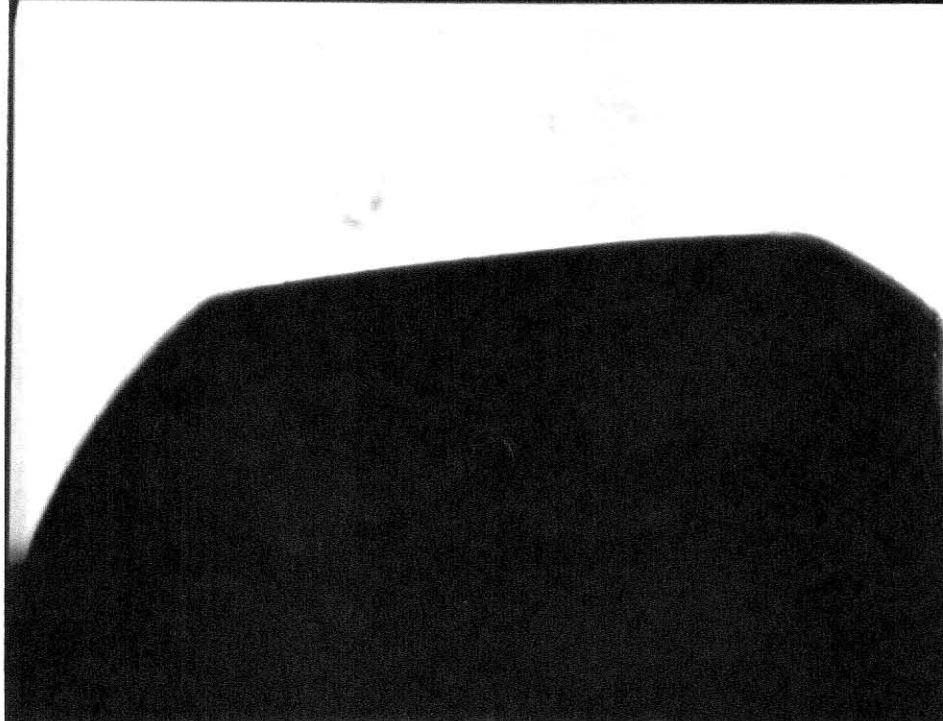
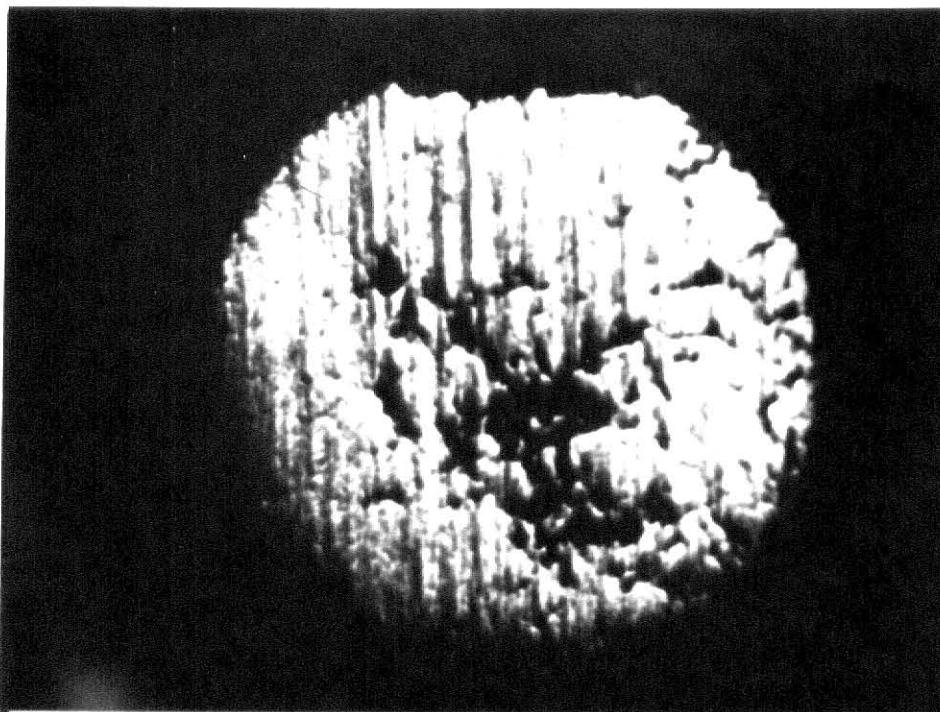
Test Diamond after 40 Runs

Figure 8a



Profile of Test Diamond after 40 Runs

Figure 8b



Test Diamond after 96 Runs

Figure 9a

Profile of Test Diamond after 96 Runs

Figure 9b

### CHAPTER III

#### EXPERIMENTAL PROCEDURE

At the beginning of this experiment, the only cutting speed reference was by Reese. He had used a surface speed of 60 ft. per minute. This was determined to be too slow, as virtually no diamond wear was visible at the end of his test. For the second diamond, a surface speed of 435 ft. per minute was used. This was too fast, as the diamond was greatly worn after three cuts. For the third diamond, a speed of 185 ft. per minute was chosen. This again proved to give very little wear, so for diamond No. 4 a speed of 220 ft. per minute was chosen. This speed was apparently very near the natural frequency of the system as the rock vibrated very badly. The test was discontinued so that the dynamometer would not be damaged. For the final test diamond (No. 5), a beginning surface speed of 173 ft. per minute was used. Due to the fact that the lathe only had fixed speeds of rotation, the surface speed decreased somewhat as the rock became smaller. (See Table 1).

For diamonds No. 3, 4, and 5, a feed of .0025 inch per revolution and for No. 2 a feed of .005 inch was used. A cut depth of .005 inch was used for all diamonds. The cuts were overlapping so that a smooth surface was left after the diamond had passed. Once a new diamond was put into use, all conditions were left the same. The rock diameter was measured after every run.

Diamond Number	RPM	Surface Speed	Feed	Cut
2	212	435	0.005	0.005
3	91	185	0.0025	0.005
4	110	220	0.0025	0.005
5	91	173	0.0025	0.005

## CUTTING CONDITIONS

Table No. 1

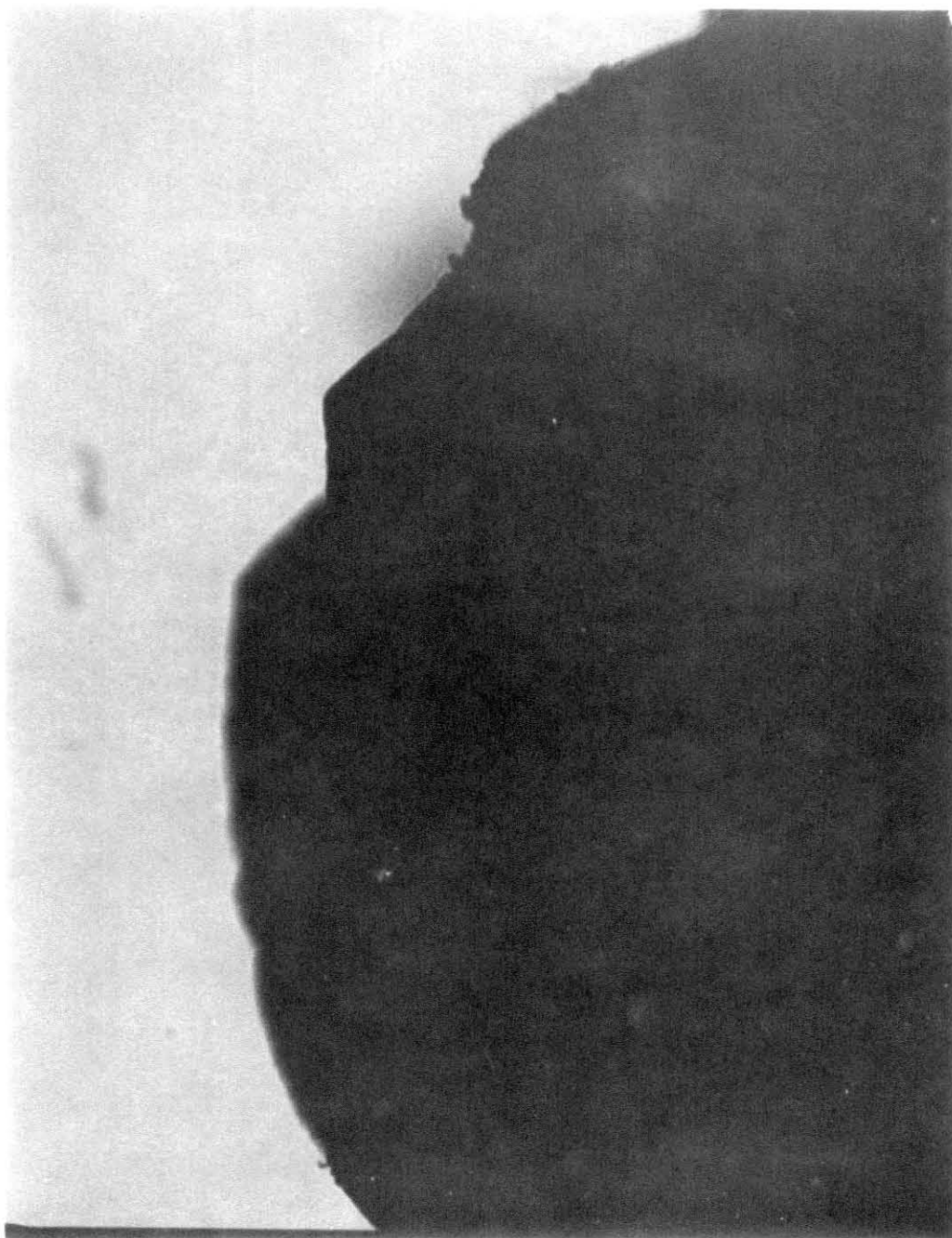
## EXPERIMENTAL RESULTS

After cutting with diamonds No. 3 and 4, it was concluded that the diamond may fracture under severe loading. Severe loading occurred when too deep a cut was accidentally taken. Some fracturing may be desired under actual cutting conditions to provide a sharp cutting edge, but for this study fractures were not desired. A photograph of the fractured diamond is shown in Fig. 10.

