# THE EFFECTS OF DESICCATION ON SOIL DEFORMATION 

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## A MASTER'S THESIS

submitted in partial fulfillment of the
requirements for the degree

MASTER OF SCIENCE

Department of Civil Engineering

KANSAS STATE UNIVERSITY
Manhattan, Kansas
1979
Approved by:


## ACKNOWLEDGEMENTS

The author wishes to express his gratitude and sincere appreciation to the following individuals:

To his wife, Jolene for her sympathy and encouragement, particularly during the writing of the thesis.

To his children, Joel and Amy for sacrificing their time with dad.
To his parents, J. D. and Maxine Wineland for their encouragement in continuing his education.

To the Kansas Department of Transportation and to G. N. Clark in particular for encouraging professional development and making time and money available for implementing the use of modern methods of computer analysis.

To the Federal Highway Administration for their efforts in making advanced technology available and in working out problems which developed in the application of this technology.

To Miss Dolores Galvan for typing the rough drafts of the thesis.
To Mrs. Joan Edwards for typing the final manuscript.
To Mr. Larry Moser for his work in preparing the graphical portions of the thesis.

To Dr. Myron Hayden, who served as principal advisor and to the rest of the committee members, Professor E. C. Lindly, Professor E. R. Russell, and Professor Stanley Clark.

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## CHAPTER I

## INTRODUCTION

The increasing use of high earthen embankments, in addition to the proximity of various highway construction projects to underground utilities, has increased the need to accurately predict any soil deformation which is likely to occur. This need is particularly true for soils which have a variable strength profile with depth, as a result of desiccation. Desiccation resulting from the evaporation of the interstitial water, causes the soil near the ground surface to consolidate, thus resulting in the development of a soil profile which decreases in strength with depth. Information gained from this research could aid in both identifying the possible existences of desiccated soils and in properly accounting for their increased strength.

## Statement of the Problem

Consolidation is the process whereby a soil mass decreases in volume as a result of the removal of interstitial water. This phenomenon was first described by Terzaghi (1) analytically in 1925. In addition to an analytical analysis, he suggested a laboratory procedure to predict the magnitude of consolidation by applying a vertical stress to a soil sample which is laterally confined.

Highway departments have customarily used consolidation theory to predict settlements in the foundations of earthen embankments. The
application of this concept increases in validity as the distance from the embankment toe increases. Thus, under the center of an embankment, the lateral strain in the soil which results from the weight of the embankment is significantly reduced because of the increase in laterally applied stress. The major deformation which is likely to occur near the toe of a slope is a lateral rather than vertical movement of the foundation soil. Experience has shown that, when a foundation soil is soft, the lateral movement in the foundation near the toe of an embankment may be many times larger than the corresponding vertical movement. The relative magnitude of the lateral and vertical displacements which are likely to occur within the foundation soils due to embankment construction is shown conceptually in Figure 1. Therefore, the application of conventional one-dimensional consolidation theory will yield results which are only a fraction of the total deformation.

Adequate determination of the magnitude of soil strain which is likely to occur as a result of the construction of an embankment is important because of the effect it may have on buried structures (i.e., utilities, drainage structures, etc.). For example, a highway recently constructed by the Kansas Department of Transportation crossed over a rural road which had two 16 inch and one 54 inch diameter water lines running parallel to it. These water lines passed under the toe of an embankment used in the bridge approach. Because of the proximity of the buried water lines to the toe of the embankment, accurate estimates of the magnitude of the vertical and lateral strains of the foundation soils had to be made. Failure to make these accurate predictions could have resulted in considerable increase in construction time and costs.

## LEGEND

< Relative Displacements

a. Asymmetrical Embankment

LEGEND
$\longleftarrow$ Relative Displacements

b. Symmetrical Embankment

Figure 1. Conceptual Illustration of Relative Displacements Under an Embankment.

As an aid in analyzing this type of problem, the Kansas Department of Transportation obtained a finite element computer program from the Federal Highway Administration. This program, developed by Ozawa and Duncan (2), can be used to analyze the various soil stresses, therefore it serves as a useful tool in stability analysis. Since the program is based on the principles and concepts of the theory of elasticity, it could also be used to predict soil displacements within an embankment. Therefore, this study was conducted in an attempt to implement the use of this finite element program to predict potential movements within the embankment and foundation. Since the program computes the stresses and corresponding strains within a soil mass based on strength parameters, an adequate method of assessing those parameters had to be developed. This is particularly important when the foundation material varies in strength as a result of desiccation.

## Scope of Investigation

The scope of this investigation is included in three phases. The first phase was the design and construction of an earthen embankment utilizing conventional design and construction procedures. Also included was the installation of monitoring devices within the embankment to measure pore pressures and movement during and after construction. The second phase consisted of correlating the deflections predicted using the finite element program to those that were actually measured by the field instruments. The results of this correlation indicated that the predicted deflections based upon the finite element program were far in excess of those measured in the field. An investigation was then conducted
to determine the reasons for this large discrepancy. The investigation lead to the conclusion that the failure to recognize and account for the increased soil stiffness which resulted from the desiccation of the foundation material was a major factor in this large difference.

The third phase consisted of the development of an adequate means of assessing the strength of a desiccated soil. During this phase the conventional sampling and testing program used to provide the design parameters was examined. Based on this examination, modifications in the previously specified method of sampling and testing were made to improve the quality of the results.

## CHAPTER II

## A LITERATURE CRITIQUE OF DESICCATION

AND RESULTING OVERCONSOLIDATION OF A SOIL

Consolidation of a soil mass is defined as the deformation which results from a change in the relative positions of the soil particles and the corresponding decrease in interstitial volume. This decrease in volume is caused by a change in the interstitial or pore pressure which could occur because of either of the two following conditions: 1) additional load applied to the soil mass, or 2 ) desiccation of the upper soil strata. Whenever a soil is consolidated more than would be expected from the vertical stress currently applied, a state of overconsolidation exists.

The fact that desiccation of a soil near the ground surface can cause overconsolidation has been known by soils engineers for many years. However, the process of desiccation and its resulting effect on the strength characteristics of a soil are not well understood. It is known that the relative effect of desiccation on a soil is dependent on a number of physical properties (i.e., grain-size, clay content, mineralogical make-up, etc.). Therefore, this chapter will present the current theories used to explain its cause and subsequent effect on the strength parameters of a soil.

Terzaghi and Peck (3) describe the process of desiccation based on the laws of physics. According to their theory, evaporation at the
air-water boundary is dependent on both the relative humidity of the ambient air and the surface tension of the water. Since the relative humidity is rarely higher than $95 \%$, evaporation occurs causing negative pore pressure to develop in the soil voids in a manner similar to a capillary tube. Thus the magnitude of the negative pore pressure which develops is dependent upon the size of the voids at the soil surface. They theorized that when the water content decreases below the shrinkage limit, air begins to penetrate the soil and the water withdraws into corners of the voids. This continues until the negative pore pressure increases and a limiting value is reached, after which evaporation ceases.