When the diamond fractured, a decrease in cutting forces occurred. As the sharp edge wore away, the forces increased and eventually became higher than the level prior to fracture. When diamond No. 3 fractured, enough of the diamond broke away that further tests would have been meaningless. The diamond was not worn enough prior to this to yield any useable information.

Diamond No. 4 broke on the first run in such a way that the area of the flat spot was still measureable. The tests on this diamond were continued until the vibrations became too large. It was not known whether the vibrations were due to the diamond being worn or if the speed coincided with the natural frequency of the system. The reason was assumed to be the latter because such large vibrations were not noticed with other worn diamonds.

The wear tests on diamond No. 5 proceeded very well yielding good data. The diamond wore at a slow rate, requiring a very large amount of cutting time to yield the desired results. For the final wear measurements, diamond No. 5 had traveled over 140 miles. For these reasons, all the data presented is taken from diamond No. 5.

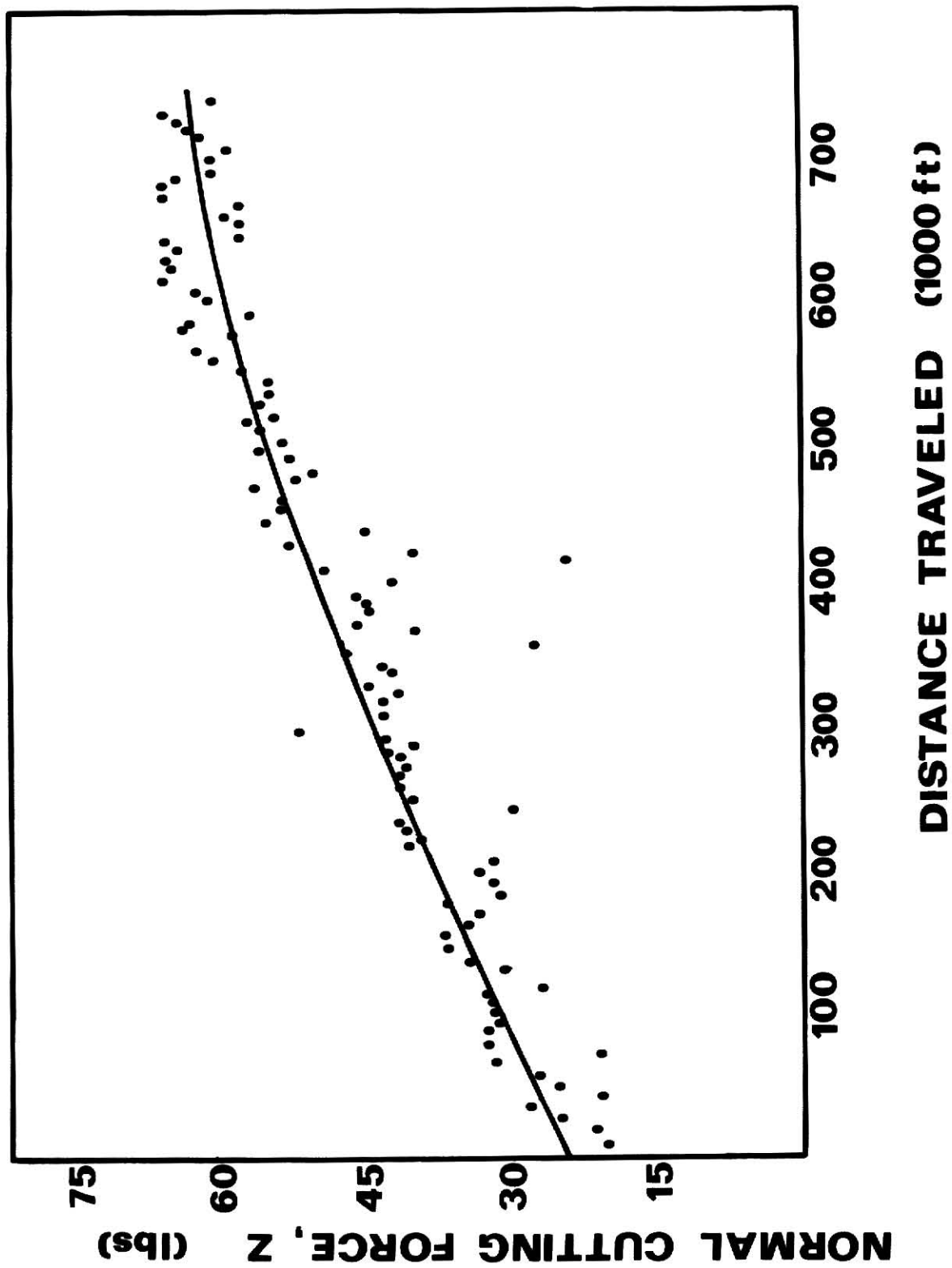


Fractured Diamond

Figure 10

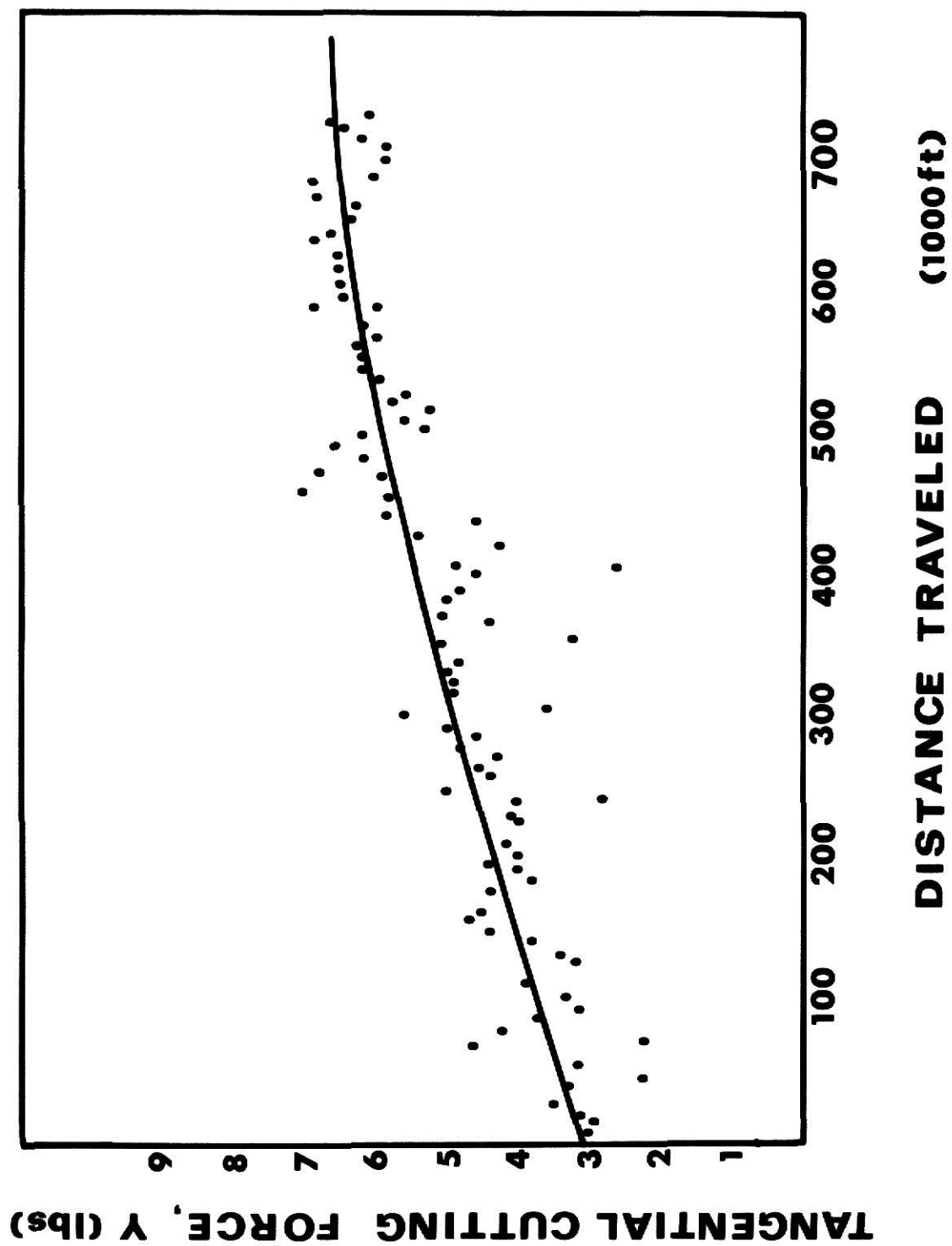


Fig.'s 11, 12, and 13 show how the forces changed in relationship to the distance traveled. The forces were lowest when the diamond was new, but as the diamond wore, the forces became larger. This is shown in Fig.'s 14 and 15.



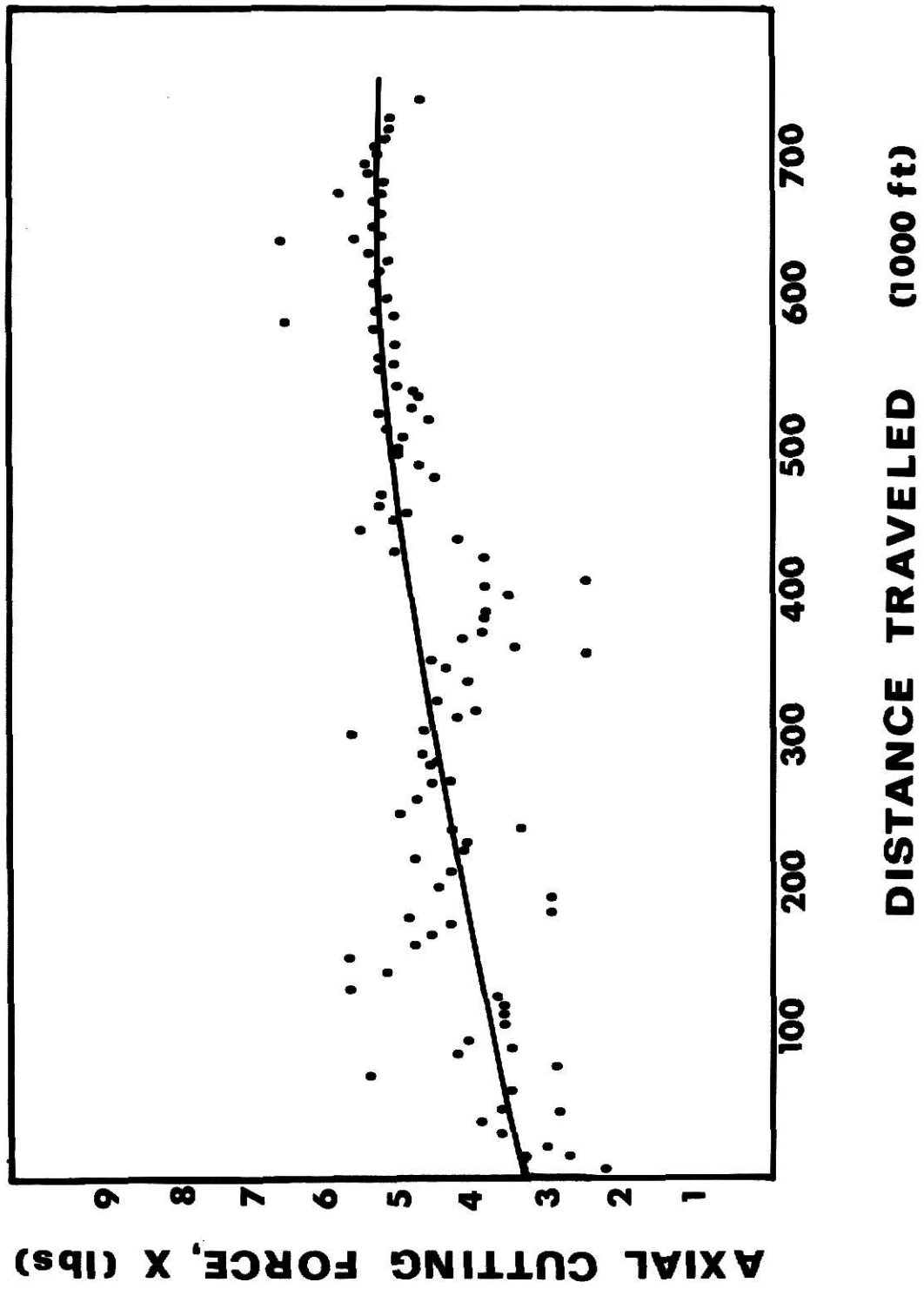
Normal Cutting Force vs. Distance Traveled

Figure 11



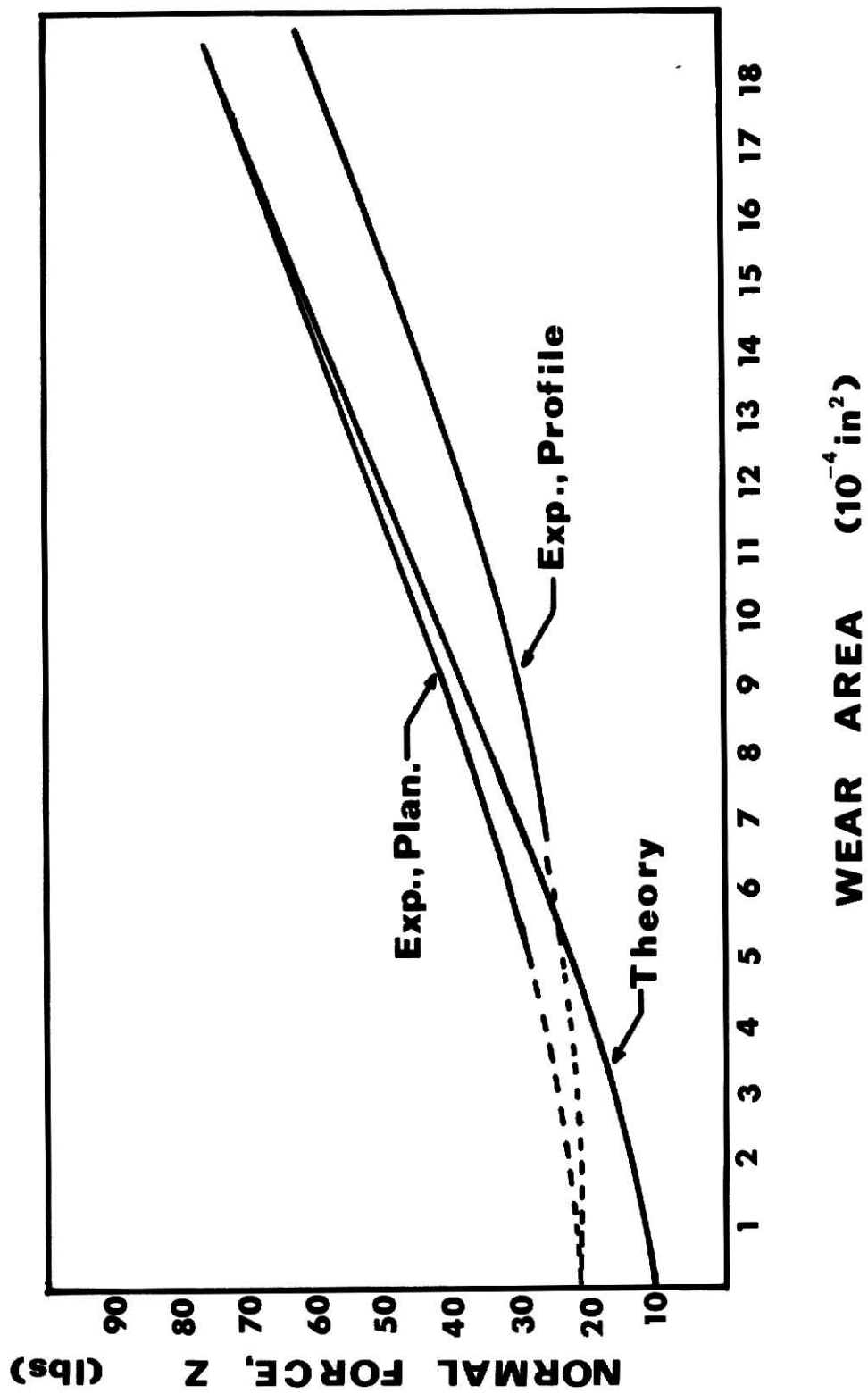
Tangential Cutting Force vs. Distance Traveled