For water contents above the shrinkage limit, the surface tension induced within the voids produces an effective pressure equal to the negative pore pressure developed. The negative hydrostatic pressure which develops within the voids causes the soil to consolidate. This form of consolidation has been observed to occur up to depths of 20 feet depending on the humidity and frequency of rainfall.

Lambe and Whitman (4) present a graph which they refer to as the relationship of the undrained shear strength to the overconsolidation ratio for an isotropically consolidated weald clay. Such a graph is presented in Figure 2. The graph consists of a ratio of the shear strength of a normally consolidated sample divided by the shear strength determined for a similar sample which is overconsolidated, plotted against the reciprocal of the overconsolidation ratio. The graph illustrates that by reducing the consolidation stress to one half its maximum value, the corresponding reduction in the undrained shear strength is only 17 percent. Thus, for the materials tested, a soil with an

$q_{f}=$ Shear strength at present effective stress.
$q_{f m}=$ Shear strength at maximum past effective stress.
$\bar{p}_{0}=$ Present effective stress.
$\bar{D}_{m}=$ Maximum past effective stress.

Figure 2. Relationship of Undrained Shear Strength to Overconsolidation Ratio.
overconsolidation ratio of two maintained 83 percent of the undrained shear strength it possessed at the maximum consolidation stress.

These authors do not directly address the question of how much the shear strength increases as a result of the overconsolidation. However, a graph is presented from which the shear strength can be estimated if the plasticity index and consolidation stress are known. An example was presented where the shear strength for a soil corresponding to the maximum consolidation stress was computed and then used to predict the shear strength of the same soil at various overconsolidation ratios by utilizing the graph shown in Figure 2.

From the relationships presented by these authors, the increase in shear strength resulting from overconsolidation can be computed. The graph illustrating the variation in the undrained shear strength as a function of plasticity index and consolidation pressure indicates that the shear strength for a particular soil is directly proportional to consolidating stress. Therefore, if the consolidation stress is doubled, the corresponding undrained shear strength is doubled. If the consolidation stress is then reduced to its original value, the soil will have an overconsolidation ratio of two and the strength will be reduced from its maximum value by 17 percent. Thus, the effect of overconsolidating a soil to twice its normally consolidated value is to increase its undrained shear strength by 66 percent. Table I illustrates the increases in shear strength for various overconsolidation ratios used, based on the discussion previously presented.

The authors point out that these relations are useful only in making preliminary estimates of undrained shear strength. It should be noted

## TABLE I

INCREASE IN SHEAR STRENGTH RESULTING FROM OVERCONSOLIDATION

| Overconsolidation Ratio | Increase in Shear Strength |
| :---: | :---: |
| 1.33 |  |
| 1.5 | $25 \%$ |
| 2.0 | $30 \%$ |
| 3.0 | $66 \%$ |
| 4.0 | $98 \%$ |

that the overconsolidation ratio for a desiccated soil generally will not be known, thus the use of these relationships to estimate the shear strength of a soil will be limited. However, these relationships do illustrate the fact that even a small amount of overconsolidation could significantly increase the shear strength of a soil.

Parry and Nadarajah (5) examined the effects of small overconsolidations by preparing samples of Kaolin from a slurry and testing them in an undrained condition. The samples were consolidated both isotropically and anisotropically and then tested in triaxial compression and extension. The anisotropic samples were consolidated under a zero lateral strain condition which is commonly referred to as $K_{0}$ consolidation.

The test results indicated that the effective stress path for an overconsolidated soil tested in compression was essentially vertical, unless the stress path corresponding to a normally consolidated condition was reached. At low confining pressures, the stress path remained vertical until a failure condition was reached. At high confining pressures, the stress path reached the stress path corresponding to a normally consolidated condition, after which they remained essentially parallel. A marked increase in pore pressure was noted when the two stress paths were in close proximity.

The occurrence of a vertical stress path implied that the average effective stress remained constant as the deviator stress increased. However, when the stress path for the overconsolidated soil reached the stress path corresponding to a normally consolidated soil, the average effective stress decreased rapidly while the deviator stress increased.

This effect can be explained using plastic theory in soils. The deformation is considered elastic only while the stress path is vertical. Therefore, plastic deformation was occurring only over a portion of the loading sequence.

The manner in which the soil was consolidated, whether isotropic or anisotropic, was shown to have an effect on the resulting shear strength. The value determined for the angle of internal friction was 1.8 degrees smaller for the anisotropicly consolidated samples.

It was noted that the increase in deviator stress during the test of the anisotropic normally consolidated sample was small. This fact indicates that a soil which is normally consolidated under $K_{0}$ conditions has a high degree of instability. However, if the soil is lightly overconsolidated, this instability is eliminated.

These authors point out that surprisingly little work has been conducted on lightly overconsolidated soils. Most of the research has been concentrated on either normally consolidated or heavily overconsolidated soils. They also pointed out that most relatively soft clays are usually lightly overconsolidated. Therefore, the need for additional research to determine the effects of light overconsolidation is apparent.

## CHAPTER III

## DESCRIPTION OF EMBANKMENT AND FOUNDATION

## Introduction

A portion of the research conducted during this study involved an analysis and design of an embankment constructed as part of an interchange on Interstate Highway 70 and U.S. Highway 75 bypass in Topeka, Kansas. This chapter describes the embankment, field investigations, soil properties, and instrumentation used prior, during, and after construction of the embankment.

## Embankment

The embankment designed during this study serves as the bridge approach embankment for the upper bridge of a three tier interchange. An overall view of the embankment is presented in Figure 3.

The embankment is approximately 1150 feet long and contains approximately 120,000 cubic yards of compacted soil. The embankment height ranges from zero to approximately forty feet. The embankment was constructed with side slopes of four feet horizontal to one foot vertical except at the high end of the embankment near the bridge approach where the slope was increased to two feet horizontal to one foot vertical. A view of this steepest portion of the embankment is presented in Figure 4. A conceptual view of a portion of the embankment is also presented in Figure 5. It can be seen that there is a cut along the toe of the


Figure 3. Embankment Constructed as Part of Interstate Highway 70 and U.S. Highway 75 Bypass Interchange


Figure 4. Steepest Portion of the Completed Embankment


Figure 5. Conceptual View of the Steepest Portion of the Embankment.
embankment at this location which extends the slope to an effective overall height of approximately fifty feet.

The embankment was constructed according to the specifications developed by the Kansas Department of Transportation (KDOT) for type B compaction and MR-5 moisture control. The specifications required that compaction continue until the roller walked out of the compacted soil and rode on the top of the lift. The water content during compaction was maintained at a minimum of 95 percent of the standard Proctor optimum water content as determined by ASTM D-698. Construction of the embankment was completed in 1976 with the major portion constructed during a two week period in July. It should be noted that, because of the special instrumentation which was used, the embankment was carefully monitored during construction to ensure that the design specifications were met.

The steepest portion of the embankment slope and the portion of the slope directly under the bridge were covered with four inch concrete riprap. This riprap can be seen in Figure 4. The riprap is used for erosion control and esthetics and has no meaningful effect on the embankment stability.