Figure 12



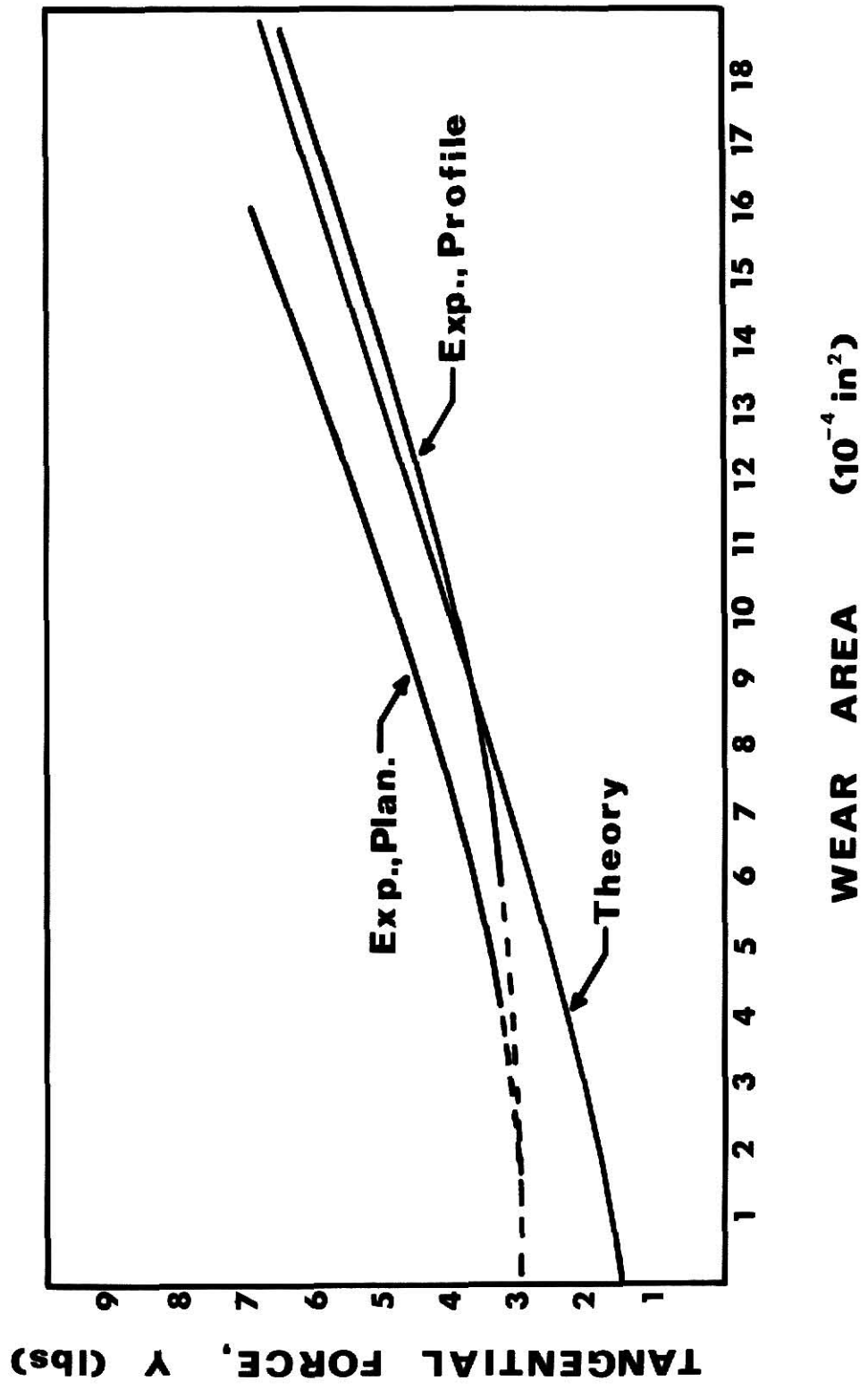
Axial Cutting Force vs. Distance Traveled

Figure 13



Normal Force vs. Wear Area

Figure 14



Tangential Force vs. Wear Area

Figure 15

By using the theory developed by Appl, (appendix 2), the data in Table 2 was obtained. This theoretical data was then plotted on the same co-ordinates as the experimental data. These graphs are shown in Fig.'s 16, 17, 18, 19, and 20.

As can be seen from Fig.'s 16 and 17, the theoretical forces were lower than the experimental forces when the diamond was new, but as the diamond wore, the curves approached the same levels. It is also seen in Fig. 18, that the experimental diamond wore faster than the theoretical diamond at first, but as the experimental wear area leveled off, the theoretical wear area surpassed it. The reasons for this are not entirely understood.

CHRISTENSEN DIAMOND PRODUCTS COMPANY  
SINGLE DIAMOND CUTTING ANALYSIS

JULY 1 1972

F.C. APPL

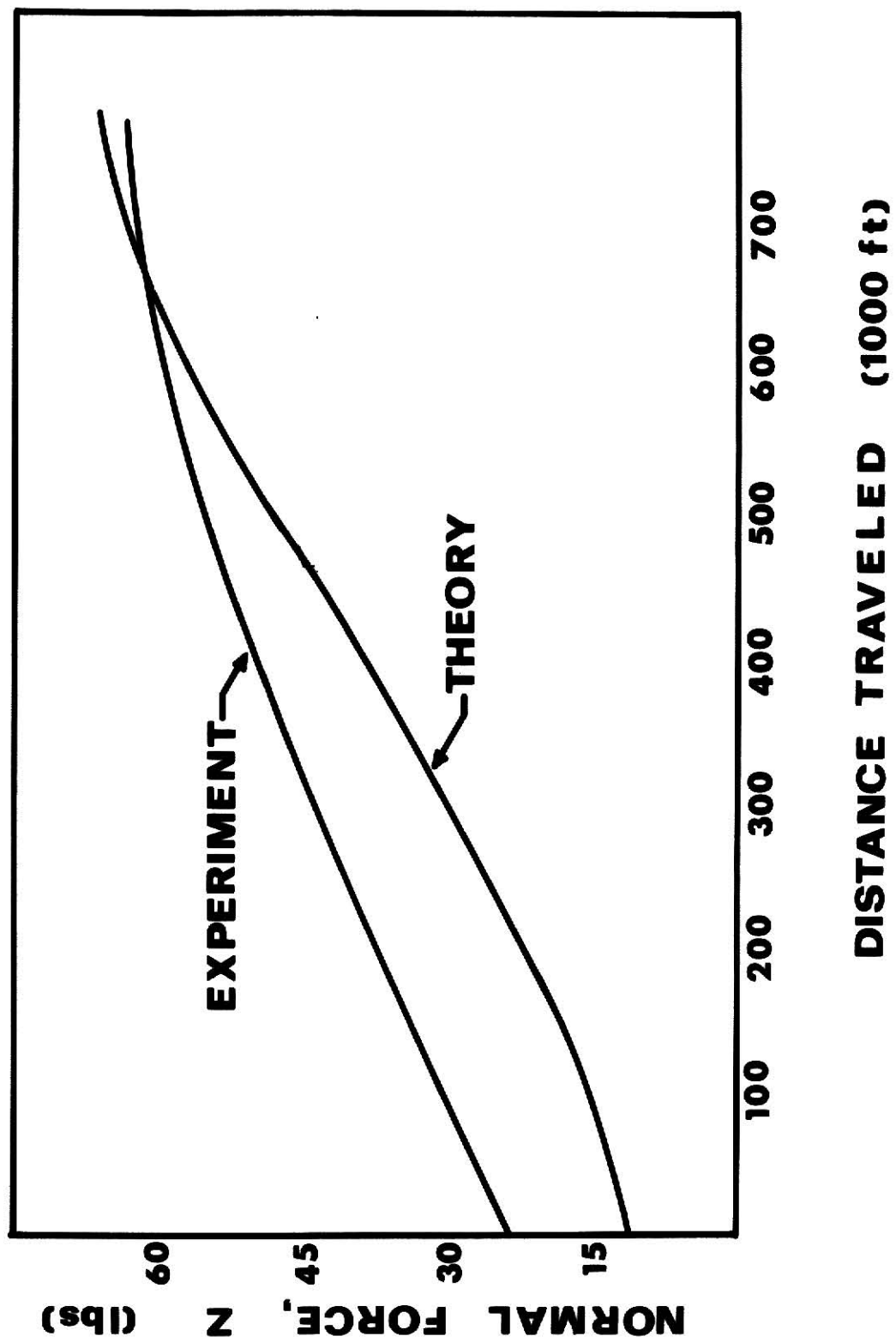
GEORGIA GRANITE

MAXIMUM NORMAL STRESS (LB/SQ IN).... 234432.  
DIAMONDS PER CARAT ..... 8.000  
RADIUS OF STONES (IN) ..... 0.04600  
ANGLE OF INTERNAL FRICTION (DEG) .... 50.00  
COMPRESSIVE STRENGTH (LB/SQ IN) ..... 18080.0  
SHEAR STRESS AT INFINITY (LB/SQ IN).... 200000.  
COEFFICIENT OF FRICTION ..... 0.0800  
CHIP SWEEP RATIO ..... 1.100  
GEORGIA GRANITE  
EFFECTIVE ANGLE (DEG) ..... 36.146  
EFFECTIVE STRENGTH (LB/SQ IN) ..... 17999.970  
CONFINING PRESSURE (LB/SQ IN)..... 0.  
CENTER SLICING ANGLE (DEG) ..... 16.60  
WEAR FACTOR ..... 0.2300E-12

WEAR ANG	WDR LOAD	IAN LOAD	RFS LOAD	CUT	LAMDA	VOLUME	WEAR AREA	WEAR DEPTH	ENERGY	DISTANCE
0.	12.7497	1.72365	12.8657	0.0009261	11.517	0.00001250	0.00000	0.0000	137889.	0.
2.	12.6663	1.73639	12.7848	0.0009014	11.537	0.00001250	0.00001	0.0000	138910.	3066.
4.	12.6363	1.77576	12.7605	0.0008399	11.677	0.00001250	0.00003	0.0001	142078.	12258.
6.	12.9663	1.84707	13.0969	0.0007601	12.041	0.00001250	0.00007	0.0003	147783.	27567.
8.	13.8947	1.95783	14.0320	0.0006765	12.693	0.00001250	0.00013	0.0004	156631.	48973.
10.	15.5672	2.11481	15.7102	0.0005985	13.640	0.00001250	0.00020	0.0007	169183.	76451.
12.	18.0352	2.32113	18.1840	0.0005299	14.844	0.00001249	0.00029	0.0010	185819.	109966.
14.	21.3027	2.58074	21.4585	0.0004724	16.255	0.00001250	0.00039	0.0014	206512.	149478.
16.	25.3234	2.89141	25.4883	0.0004243	17.817	0.00001250	0.00051	0.0018	231333.	194940.
18.	30.0499	3.25173	30.2253	0.0003842	19.489	0.00001250	0.00063	0.0023	260144.	246294.
20.	35.4296	3.65960	35.6181	0.0003506	21.240	0.00001250	0.00078	0.0028	292766.	303480.
22.	41.4125	4.11278	41.6162	0.0003224	23.048	0.00001250	0.00093	0.0033	329018.	366427.
24.	47.9494	4.60827	48.1703	0.0002984	24.898	0.00001250	0.00110	0.0040	368655.	435057.
26.	54.3944	5.14369	55.2344	0.0002781	26.779	0.00001251	0.00128	0.0047	411200.	509290.
28.	62.4971	5.71463	62.7579	0.0002633	28.683	0.00001251	0.00147	0.0054	456446.	589032.
30.	70.4136	6.31844	70.6965	0.0002449	30.605	0.00001250	0.00166	0.0062	505292.	674189.
32.	78.6973	6.95276	79.0037	0.0002314	32.540	0.00001250	0.00187	0.0070	556034.	764655.