The compacted embankment soils came from excavations made in the vicinity and are therefore similar to the foundation soils described subsequently. The grain size characteristics of the embankment soils have been summarized and are presented in Table II. The physical properties of the embankment soils are summarized in Table III. The standard compaction tests on the embankment soil yielded a standard proctor density of 100 pounds per cubic foot dry weight and an optimum water content of $21.5 \%$. All tests were conducted according to KDOT standard test procedures.

TABLE II - EMBANKMENT SOIL GRAIN SIZE

| Sample Number | Percent Passing |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Sieve Analysis |  |  |  | Hydrometer Analysis |  |  |  |  |
|  | Standard Sieve Size |  |  |  | Particle Size (Millimeters) |  |  |  |  |
|  | 10 | 40 | 100 | 200 | . 05 | . 03 | . 01 | . 005 | . 002 |
| A-1 | 100 | 100 | 99 | 97 | 89 | 71 | 37 | 28 | 22 |
| B-1 | 100 | 99 | 96 | 91 | 86 | 75 | 47 | 37 | 30 |

TABLE III - PHYSICAL PROPERTIES OF EMBANKMENT SOILS

| Sample <br> Number | Liquid <br> Limit | Plastic <br> Limit | Plasticity <br> Index | Specific <br> Gravity | Classification |
| :--- | :---: | :---: | :---: | :---: | :---: |
| A-1 | 36 | 22 | 14 | 2.63 | CL |
| B-1 | 42 | 22 | 20 | 2.65 | CL |

## Foundation

The foundation soils at this location were identified as being basically fluvial in origin. Fluvial soils generally consist of sand and silt and may contain clay. Fluvial soils generally become coarser with depth.

The first step in the subsurface investigation prior to construction of the embankment was to review any available information on conditions and characteristics of the soil in the area of the proposed embankment and utilize this information to plan the field investigation. The information available to KDOT included a Soil Survey conducted for the construction of Interstate 70 and the logs of borings made for the design of the footings to be used on the proposed bridge. In addition, a Soil Survey conducted for Shawnee County by the Soil Conservation Service was reviewed.

All of the available information indicated that the subsoils were uniform throughout this area and were underlain by a virtually level shale formation at an average depth of 25 feet. Because of the wealth of information available within the immediate area of the embankment, it was believed that only one additional boring would be required. This boring was taken near the toe of the proposed embankment.

The first phase of the subsurface investigation consisted of logging the soils. This logging was accomplished by using a Bull Soil Sampler (BSS). The BSS is used to hydraulically push the sample tube into the ground to obtain a soil sample. The sample tube consists of a $11 / 8$ inch diameter tube which has a portion of one side cut away so that the soil
can be viewed while still in the tube. These samples formed the basis of the boring log which is in Appendix A.

The second phase of the subsurface investigation consisted of taking several undisturbed samples. Based on the information obtained in the first phase of the investigation, the soil profile consisted of approximately one foot of topsoil, sixteen feet of uniform silty clay, and seven feet of clay loam over shale. The topsoil was to be removed before construction of the embankment so it was not sampled. One set of samples were taken from each of the two remaining soil layers. Each set consisted of three samples.

The undisturbed samples were taken using a three inch diameter seamless steel thin walled Shelby tube. Continuous flight hollow stem augers were used for drilling to the required depths. The sample was obtained by lowering the sampler through the hollow auger at the desired depths.

After construction of the embankment, thirty additional undisturbed samples of the foundation soils were taken using a three inch diameter Shelby tube sampler. This sampling was conducted at a location near the embankment, but not within the area of influence of the embankment. Twentyone of these samples were taken at a depth of five feet, two at a depth of ten feet, three at a depth of fifteen feet, and four at a depth of twenty feet.

The laboratory analysis of these soils showed that they contain fine sand, silt, and clay with silt being the most predominant particle size. The soils classify as inorganic clay of low to medium plasticity (CL) according to the Unified Classification system.

The grain size characteristics of the foundation soils are summarized in Table IV. The physical properties of the foundation soils are summarized in Table $V$.

A total of twenty-four samples were taken from 1.2 feet to 17.6 feet in depth. Two reports of soil tests summarizing these twenty-four samples are included in Appendix $A$. The first shows the limits within which all of the tests fell. The second shows the averages of the tests from various depths within the strata. There is a slight increase in the quantity of fine sand and a corresponding decrease in the quantity of silt as depth increases. This increase in sand is typical of fluvial deposits. The variation in grain size is small and would not indicate any significant change in the soil strength.

Comparing the liquid limit (LL), plastic limit (PL) and plasticity index (PI) for the twenty-four samples from this strata, as shown in Table $V$, it can be seen that the PL remains relatively constant throughout the strata. However, there is a slight decrease in the LL which results in a decrease in the PI with depth. The average LL of the sixteen samples from a depth of approximately five feet is 39.0 . This average dropped to 38.6 for the five samples from a depth of approximately ten feet and 35.3 for the three samples from a depth of approximately fifteen feet.

A statistical analysis was performed to determine whether the tests indicated a significant change in the LL or whether this variation could be accounted for a sampling variation. At a level of significance of 0.01 , this analysis indicated that the LL variation cannot be considered to be significant when comparing samples from a depth of five feet with those from a depth of ten feet or when comparing samples from a depth of ten