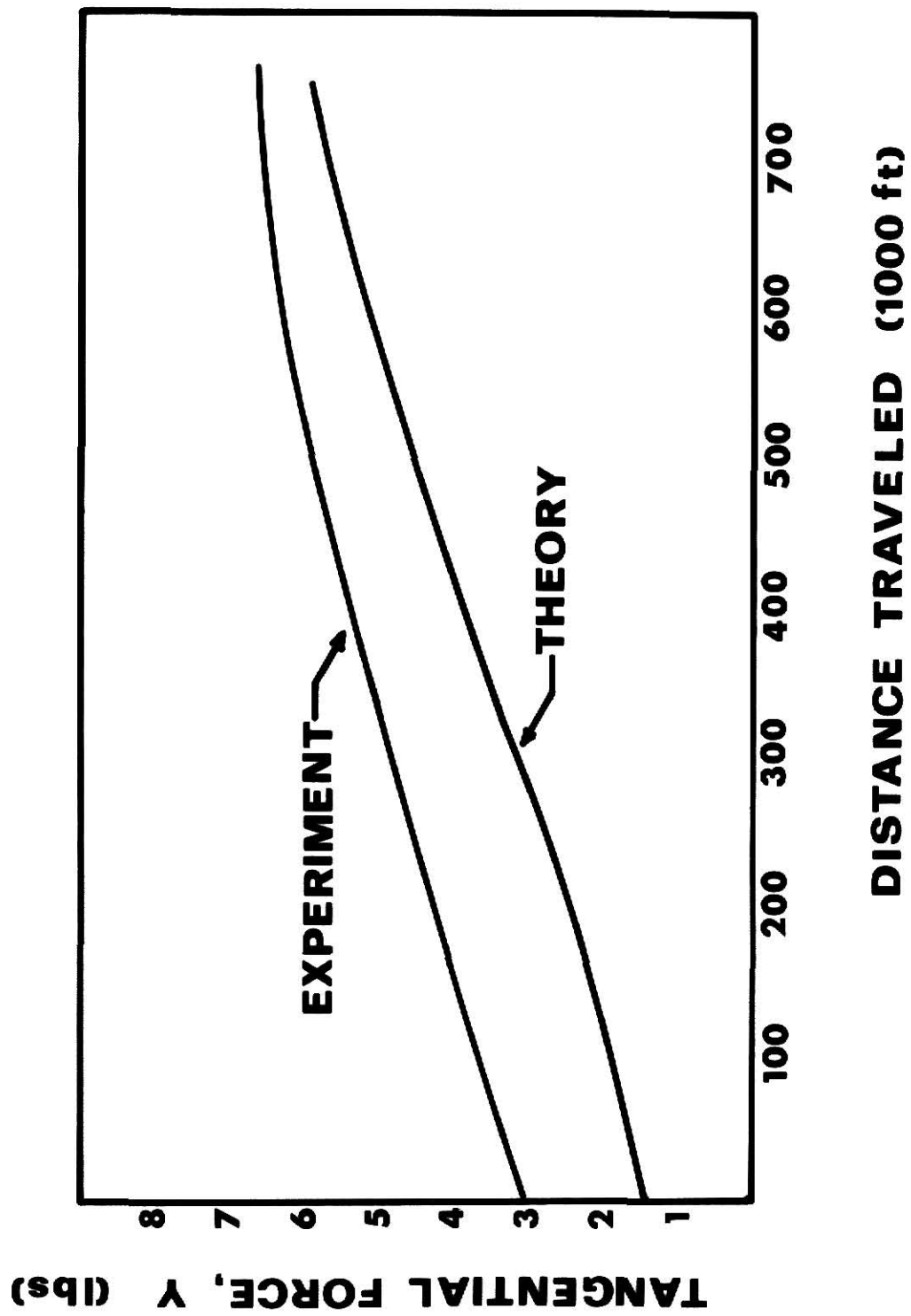
THEORETICAL RESULTS





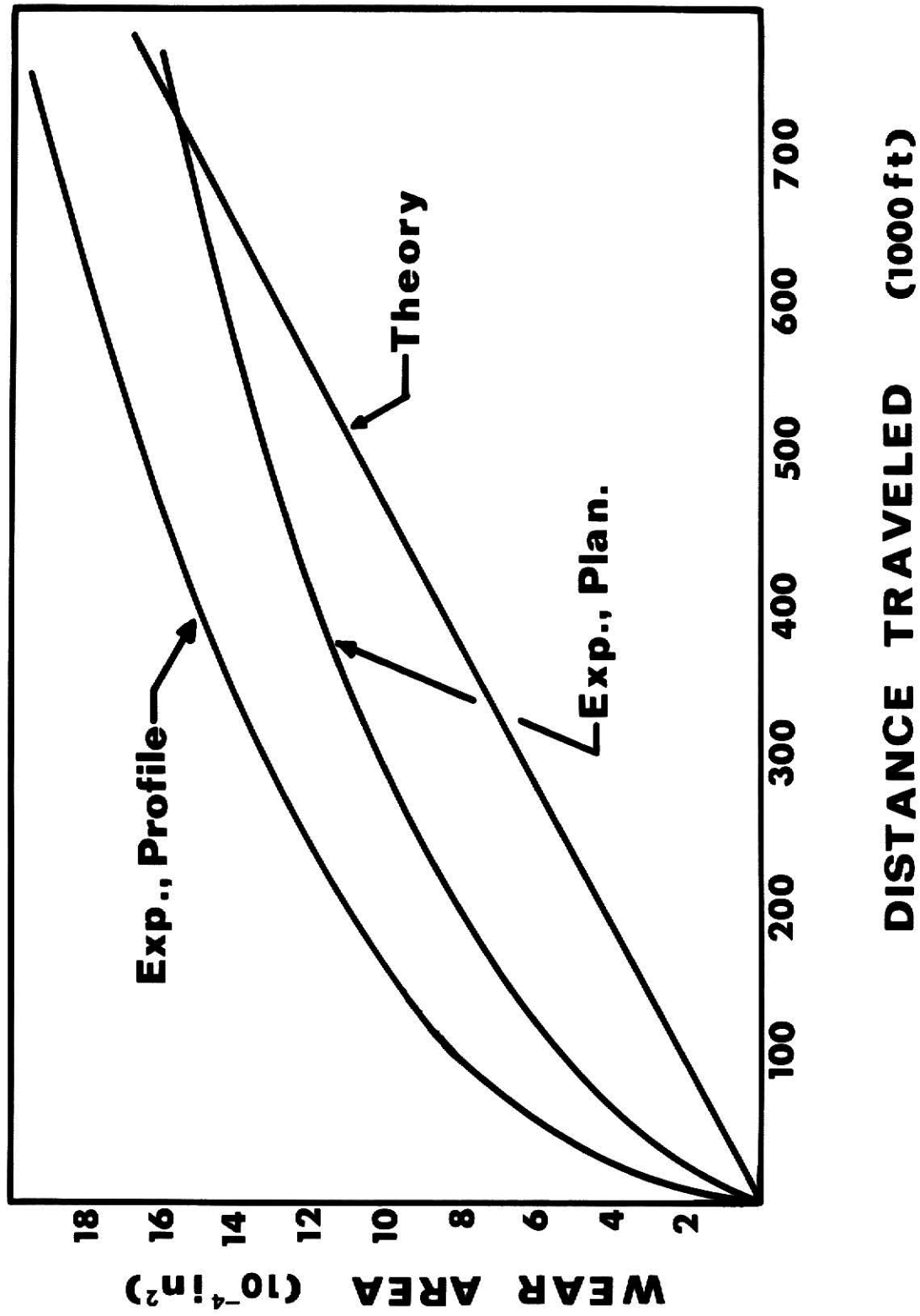
Normal Force vs. Distance Traveled

Figure 16



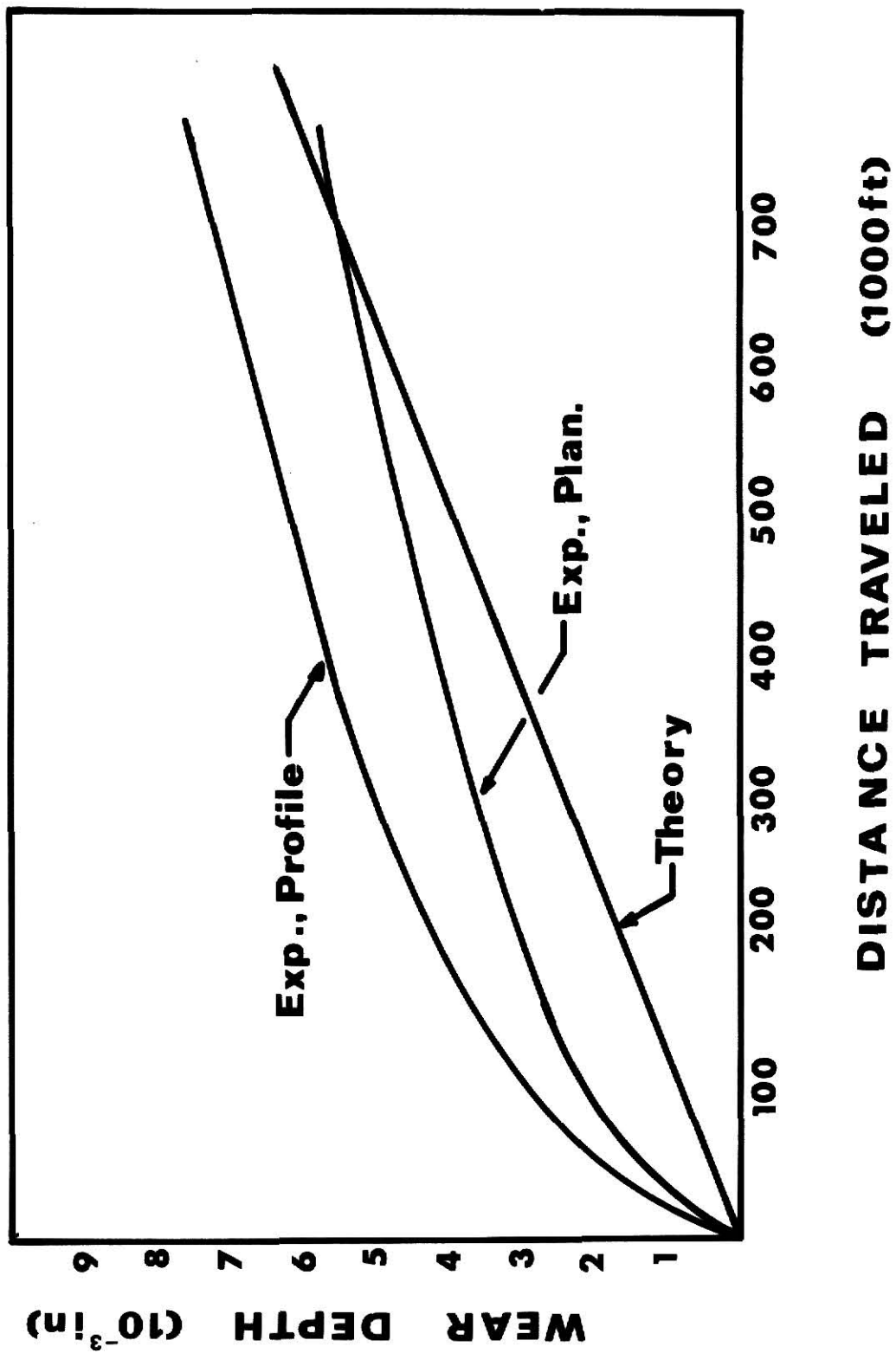
Tangential Force vs. Distance Traveled

Figure 17



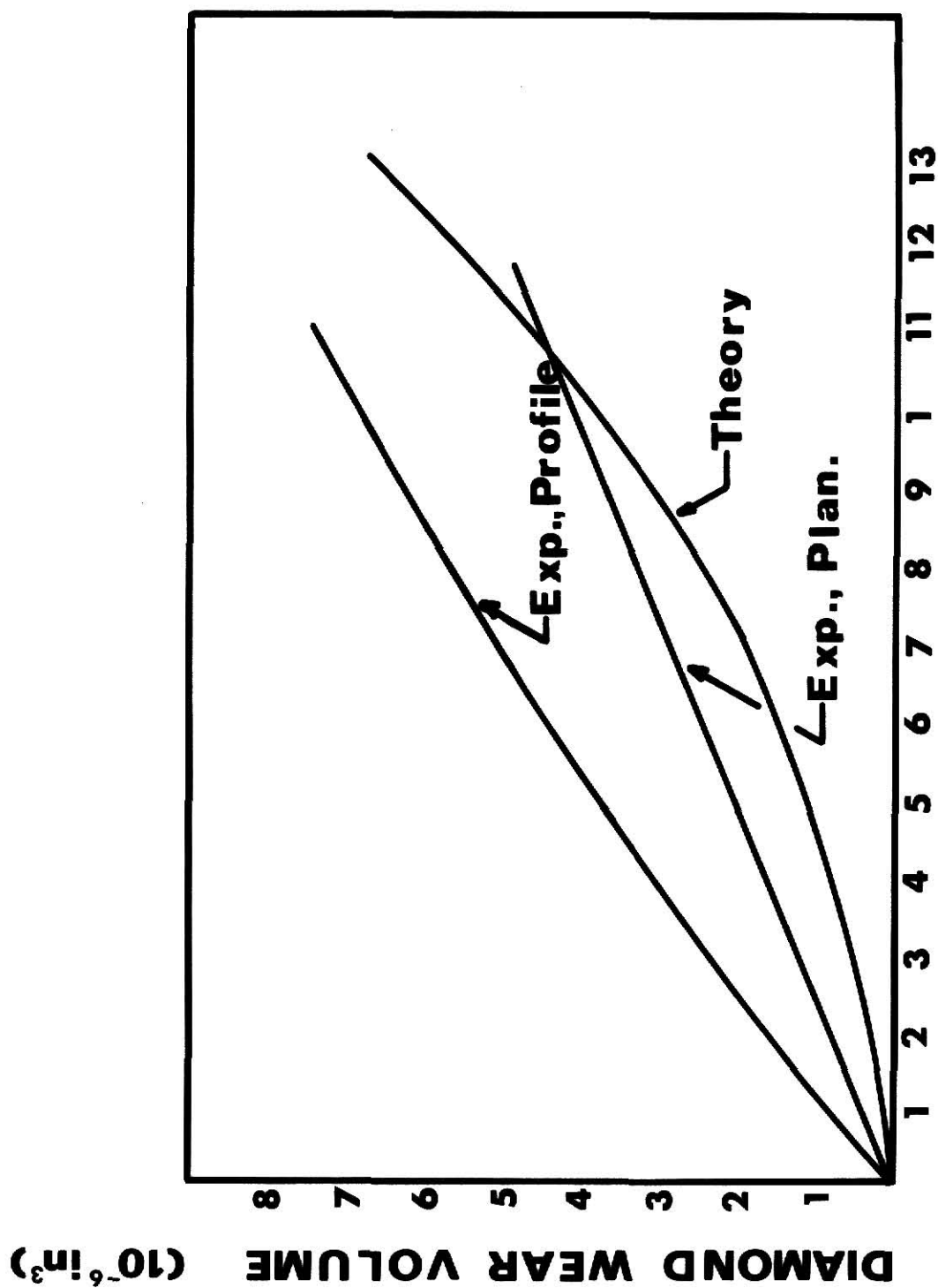
Wear Area vs. Distance Traveled

Figure 18



Wear Depth vs. Distance Traveled

Figure 19



## VOLUME REMOVED ( $10 \text{ in}^3$ )

Diamond Wear Volume vs. Volume Removed

Figure 20

## CHAPTER V

### CONCLUSION

The forces were analyzed in relation to cutting distance and wear area. It was found that there was a definite relationship between the rate of wear and the cutting speed, but because of the time element, this was not considered.

It is felt that this study is valid and a good beginning point for further studies. It is important to learn more about the speed effect. This will require that data for several different speeds be obtained.

## CHAPTER VI

### RECOMMENDATIONS

To enhance the value of this work, several additional tests need to be made. Other types of rock should be tested, as granite is a small part of the rock cut in practice.

Another variable not considered was diamond size. All the tests were based on a .092 inch diamond. It is expected that similar results would be obtained for diamonds of other size, but this should be verified experimentally.

A lathe with variable speed is recommended for further tests. This would allow the cutting speed to be held constant.

It would also be helpful if a method to measure diamond wear area could be devised that did not require that the diamond be removed from the dynamometer. This would reduce the possibility of taking too deep a cut which could cause premature diamond fracture.

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2. Gerhardt, J. S., "Thermal Problems and Grinding Wheel Characteristics". Technical Paper, No. MR70-805, Society of Manufacturing Engineer, 1970.
3. Keen, D. and A. F. Grogan. "Wear of Single Point Diamond Tools in the Machining of Aluminum/Silicon Alloy Pistons - A Final Report". Industrial Diamond Review, June 1971, 228-235.
4. Loladze, T. N., and G. V. Bokuchava. The Wear of Diamonds and Diamond Wheels.
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6. Reese, J. H. "An Experimental Investigation of the Cutting Action of a Single Diamond." (Unpublished Master's Report, Kansas State University, 1970).



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C      READ COEFFICIENT OF FRICTION
C      71 READ(CO) 1
C      READ CATCH SLIDING ANGLE
C      171 READ(CO) CO
C      72 READ(CO) CO
C      73 PI=3.1415927
C      200 CONTINUE
C      232 IF (CO) 204,204,220
C      204 T31=1.0
C      206 T32=1.0
C      208 T34=C.O
C      210 T36=C.O
C      212 T35=C.O
C      214 T36=C.O
C      216 GO TO 406
C      220 IF (CO-20.0) 241,222,222
C      222 T31=PI/4.0
C      224 T32=((PI*PI)/16.0)+C.25
C      226 T33=1.0
C      228 T36=((PI/2.0)-1.0
C      230 T35=T31
C      232 T36=T32-3.5
C      234 GO TO 405
C      240 C=CO*PI
C      242 T8=(2.0*C)/PI
C      244 SIN=COS((PI/2.0)-C)
C      246 COS=COS((PI/2.0)-C)
C      248 TPI=PI*1.0
C      250 TPI=PI-1.0
C      252 PI2=PI/2.0
C      254 SIN=SI*(PI2+TPI)
C      256 SIN=SI*(PI2+TPI)
C      258 COS=CO*(PI2+TPI)
C      260 COS=CO*(PI2+TPI)
C      262 SIN=SI*(PI2+TPI)
C      264 COS=CO*(PI2+TPI)
C      270 T1=(COS*COS*PI+SI*SI*(COS*PI-1.0))/(2.0*PI)
C      272 T2=(COS*COS*PI+SI*SI*(COS*PI-1.0))/(2.0*PI)
C      274 T3=T1-T2
C      276 T35=T1+T2
C      278 T1=(COS*PI2+SI*PI*(COS*PI-1.0)/PI)
C      280 T1=(SI*PI*(PI2+SI*PI*(COS*PI-1.0)/PI)+(2.0*PI)
C      282 T2=(COS*PI2+SI*PI*(COS*PI-1.0)/PI)
C      284 T2=(SI*PI*(PI2+SI*PI*(COS*PI-1.0)/PI)+(2.0*PI)
C      286 T2=T1-T2
C      288 T36=T1+T2
C      290 T3=(COS*PI+SI*PI*(COS*PI-1.0)/PI)
C      292 T3=(COS*PI*(COS*PI-1.0)/PI+PI2*SI*PI)
C      294 T3=(T3-(SI*PI*(SI*PI*(COS*PI-1.0)/PI)
C      406 CONTINUE
C      ALPR=ALPD*PI
C      410 AD2=AC*AD
C      420 SIN=SI*(ALPR)
C      422 COS=COS*(ALPR)
C      TAUD=SI*(1.0-SIN)/PI*0.000000
C      SIGX=SI*(COSAL)
C      SIGY=SI*(COSAL)
C      B=TALL-TAUD

```

```

105 PS1=(C.O)
106 PS1=PS1/R
107 453 DELALP=0.1
108 ALP=ALP*
109 KKT=1
110 437 SIGNAL=SI*(ALP)
111 COSAL=COS(ALP)
112 TANALP=SI*TAN(COSAL)
113 TAU=SIG*(1.0-SIGNAL)/(1.0*CCSAL)
114 PSK=PS1+SIGA
115 PSX2=PSK*PSK
116 EPX=EXP(-PSX)
117 G=1/(1-TAU/R)*(2.0*TAU/SIGX-1.0/COSAL)
118 G=C-TANALP/R*2.0*SIGX*SIGNAL/(1.0*8*CCSAL*COSAL)
119 G=G+2.0*TAU*(EPX-1.0)/(PSK*SIGX)
120 G=C-2.0*(PS1+1.0)*(PX-1.0)/(PSK2*COSAL)
121 IF(KKT-11439.439.441)
122 GG=G
123 ALP1=ALP
124 ALP=ALF-DELALP
125 KKT=2
126 GOTO437
127 441 IF(GG/G)447.443.443
128 443 ALP1=ALP
129 GG=G
130 ALP=ALP-DELALP
131 GOTO437
132 447 ERR=TANALP-ALP1*(ALP1-ALP)/(ALP*ALP)
133 WRITE(13.1)ALP,ALP1,G,GG,ERR
134 IF(GG-2.0)451.451.449
135 449 DELALP=DELALP/2.0
136 ALP=ALP+DELALP
137 GOTO437
138 451 ALD=ALF/PIC
139 SIGNAL=SI*(ALP)
140 COSAL=COS(ALP)
141 A1=0.5*(1.0+SIGNAL)/SIGNAL
142 A2=0.5*(1.0-SIGNAL)/SIGNAL
143 BET=SI*AL/COSAL
144 PIB=PI*BEY
145 EPS9=EXP(PI*PIB)
146 SIG=(TAU+RET+SIGC)*2.0*COSAL/(1.0-SIGNAL)
147 SIGX1=SIG*(1+(1+EPS9)*A2)+SICC
148 ES=(SIGX1-SIGX)/(SIGX1-SIGX)/(SIGX1+SIGX1)
149 IF(SHICH1) WRITE(6.1) ER
150 IF(ER-ERR2) 433.433.435
151 435 SIGX=(SIGX1+SIGX)/2.0
152 GOTO453
153 433 SIGMA=SIG
154 SYRB=2.3*SIGMA
155 ALD=ALP/PIC
156 SI=TAU+2.7*COSAL/(1.0-SIGNAL)
157 SWX=SIGPA*(1+(1+EPS9)*A2)
158 434 BX8=RET*DET
159 436 BX01=BX0+1.0
160 438 HIN=1.0/BET
161 I=0
162 340 CONTINUE
163 I=I+1

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164 PSIN(1)=PSIN*(1-1)*DELPSI
165 PSIN=PSIN(1)+PIC
166 SINPS=SI*(PSIN)
167 VOL(1)=VOL(1)
168 CAP1=C*Q
169 APPR1=PSIN
170 Q=2.0*VOL(1)/(AD2*VCVD)
171 APPR2=(0.75*Q)+0.37*PSIN
172 APX2=2.0*APPR2
173 QAP2=APX2-SIN(APX2)-(2.0*PSIN-SIN(2.0*PSIN))
174 ERB1=C-QAP2
175 EKA=ERR1/QAP2
176 ERD2=ERR*ERR
177 IF(ERCR-ERRC)337,337,326
326 APPR3=APPR2
APPR2=APPR2+((APPR2-APPR1)/(CAP2-CAP1))*ERR1
CAP1=CAP2
APPR1=APPR3
GO TO 316
337 TAM=APPR2
TAMQ(1)=TAM/PIC
CUT(1)=AD*(COS(PSIN)-COS(TAM))
342 SINLA=SIH (TAM)
COSLA=COS(TAM)
344 TAMX2=2.0*TAM
346 SINZL=SIH (TAMX2)
347 COSZL=COS (TAMX2)
348 BLXPZ=(-2.0*BET+TA*
349 E=2BL=EXP (BLXPZ)
EPZBP=EXP(-2.0*BET*PSIN)
352 PZM=((2.0*BET+SINLA*SINLA)+SINZL*BIM)*(-EMZBL)
PZM=PZM+EPZBP*(2.0*BET+SIH(SINLA)*SIN(PSIN)+SIN(2.0*PSIN)+8(IN)
PZM=PZM+AI*EPIB
PZM=((CZV/RXR1)+(AZ*(SINZL-TAMX2-SIN(2.0*PSIN)+2.0*PSIN)))
356 PLS=PZM*((TJ3/2.0)-(TJ4/PI))
357 PZM=PZM/PI
358 PM2(1)=PZM*AD2*SICMA
PIN=(EPZBP*(BET+SIN(2.0*PSIN)+COS(2.0*PSIN)))-(EMZBL*((BET*
1SINZL)+COSZL))
362 PIN=(PIN*AI)/9XR1
PIN=(PIN*EPIB)+A2*(COSZL-COS(2.0*PSIN))
366 PIN=(PIN*PI)/8.0
PHI(1)=PIN*AC2*SICMA+PI*STR+AD2*SIN(PSIN)+SIN(PSIN)
503 PLSU=PLSU
504 TI1=(2.0*TJ1)-(4.0*TJ2/PI)
506 TI2=(2.0*TJ5)-(4.0*TJ6/PI)
508 PZS=TI1*AI*EPIB
PZS=PZS+((EPZBP*(2.0*BET+SIN(PSIN)+COS(PSIN))
1-(TEPZBL)*(2.0*BET+SINLA)*COSLA))/((4.0*RXB)+1.0)
512 PZSS=(TI2*AI*EPIB)/(4.0*RXB)
PZSS=PZSS+((EMZBL)*((BET+SINZL+COSZL)+EMZBP*(BET+SIN(2.0*
1PSIN)+COS(2.0*PSIN)))
PZSS=(TI1*(COSLA-COS(PSIN)))+(TI2/4.0)*(COS(2.0*PSIN)-COSZL))
520 PZS=(PZSS*AI)-PZSS +PZS
522 PZSU=L*PZS
524 PIA=(PI*PLSU)
PII(1)=PIA*AD2*SICMA+PI*AD2*STR+SIH(PSIN)+SIN(PSIN)
526 PZA=(PZV+PZSU)
PZII(1)=PZA*AC2*SICMA+PI*AD2*STR+U*SIH(PSIN)+SIN(PSIN)
530 CONTINUE

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221 //L(1)=C/D*AD2*0.5*(TAPX2-SIN2L-2.0*PSIW+SIN(2.0*PSIW))
222 //L(1)=AD*(COS(PSIW*PI)-COS(PSIW))/(WKS*U*STRB)/Z
223
224 ADO CONTINUE
225
226 P22=RL(1)*PI(1)+PI(1)+(P2(1)*P2(1))
227
228 P24=RL(1)*COT(PI(1))
229
230 P26=PI(1)-P2(1)/VOL(1)
231
232 EXP(1)=P2(1)/VOL(1)
233
234 EXP(1)=P2(1)/VOL(1)
235
236 ADO CONTINUE
237
238 P24=RL(1)=PI*AD2*SIN(PSIW)*SIN(PSIW)
239
240 P26=PI(1)=AD*PI*0-COS(PSIW)
241
242 IF(1-CL1)GO TO 878
243
244 WRITE(6,3003)NOTE
245
246 //WH 5X3HS SINGLE DIAMOND CUTTING ANALYSIS
247
248 Z/INSTR1343,42X,27H F-C. APPL
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APPENDIX 2  
EXPERIMENTAL DATA