TABLE IV - Foundation Soil Grain Size

| Sample Number | Depth | Percent Passing |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sieve AnalysisStandard Sieve Sizes |  |  |  | Hydrometer Analysis Particle Size (Millimeters) |  |  |  |  |
|  |  | 10 | 40 | 100 | 200 | . 05 | . 03 | . 01 | . 005 | . 002 |
| 1-1 | 5.8 | 100 | 99 | 96 | 93 | 87 | 73 | 37 | 26 | 20 |
| 2-1 | 4.5 | 100 | 100 | 98 | 94 | 87 | 72 | 38 | 28 | 18 |
| 3-1 | 4.7 | 100 | 100 | 98 | 94 | 87 | 72 | 41 | 30 | 20 |
| 4-1 | 4.7 | 100 | 100 | 99 | 95 | 88 | 74 | 38 | 29 | 22 |
| 5-1a | 4.5 | 100 | 100 | 99 | 95 | 88 | 75 | 42 | 30 | 24 |
| 5-1b | 5.1 | 100 | 100 | 99 | 95 | 88 | 73 | 37 | 28 | 21 |
| 6-1 | 4.9 | 100 | 100 | 99 | 95 | 87 | 70 | 41 | 32 | 24 |
| 7-1 | 4.5 | 100 | 100 | 99 | 97 | 91 | 76 | 39 | 29 | 22 |
| 8-1 | 4.6 | 100 | 100 | 99 | 96 | 89 | 74 | 40 | 32 | 25 |
| 13-1 | 4.7 | 100 | 100 | 98 | 94 | 88 | 73 | 38 | 28 | 22 |
| 14-1 | 4.6 | 100 | 99 | 97 | 94 | 85 | 72 | 36 | 26 | 20 |
| 15-1 | 4.5 | 100 | 100 | 99 | 96 | 90 | 76 | 41 | 30 | 24 |
| 16-1a | 4.4 | 100 | 100 | 99 | 96 | 90 | 77 | 43 | 32 | 24 |
| 16-1b | 5.1 | 100 | 100 | 98 | 94 | 88 | 73 | 39 | 30 | 24 |
| 17-1 | 4.6 | 100 | 100 | 98 | 95 | 88 | 74 | 36 | 28 | 22 |
| 18-1 | 4.7 | 100 | 100 | 98 | 95 | 88 | 74 | 40 | 30 | 24 |
| 18-2 | 9.6 | 100 | 97 | 90 | 82 | 76 | 64 | 40 | 30 | 23 |
| 18-3 | 11.0 | 100 | 97 | 90 | 82 | 76 | 68 | 43 | 34 | 28 |
| 1 T | 10.4 | 100 | 100 | 99 | 97 | 90 | 77 | 45 | 31 | 22 |
| 2 T | 11.0 | 100 | 99 | 98 | 95 | 90 | 80 | 42 | 30 | 20 |
| $3 T$ | 12.0 | 100 | 99 | 98 | 95 | 90 | 80 | 42 | 30 | 20 |
| 17-3 | 15.6 | 100 | 99 | 92 | 84 | 76 | 65 | 40 | 30 | 23 |
| 18-4 | 14.5 | 100 | 99 | 92 | 85 | 77 | 64 | 39 | 29 | 22 |
| 18-5 | 16.3 | 100 | 99 | 95 | 88 | 82 | 69 | 42 | 31 | 24 |
| 17-4 | 20.6 | 100 | 99 | 89 | 79 | 71 | 60 | 36 | 26 | 16 |
| 18-6a | 19.3 | 100 | 100 | 92 | 82 | 75 | 63 | 37 | 27 | 18 |
| 18-6b | 19.9 | 100 | 99 | 91 | 81 | 72 | 60 | 35 | 25 | 14 |
| 18-7 | 21.4 | 98 | 83 | 73 | 64 | 58 | 50 | 35 | 26 | 18 |
| $1 \mathrm{C}-3 \mathrm{~A}$ | 19.3 | 100 | 99 | 93 | 82 | 73 | 62 | 39 | 30 | 23 |
| 1C-3B | 21.0 | 100 | 99 | 92 | 82 | 73 | 61 | 38 | 29 | 22 |
| 1C-3C | 22.5 | 100 | 96 | 86 | 74 | 66 | 56 | 36 | 27 | 20 |

TABLE V - Physical Properties of Foundation Soils

| Sample Number | Liquid <br> Limit | Plastic Limit | Plasticity Index | Specific Gravity | Classification |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1-1 | 37 | 21 | 16 | 2.60 | CL |
| 2-1 | 38 | 20 | 18 | 2.63 | CL |
| 3-1 | 39 | 21 | 18 | 2.65 | CL |
| 4-1 | 39 | 21 | 18 | 2.63 | CL |
| 5-1a | 40 | 21 | 19 | 2.63 | CL |
| $5-1 \mathrm{~b}$ | 39 | 20 | 19 | 2.65 | CL |
| 6-1 | 40 | 20 | 20 | 2.63 | CL |
| 7-1 | 40 | 20 | 20 | 2.65 | CL |
| 8-1 | 39 | 20 | 19 | 2.63 | CL |
| 13-1 | 37 | 20 | 17 | 2.60 | CL |
| 14-1 | 39 | 20 | 19 | 2.72 | CL |
| 15-1 | 39 | 20 | 19 | 2.65 | CL |
| 16-1a | 40 | 20 | 20 | 2.63 | CL |
| 16-1b | 38 | 21 | 17 | 2.62 | CL |
| 17-1 | 40 | 22 | 18 | 2.60 | CL |
| 18-1 | 40 | 21 | 19 | 2.63 | CL |
| 18-2 | 42 | 20 | 22 | 2.67 | CL |
| 18-3 | 37 | 19 | 18 | 2.67 | CL |
| 1 T | 39 | 19 | 20 | 2.67 | CL |
| 2 T | 39 | 20 | 19 | 2.65 | CL |
| 3 T | 36 | 21 | 15 | 2.65 | CL |
| 17-3 | 36 | 20 | 16 | 2.63 | CL |
| 18-4 | 36 | 21 | 15 | 2.65 | CL |
| 18-5 | 34 | 20 | 14 | 2.65 | CL |
| 17-4 | 31 | 19 | 12 | 2.65 | CL |
| 18-6a | 33 | 20 | 13 | 2.63 | CL |
| 18-6b | 32 | 20 | 12 | 2.62 | CL |
| 18-7 | 32 | 20 | 12 | 2.70 | CL |
| 1C-3A | 34 | 18 | 16 | 2.62 | CL |
| 1C-3B | 36 | 20 | 16 | 2.62 | CL |
| 1C-3C | 35 | 20 | 15 | 2.65 | CL |

feet with those from a depth of fifteen feet. However, the change in LL is significant if the samples from a depth of five feet are compared with those from a depth of fifteen feet. Although this analysis does indicate that the LL and PI do decrease with depth, the change is very slight and would not indicate any significant change in strength with depth.

## Instrumentation

The instrumentation used during the construction of the embankment consisted of piezometers to measure pore water pressure and an inclinometer to measure any movement of the foundation soil. The locations of the instrumentation are shown in Figure 6.

The piezometers were the pneumatic pressure type which were manufactured by the Slope Indicator Company. The piezometer tips were surrounded by sand and placed at the points shown in Figure 6. The drill hole was sealed using commercial bentonite pellets. The tips were made from a porous material with diaphragms and tubes for containing the nitrogen gas used in the portable readout. The support equipment consisted of a gas supply, metering device, and various gauges. When a reading was taken, gas from the readout device passed to the tip where it opened the diaphragm and was vented to the atmosphere. The gas flow was then stopped and the pressure dropped until the diaphragm closed causing the escape of gas to stop. At this point, the gas pressure on one side of the diaphragm was equal to the water pressure on the other side of the diaphragm, so measurement of the gas pressure gave the measurement of the pore pressure directly.


Figure 6. Conceptual View of the Embankment Showing the Location of the Instrumentation.

The inclinometer was also manufactured by the Slope Indicator Company. The inclinometer consisted of a probe which is lowered into a grooved aluminum casing, and a readout device which is connected to the probe by wires. The probe consisted of a pendulum and variable resistor which serves as part of a Wheatstone Bridge. The readout device made up the remainder of the Wheatstone Bridge.

The probe was lowered down the casing and the inclination of the casing was correspondingly determined at various intervals. The inclination was used to compute the embankment deflections. In this way, any movement in the soil which would result in the movement of the casing was measured.

## CHAPTER IV

## TEST RESULTS

The results of the triaxial tests are presented in the first section of this chapter. The pore pressure and deformations measured by the field instrumentation are presented in the last section.