Run No.	Z	Y	X	Rock Diameter (in)	Diamond Wear Area (10 <sup>-4</sup> in <sup>2</sup> ) (Profile)	(Plan)
1	14	3.0	2.2	7.293		
2	19	2.19	2.17	7.283		
3	21	3.1	3.0	7.276		
4	25	3.5	3.6	7.267		
5	27	3.2	3.9	7.258		
6	21	2.2	2.8	7.249		
7	26	3.1	3.6	7.238		
8	27	3.2	3.5	7.230	6.600	4.51
9	32	4.6	5.4	7.220		
10	20	2.2	2.9	7.210		
11	33	4.2	4.2	7.197		
12	33	3.7	3.5	7.187		
13	31	3.1	4.1	7.179		
14	32	3.3	3.6	7.169		
15	32	3.9	3.6	7.158		
16	33	4.0	3.6	7.149	8.96	6.49
17	27	3.2	3.7	7.139		
18	31	3.4	5.7	7.129		
19	30	3.8	5.2	7.121		

## EXPERIMENTAL DATA

Run No.	Z	Y	X	Rock Diameter (in)	Diamond Wear Area ( $10^{-4}$ in <sup>2</sup> )	
					(Profile)	(Plan)
20	34	4.4	5.7	7.113		
21	37	4.7	4.8	7.103		
22	35	4.5	4.6	7.091		
23	33	4.1	4.3	7.082		
24	37	4.4	4.9	7.063	10.86	8.56
25	31	3.8	2.9	7.053		
26	32	4.0	2.9	7.043		
27	33	4.4	4.5	7.034		
28	32	4.0	4.3	7.024		
29	41	4.2	4.8	7.014		
30	40	4.0	4.2	7.004		
31	41	4.0	4.1	6.995		
32	42	4.0	4.3	6.985	12.31	9.28
33	30	2.8	3.3	6.974		
34	40	5.0	5.0	6.967		
35	42	4.4	4.8	6.958		
36	42	4.6	4.6	6.948		
37	40	4.4	4.3	6.938		
38	42	4.8	4.6	6.928		
39	40	4.6	4.5	6.919		
40	44	5.0	4.7	6.909	13.39	9.72
41	52	5.6	5.7	6.899		



## EXPERIMENTAL DATA

Run No.	Z	Y	X	Rock Diameter (in)	Diamond Wear Area ( $10^{-4}$ in <sup>2</sup> )	
					(Profile)	(Plan)
42	44	3.6	4.7	6.885		
43	44	4.9	4.2	6.876		
44	43	4.9	4.0	6.865		
45	45	5.0	4.5	6.855		
46	43	4.8	4.1	6.845		
47	44	4.9	4.4	6.835		
48	48	5.1	4.5	6.826	14.29	10.48
49	28	3.3	2.5	6.817		
50	41	4.4	3.5	6.809		
51	46	5.1	4.2	6.799		
52	45	5.0	3.9	6.790		
53	45	5.0	3.9	6.780		
54	46	4.9	3.9	6.771		
55	43	4.6	3.6	6.762		
56	49	4.9	3.9	6.752	15.22	11.35
57	23	2.6	2.4	6.742		
58	41	4.3	3.9	6.734		
59	53	5.4	5.1	6.727		
60	45	4.6	4.3	6.718		
61	55	5.9	5.6	6.709		
62	53	5.7	5.1	6.699		
63	53	5.8	5.0	6.690		

## EXPERIMENTAL DATA

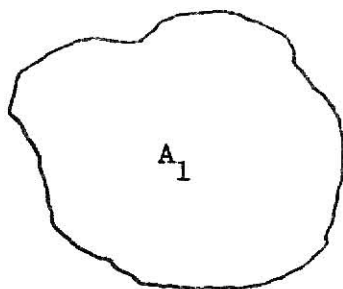
Run No.	Z	Y	X	Rock Diameter (in)	Diamond Wear Area ( $10^{-4}$ in <sup>2</sup> ) (Profile)	(Plan)
64	56	7.0	5.3	6.679	16.18	11.93
65	52	5.8	5.3	6.670		
66	51	6.8	4.6	6.661		
67	53	6.2	4.8	6.651		
68	55	6.6	5.1	6.641		
69	54	6.2	5.1	6.632		
70	55	5.3	5.0	6.621		
71	57	5.6	5.2	6.611		
72	53	5.2	4.7	6.602	16.92	12.87
73	55	5.8	5.3	6.593		
74	54	5.7	4.9	6.584		
75	53	5.7	4.8	6.574		
76	58	6.0	4.9	6.564		
77	61	6.2	5.1	6.555		
78	63	6.3	5.3	6.545		
79	59	6.0	4.6	6.534		
80	64	6.2	5.1	6.525	17.67	13.62
81	63	6.9	6.6	6.515		
82	57	6.1	5.1	6.506		
83	62	6.5	5.3	6.495		
84	63	6.5	5.2	6.484		
85	66	6.5	5.3	6.473		
86	65	6.7	5.4	6.463		

## EXPERIMENTAL DATA

Run No.	Z	Y	X	Rock Diameter (in)	Diamond	
					Wear Area (10 <sup>-4</sup> in <sup>2</sup> ) (Profile)	(Plan)
87	65	6.6	5.3	6.453		
88	64	6.6	5.2	6.444	18.18	14.47
89	66	6.9	6.7	6.433		
90	59	6.7	5.7	6.423		
91	59	6.3	5.3	6.412		
92	60	6.4	5.4	6.402		
93	59	6.3	5.3	6.392		
94	66	6.9	5.9	6.383		
95	67	6.9	5.3	6.371		
96	65	6.1	5.3	6.362	18.70	14.90
97	61	5.9	5.5	6.352		
98	61	5.9	5.5	6.343		
99	60	5.9	5.4	6.333		
100	62	6.2	5.4	6.324		
101	63	6.2	5.3	6.314		
102	65	6.5	5.3	6.304		
103	67	6.7	5.7	6.294		
104	61	6.1	4.8	6.284	19.50	15.43

## APPENDIX 3

## Diagram of Worn Diamond and Calculations

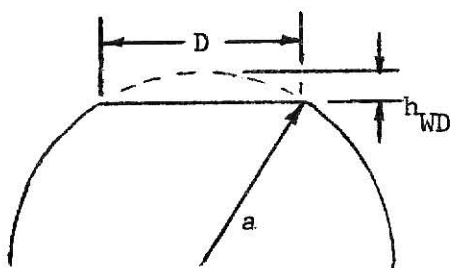


Area measured with a planimeter from Fig. 8a

$$A_1 = \pi (R_{eq})^2$$

$$R_{eq} = (A/\pi)^{1/2}$$

$R_{eq}$  is the radius of a circle with area  $A_1$  (Plan).



$D$  is measured from Fig. 8b

$$D = 2 R^*$$

$$R^* = D/2$$

$R^*$  is the radius of a circle with area  $A_2$  (Profile).

$$h_{WD} = a - (a^2 - R^2)^{1/2}$$

$$Vol = \frac{\pi}{3} (h_{WD})^2 (3a - h_{WD})$$

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I would like to thank Dr. F. C. Appl for his assistance and advice. I would also like to thank Carl Hansen for his assistance with the experimental work. I am also grateful for financial support given by Kansas State University and Christensen Diamond Products Company. I would very much like to thank my parents for their patience and understanding love during the time I was in school.

VITA

DONALD L. HELLAR

Candidate for the Degree  
Master of Science

THESIS:       An Experimental Investigation of the Cutting Forces and  
              Wear Area of a Single Diamond

MAJOR FIELD:   Mechanical Engineering

BIOGRAPHICAL:

Personal Data: Born September 18, 1948 at Kingman, Kansas;  
                 the son of Alva L. and Bernice E. Hellar.

Education:     Graduated from high school at Cunningham,  
                 Kansas in 1966; received an A.A. degree  
                 from Pratt Community Junior College in 1968;  
                 received a B.S. in Mechanical Engineering  
                 from Kansas State University in 1970; completed  
                 requirements for the M.S. degree in August 1972.

AN EXPERIMENTAL INVESTIGATION OF THE CUTTING  
FORCES AND WEAR AREA OF A SINGLE DIAMOND

by

DON HELLAR

B.S., Kansas State University, 1970

---

AN ABSTRACT OF A MASTER'S THESIS  
Submitted in Partial Fulfillment of the  
Requirements for the Degree  
MASTER OF SCIENCE

Department of Mechanical Engineering  
Kansas State University  
Manhattan, Kansas

1972

## ABSTRACT

The use of diamonds as a cutting tool material has a long history. With the increased use of diamonds for this purpose and the large costs that are involved, studies of the cutting action and wear of the diamond have become more important.

The purpose of this work, was to discover how a diamond wears under actual cutting conditions, and to compare these results with a previously developed theory on diamond wear. To do this, a diamond was used as a cutting tool for cutting a cylindrical piece of granite chucked in a lathe. The cutting forces were recorded on a specially built dynamometer.

The experimental results revealed that the relationship between diamond wear and cutting distance did not increase linearly, but progressed rapidly in the beginning and then slowed down. All experimental results were compared to the theory and found to be of similar trends but of slightly different magnitudes.