## Triaxial Test Results

The test results are presented in three groups: foundation samples taken before construction, embankment samples taken during construction, and foundation samples taken after construction. The last group is further divided into samples tested by the Kansas Department of Transportation and those tested by the University of California at Berkeley.

## Foundation Samples Taken Before Construction

This group consists of two sets of samples with three samples per set. The locations where the samples were taken are shown on the boring log presented in Appendix A.

The triaxial test results are shown in Figures 7 and 8. A summary of the test results is presented in Table VI. Samples $1-T, 2-T$, and $3-T$ were tested by a modified test procedure consisting of the following steps: saturation on the vacuum saturator, consolidation to the confining stress with free drainage and then loaded in the undrained condition. Samples 1C-3A, 1C-3B, and 1C-3C were tested according to standard


Figure 7. Triaxial Test Results, Samples 1T, 2T, 3T


Figure 8. Triaxial Test Results, Samples 1C-3A, 1C-3B, 1C-3C

TABLE VI - TRIAXIAL TEST RESULTS, FOUNDATION SOILS

| Sample <br> Numbers | Depth <br> (Ft.) | Chamber Pressure <br> Range (TSF) | $c$ | $\phi$ | $c^{\prime}$ | $\phi^{\prime}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 T, 2 T, 3 T$ <br> $1 C-3 A, 1 C-3 B$ <br> $1 C-3 C$ | $10.1-12.4$ | $0.5-2.5$ | 0 | 14 | 180 | 22.5 |

TABLE VII - TRIAXIAL TEST RESULTS, EMBANKMENT SOILS

| Sample <br> Numbers | Location | Chamber Pressure <br> Range (TSF) | c | $\phi$ |
| :--- | :---: | :---: | :---: | :---: |
| A-1, A-2, A-3 <br> $\mathrm{B}-1, \mathrm{~B}-2, \mathrm{~B}-3$ | Elev. 910.5 | Elev. 919 | $0.5-2.5$ | 3,338 |

Kansas Department of Transportation test procedures. These procedures include saturating the samples on the vacuum saturator, using backpressure saturation, and testing the samples in the consolidated undrained condition with pore pressure measurements.

## Embankment Samples Taken During Construction

The group consisted of two sets of samples with three samples per set. The samples were taken from the embankment at two different elevations as the embankment was constructed.

The results of the triaxial tests conducted on these samples are presented in Figures 9 and 10. A summary of the test results is also presented in Table VII. These tests were conducted using the in-situ water content under the unconsolidated undrained condition with pore pressure measurement taken. The strain rate was adjusted to provide a constant rate of strain of two percent per hour.

## Foundation Samples Taken After Construction

After construction of the embankment, thirty additional undisturbed samples were taken from the foundation soils at a location adjacent to the embankment. The thirty samples were tested in nine sets with from two to six samples per set. The results of these tests are presented in Figures 11 through 19. The results are also summarized in Table VIII.

## Field Instrumentation Results

The results of the field instrumentation are presented in Figures 20 through 22. Figure 20 presents the pore pressure measurements and the


Figure 9. Triaxial Test Results, Samples A-1, A-2, A-3.


Figure 10. Triaxial Test Results, Samples B-1, B-2, B-3.


Figure 11. Triaxial Test Results, Samples 14-1, 15-1, 16-1a.


Figure 12. Triaxial Test Results, Samples 17-1, 16-1b, 18-1, 13-1.


Figure 13. Triaxial Test Results, Samples 1-1, 7-1, 8-1.


Figure 14. Triaxial Test Results, Samples 2-1, 3-1, 4-1, 5-1a, 5-1b, 6-1.


Figure 15. Triaxial Test Results, Samples 18-2, 18-3.


Figure 16. Triaxial Test Results, Samples 17-3, 18-4, 18-5.


Figure 17. Triaxial Test Results, Samples 18-6a, 18-6b, 18-7, 17-4.


Figure 18. Triaxial Test Results, Samples 9-1-2, 11-1-2.


Figure 19. Triaxial Test Results, Samples 12-1-3, 9-1-3, 11-1-1.

TABLE VIII - TEST RESULTS, POST CONSTRUCTION SAMPLES

| Sample Numbers | Depth (Ft.) | Type Test | Strain Rate (\%/hr.) | Pressure Range (TSF) | $\begin{gathered} \mathrm{c} \\ (P S F) \end{gathered}$ | $\begin{gathered} \phi \\ \text { (degrees) } \end{gathered}$ | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TESTS BY KANSAS DEPARTMENT OF TRANSPORATION |  |  |  |  |  |  |  |
| $\begin{aligned} & 14-1, \quad 15-1 \\ & 16-1 a \end{aligned}$ | 5 | CU | 2 | 0.5-1.5 | 2,719 | 7 | Vacuum Saturation |
| $\begin{array}{ll} 13-1, & 16-1 b \\ 17-1, & 13-1 \end{array}$ | 5 | CU | 2 | 0.5-2.0 | 695 | 20 | Back Pressure Saturation |
| 1-1, 7-1, 8-1 | 5 | UU | 5 | 0.5-2.0 | 935 | 16 | As Cut Mois ture |
| $\begin{aligned} & 2-1,3-1,4-1 \\ & 5-1 a, 5-1 b \\ & 6-1 \end{aligned}$ | 5 | UU | 60 | 0.5-2.5 | 1,430 | 12 |  |
| 18-2, 18-3 | 10 | UU | 60 | 0.5-1.5 | 1,421 | 0 |  |
| 17-3, 18-4 | 15 | UU | 60 | 0.5-1.5 | 322 | 7 |  |
| $\begin{aligned} & 17-4,18-6 a \\ & 18-6 b, 18-7 \end{aligned}$ | 20 | UU | 60 | 0.5-2.0 | 646 | 0 |  |

TESTS BY UNIVERSITY OF CALIFORNIA AT BERKELEY

| $9-1-2,11-1-2$ | 5 | $U V$ | $*$ | $1.02-2.05$ | 2,473 | 0 |  |
| :--- | :--- | :--- | :--- | ---: | ---: | ---: | ---: |
| $12-1-3,9-1-3$ <br> $11-1-1$ | 5 | CU | $* *$ | $0.51-1.02$ | 843 | 25 |  |

* controlled stress test (strain equaled $20 \%$ in 30 minutes or less)
** controlled stress test (strain equaled $20 \%$ in 3 hours or less)

a. Embankment Construction

b. Measured Pore Pressure

Figure 20. Pore Pressure Measurements and Embankment Construction as Related to Construction Time.
DEFLECTION (ins.)


Figure 21. Deflection of Inclinometer Casing.






Figure 22. Settlement Measured at the Inclinometer Joints.
embankment height expressed as a function of the construction time. Piezometer number one was located at a depth of five feet. The water level had dropped below the five foot level by the time the piezometer was installed and therefore no significant pore pressure was ever measured at this depth. Piezometers two, three, and four did show an increase in pore pressure within the embankment as construction progressed.

The deformation of the soil was measured by the deflection of the inclinometer casing as described previously. The deflection of the inclinometer casing, expressed as a function of time, is presented in Figure 21. As can be seen in this figure, the top of the inclinometer casing moved horizontally almost four inches as the embankment was constructed. In addition, some movement has taken place since completion of the construction sequence. It can also be seen that approximately the upper ten feet of the casing stayed essentially vertical while the lower portion of the casing underwent major deformation to a depth of approximately twenty-two feet. The deflected shape of the inclinometer casing is of considerable significance to this study since it confirms that the upper soils that had undergone desiccation did not deform although the lower soils did deform considerably.

Figure 22 shows the settlement of the inclinometer casing as measured at its joints. It is important to note that the settlement was less than one inch for any of the joints. Another important point is that the top two joints moved down equal amounts, thus indicating that no consolidation had taken place in the top ten feet. However, each of the remaining joints moved closer together with the greatest relative movement being
between joints three and four, thus indicating that the maximum consolidation occurred in the strata between sixteen and twenty-one feet.

## CHAPTER V

## STABILITY AND DEFORMATION ANALYSIS

Presented in this chapter are the results of two different methods of analysis performed on the embankment. The first method of analysis presented is that of a conventional slope stability procedure utilizing a circular arc form of failure. The second method consists of a slope stability analysis using a method of finite elements. The effect of desiccation on the deformation and stability of the embankment as determined by both methods of analysis is presented and discussed.

## Slope Stability Analysis

A simplified form of the method of stability analysis as developed by Bishop (6) was used. In this analysis, a circle representing a possible failure surface was passed through the embankment and the area above the circle was divided into vertical slices. The weight of each slice was computed and resolved into components, with one component acting along the potential failure surface and the other component acting perpendicular to the potential failure surface. The weight component which acts perpendicular to the potential failure surface, when multiplied by the coefficient of friction $(\tan \phi)$, is equal to the frictional resistance which resists overturning of the slice. The arc length which forms the lower boundary of the slice multiplied by the cohesion is equal to the cohesional resistance to sliding. The total driving force of the potential slide equals
the sum of the weight components acting along the failure surface for all of the slices. The total resisting force is equal to the summation of the cohesional and frictional resistance for all of the slices. The ratio of the resisting forces divided by the driving forces is the factor of safety against sliding for the embankment.

The computational portion of the analysis was performed utilizing the ICES Lease (7) computer program. This program was developed to analyze the embankment as a layered system. Numerous potential failure circles are generated until the circle is found which yields the minimum factor of safety.

Three slope stability analyses of the embankment will be presented. The first and second analyses are similar, except that the first analysis does not consider the effects of desiccation while the second analysis does. The third analysis is the analysis used to monitor stability of the embankment during construction.

As presented and discussed in Chapter III, it was determined that there was a slight change in the liquid limit and the percentage of sand with depth. It is common for such changes to occur within a stratum of soil. Sampling is therefore normally conducted near the middle of the soil stratum and the test results are considered to be the average for that stratum. In the first analysis, the data for the upper stratum was obtained from samples taken just below the desiccated zone. Therefore, this analysis did not take into account the increased strength in the upper part of the strata which resulted from desiccation.

After the retesting as described in Chapter III, two analyses were performed. The total stress analyses were performed, utilizing the
soil strength as determined from unconsolidated undrained triaxial tests.

In the first analysis, the foundation was considered to consist of two soil strata with the strength in each assumed constant. The triaxial test results presented in Figures 14 and 15 were used to represent these strata. The triaxial test results presented in Figure 8 were used to represent the embankment soils. The analysis did not consider the increased strength near the ground surface as a result of desiccation. The slip circle which produced the lowest factor of safety is presented in Figure 23.

For the second analysis, the upper stratum was divided into three layers and the lower stratum was again considered to be one layer. Therefore, the foundation was divided into a total of four layers to account for the variation in strength with depth. A total stress analysis was performed utilizing the triaxial test results presented in Figures 12, 13, 14, and 15 . The slip circle which produced the lowest factor of safety using this method of analysis is presented in Figure 24.

As can be seen in Figure 23, the first analysis which omitted the effects of desiccation yielded a factor of safety of 0.89 . A factor of safety which is below one indicates that the embankment is unstable. Thus, the first method of analysis which did not consider the effect of desiccation indicates that the embankment was unsafe and could lead to failure. However, when the increased strength as a result of desiccation was taken into account as in the second analysis, the factor of safety


Figure 23. Slope Stability Analysis, Not Considering Desiccation


Figure 24. Slope Stability Analysis, Considering Desiccation.
was increased to 1.07 , as shown in Figure 24, thus indicating the embankment stability was marginal.

It should be noted that the previously described analyses assumed the worst case loading conditions; this implies that there was no dissipation of excess pore pressure during construction. The third analysis was therefore used to monitor the actual stability of the embankment during construction. This analysis utilized the measured pore pressure presented in Figure 18, in an effective stress analysis. The minimum factor of safety utilizing an effective stress concept was computed to be 1.30. Therefore, the embankment was constructed without any delay since the buildup of excess pore pressure did not reduce the strength below an acceptable level. The measured pore pressure was not as large as anticipated because the water table had been lowered from 3.6 to 8.0 feet below the soil surface as a result of very dry weather in addition to dewatering of the excavations for the bridge piers.

## Deformation by Finite Element Analysis

The deformation analysis was performed using the finite element computer program ISBILD (2). This program was developed at the University of California at Berkeley under the sponsorship of the National Science Foundation. The program was developed for the purpose of analyzing the static stresses and strains within an embankment and embankment foundations. The analysis is performed by dividing the structure into a finite number of elements. The individual elements are defined by entering the boundary nodal coordinates and the number of elements desired into the computer program and allowing an internal coordinate generator to define the nodal
coordinates. If boundary conditions prevent movement of certain nodal points in either the ' $X$ ', ' $Y$ ' or both directions, this can be specified as a boundary condition code in the nodal point description.

The program is set up so that all elements are entered as rectangles. By specifying the same nodal point as two corners of the rectangle, a triangle will be generated. A method of utilizing data from conventional laboratory tests is used to describe the stress-strain characteristics of soil. This is accomplished by fitting a hyperbola to the stress-strain curve as developed by Wong and Duncan (8). The description of the material properties then consists of entering the parameters to describe a hyperbola ( $K, N$ ) which is used to describe the stress-strain characteristics of the soil. Other soil parameters which are entered include the unit weight (UNIT WT), cohesion intercept (C), friction angle (PHI), and Poisson ratio parameters ( $D, G, F$ ). All of these parameters can be determined from triaxial tests as described in Chapter IV. An example of the input data required to perform this analysis is included in Appendix B.

The program simulates the construction of the embankment by computing the initial foundation stresses and then superimposing the forces on each node corresponding to those developed as a result of the addition of one layer of embankment. The corresponding stresses and strains for all of the elements are determined in two iterations. The first iteration consists of simulating the weight of the newly placed embankment to the foundation soil, however, the newly placed embankment is considered to have no strength. The stress and corresponding strains are computed for this condition. The second iteration considers the strength of the newly placed embankment by modifying the stiffness of the elements used to
simulate the embankment. The element stresses and nodal displacements are then recomputed. This process is repeated until the placement of all the embankment layers has been simulated. The element stresses and deformations are printed at the completion of each second iteration.

An example of the output from the computer program is presented in Appendix C. The output consists of nodal displacements and stresses as computed for each element. Only the values corresponding to those of the final layer are presented in Appendix C.

The final displacement consists of those in both $X$ and $Y$ directions (DELTA- $X$, DELTA- $Y$ ), the total displacements in both the $X$ and $Y$ directions (X-DISP, $Y$-DISP), and the total resultant displacement (TOTAL). The final stresses consist of the normal stress in the $X$ and $Y$ directions (SIG-X, SIG-Y), principal normal stresses (SIG-1, SIG-3), shearing stress in the $X-Y$ direction (TAU-XY), maximum shearing stresses (TAU-MAX), angle of maximum shearing stress (THETA), ratio of principal stresses (SIG1/SIG3), the portion of the available shear strength which is currently mobilized (SLPRES), and the maximum portion of the strength which has been mobilized (SLMAX).

In addition to the output previously described, supporting data is printed for each layer as shown in Appendix D. This output consists of the elastic modulus (ELAS MOD), bulk modulus (BULK MOD), shear modulus (SHEAR MOD), Poisson ratio (POIS), strain in the $X$ and $Y$ directions (EPS-X, EPS-Y), principal strains (EPS-1, EPS-3), unit shearing strains in the XY direction (GAM-XY) and principal unit shearing strain (EPS-1, EPS-3, GAMMAX).

## First Finite Element Analysis of the Embankment

In the initial attempt to analyze the embankment, the foundation and the embankment were simulated as separate soils. The element grid pattern used in this analysis is presented in Figure 25. The lower five layers represent the foundation soil and the upper eight layers represent the embankment. As stated previously, the program simulates the placement of the embankment one layer at a time. The final shape of the grid as computed by the program is presented in the overlay for Figure 25.

The vertical line through the foundation soil below the toe of the slope represents the location of the inclinometer casing. Table IX presents computed and measured deflections at various depths along this line.

It should be noted that the excavation at the toe of the fill slope had not been simulated. This could have resulted in larger computed deflections than those shown in the overlay for Figure 25. However, this analysis was not conducted since the computed deflections already greatly exceeded those measured in the field.

## Second Finite Element Analysis of the Embankment

The finite element analysis was again performed utilizing the soil parameters obtained from the tests on soil samples taken adjacent to the completed embankment. Four soils were used to simulate the foundation. In this way the variation in strength as a result of desiccation of the upper soil was taken into account.

The computed deflections are presented in Table $X$ along with those measured by the slope inclinometer. Although the second analysis did not


FIGURE 25. Grid for Finite Element Analysis

TABLE IX - DEFLECTIONS COMPUTED NOT CONSIDERING DESICCATION

| Depth | Computed <br> Deflection (in.) | Measured <br> Deflection*(in.) |
| :---: | :---: | :---: |
| 0 | 57.3 | 5.3 |
| 5 | 9.8 | 4.9 |
| 10 | 5.1 | 3.4 |
| 15 | 2.4 | 1.6 |
| 20 | 1.1 | 0.04 |
| 26 | 0.0 | -0.03 |
|  |  | *November 15, 1977 |

TABLE X - DEFLECTIONS COMPUTED CONSIDERING DESICCATION

| Depth | Computed <br> Deflection (in.) | Measured <br> Deflection (in.) |
| :---: | :---: | :---: |
| 0 | 8.70 | 5.3 |
| 5 | 8.59 | 4.9 |
| 10 | 8.51 | 3.4 |
| 15 | 6.78 | 1.6 |
| 20 | 4.53 | 0.04 |
| 26 | 0.00 | -0.03 |

accurately predict the actual magnitude of deflection for the inclinometer, the difference could be attributed to the difference between laboratory and in situ strength parameters.

## Effects of Desiccation on Deformation and Slope Stability

A comparison is presented in Figure 26 between the deflections measured by the slope inclinometer and those computed by the use of the finite element analyses. It should be noted that the first analysis indicated that the maximum deflection would occur at the ground surface with considerable deformation within the top ten feet. The actual measurements indicated that the top ten feet of the inclinometer casing remained nearly vertical, but shifted over relative to the bottom of the casing. The major deformation was measured between 10 and 20 feet. It can be seen in Figure 26 that the second analysis predicted the general shape of the deflected inclinometer.

These analyses show the important effect which desiccation has on the deformation. If the soil was normally consolidated, it would be expected that the maximum deformation would occur in the upper strata. The first analysis predicted this type of movement with the predicted displacement decreasing rapidly with depth. However, desiccation caused the upper portion of the soil to be stiffer than the soil below and therefore the soil particles in this portion moved very little relative to each other. The second analysis predicted a deformed shape very similar to that actually measured by the inclinometer.

By properly accounting for desiccation in deformation analyses, more accurate estimates of the deformation can be made. Since accounting for


Figure 26. Predicted and Measured Deflections.
desiccation will reduce the magnitude of the expected deformation, the effect on underground structures will not be as severe as would be predicted if desiccation were not considered. Therefore, considerable cost savings may be possible. For example, most underground structures may not be able to withstand the deflection of fifty-seven inches as predicted by the analysis omitting the effects of desiccation. However, they may not be adversely affected by movement of only eight inches as predicted in the analysis considering desiccation. Therefore, the added cost of relocating such structures may be eliminated.

When desiccation was considered in the slope stability analysis, an increase in the factor of safety against sliding from 0.89 to 1.07 was obtained. This resulted in an increase of approximately 25 percent in the factor of safety. By properly accounting for desiccation in the analysis of embankments, it will be possible to design embankments with steeper side slopes, thus providing for additional cost savings.

## CHAPTER VI

## IDENTIFYING AND ACCOUNTING FOR DESICCATION

The research conducted during this study has shown that the consolidation which results from desiccation has an important influence on the stability of embankments and on the corresponding deformation of the foundation soils. Examples of how desiccation was accounted for in the stability analysis were presented in Chapter V. This was accomplished primarily by dividing the foundation soils into several layers and assigning appropriate strength parameters to the various layers.

The most important step in accounting for desiccation is to recognize the variations in strength and to design the subsurface exploration program such that any variation can be adequately identified. This chapter describes several parameters which should be used in identifying desiccated soils as determined by this study.

## Identifying Desiccation

Visually inspecting the soil and recognizing that desiccation has occurred can be very difficult. In the locations examined in this study, the soil had desiccated to a depth of over ten feet at some time in the past. However, at the time of the initial investigation, the groundwater table was at a depth of less than four feet. Since the foundation soil existed in the saturated state, it made recognition of the desiccated soils very difficult.

Moisture tests can aid in determining the depth of desiccation. When desiccation occurs, the negative pore pressure causes consolidation of the soil and therefore a smaller void ratio. When the soil is then resaturated, the water content in the desiccated zone will be lower than for soils in the same stratum, but below the desiccated zone. Therefore, when moisture tests show a sample of soil to have a lower water content than other samples of the soil from lower elevations, the lower water content is a good indication that desiccation has occurred.

The average of the moisture tests run on soil samples from various depths are presented in Table XI. These tests were run on samples taken during the resampling program used for the second finite element analysis. At the time these samples were taken, groundwater stood at a depth of about eight feet.

It can be noted that there is a pronounced increase in the water content between the ten and fifteen foot depths which corresponds to the change from a desiccated to a nondesiccated soil. Since the tests at both ten feet and fifteen feet were below the water table, the change in water content relates directly to the change in void ratio. It should be noted that an increase in water content with depth does not implicitly imply an overconsolidated soil.

A soil index related to the Atterberg Limits which can also be used as an indication of desiccation is the liquidity index. The liquidity index is defined as the difference between the natural water content and the plastic limit divided by the plasticity index. The change in liquidity index is directly related to the change in water content for the soil stratum. For desiccated soils, the liquidity index will be small and

TABLE XI - MOISTURE CONTENTS AT VARIOUS DEPTHS

| Depth <br> (Feet) | Water Content <br> (\% of Dry Weight) |
| :---: | :---: |
| 5 | 22.7 |
| 10 | 24.5 |
| 15 | 30.0 |
| 20 | 29.75 |

TABLE XII - LIQUIDITY INDEX AT VARIOUS DEPTHS

| Depth | Liquidity Index |
| :---: | :---: |
| 5 | 12 |
| 10 | 25 |
| 15 | 65 |
| 20 | 74 |

TABLE XIII - DENSITY AT VARIOUS DEPTHS

| Depth <br> (Feet) | Average Density <br> (Pounds/Ft3) |
| :---: | :---: |
| 5 | 103 |
| 10 | 102 |
| 15 | 93 |
| 20 | 92.5 |

can be negative. For nondesiccated soil, this index will be positive and much larger than for desiccated soils. The liquidity indices for samples from various depths are presented in Table XII. It can be seen that there is an increase of forty in the liquidity index between the ten and fifteen foot depth.

Another factor which could be used to help identify the possible existence of a desiccated zone is the soil density. When desiccation occurs, the negative pore pressure causes consolidation of the soil and therefore an increase in the density. The average densities of the soil at various depths are presented in Table XIII. As in the previously described results, there is a pronounced change at the boundary between the desiccated and nondesiccated zone.

Of the three tests evaluated for identifying the desiccated zone in the field, the density test is probably the best available. However, the density test is much more difficult and also expensive to run than the moisture test. Liquidity index would be very difficult to determine in the field and therefore has less potential as an aid in identifying desiccation so that the sampling locations can be chosen.

The other tests which could be run in the field include Dutch Cone penetrometer, hand van shear, and pocket penetrometer tests. Hand vane shear and pocket penetrometer tests would require removing undisturbed samples for testing. The test results could be plotted to show any variation in strength which may exist as a result of desiccation. Further research should be conducted to evaluate the potential of these tests in identifying desiccation.

## CHAPTER VII

## CONCLUSIONS AND RECOMMENDATIONS

The primary objective of this research was to determine the effects of desiccation on the deformation and stability of an embankment. Several other important items were also determined. These items included the evaluation of various methods for recognizing desiccated zones of soil. The research objectives were accomplished by comparing the actual deformations which took place under an embankment constructed by the Kansas Department of Transportation with those predicted by using several methods of analysis. From the results obtained from this study, the following can be concluded:

1. Desiccation causes the magnitude of the deformation of the foundation soils to be altered. In the embankment investigated, the maximum deflection predicted without accounting for desiccation in the analysis exceeded the actual deflection by over an order of magnitude. When the effects of desiccation was accounted for in the analysis, the predicted deflection exceeded the measured deflection by only sixty-four percent. The analysis conducted without considering desiccation predicted that the maximum deformation should occur in the upper portion of the foundation soil; however, little deformation was actually measured in this portion.
2. The consideration of desiccation increases the overall stability calculated for embankments constructed over soft foundations. For the embankment analyzed, the computed minimum factor of safety against sliding was increased by approximately 25 percent when desiccation was accounted for in the analysis.
3. Since it is very difficult to recognize the existence of desiccated zones if the groundwater has risen and the soils are resaturated, tests should be performed to aid in their identification. The use of moisture tests, Atterberg limits, and soil density tests are suited for this purpose. The desiccated zone will have a higher density and lower water content than a corresponding zone which is not desiccated. The liquidity index can be used to identify the desiccated zone since this index is sensitive to a variation in natural water content.
4. Reasonably accurate analyses can be performed on desiccated soils by recognizing the variation in strength and choosing the sampling locations in such a way that the soil conditions can be adequately determined and modeled.

With respect to further research regarding the effects of desiccation on deformation and embankment stability, the following recommendations are made:

1. Work should be conducted to further develop procedures for use in the recognition of desiccated zones. Further development of tests are needed which can be used during the initial phase of the field investigation, the results of which are available immediately to aid in the design of the subsurface exploration
program. Such tests as Dutch Cone penetrometer, pocket penetrometer, and hand vane shear should be evaluated in respect to the identification of desiccated zones.
2. Any further work regarding desiccation should include determination of the overconsolidation ratio of the desiccated soil. This will facilitate correlation with other work recorded in the literature.

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## APPENDIX A

LOG OF BOREHOLE AND REPORT OF SOIL TESTS


## REPORT OF SOIL TESTS



| SAMPLE <br> NUMBER | STATION | OIST. \& | DEPTH | L.L.L. | L.P.L. | $*$ <br> P.I. | O RET. <br> ON NO.IO PPASS. GRAV | CLASSI- <br> FICATION |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | 37.3 | 20.2 | 17.1 |  | 2.64 |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

REMARKS* Average test results.

- —————————————————


## REPORT OF SOIL TESTS



PHYSICAL PROPERTIES OF PORTION PASSING NO.___SIEVE

| SAMPLE NUMBER | STATION | OIST, \$ | DEPTH | LL. | $$ | $\begin{array}{r} \text { * } \\ \text { P. } \\ \hline \end{array}$ | \% RET. ON NO. 10 | SPEC. GRAV PASS. NO. 10 | CLASSIFICATION |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 5' | 39.0 | 20.5 | 18.5 | 0 | 2.63 | SICL |
|  |  |  | $10^{\prime}$ | 38.6 | 19.8 | 18.8 | 0 | 2.66 | Sic |
|  |  |  | $15^{\circ}$ | 35.3 | 20.3 | 15.0 | 0 | 2.64 | $c$ |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

REmARKs * Average test results.

## APPENDIX B

INPUT FOR THE FINITE ELEMENT COMPUTER PROGRAM

TOTAL NIMBEP OF ELEMENTS**********155 TOTAL NUMBER OF NODES * ************180 NUMBER CF ELEMENTS IN FCUNDATION:* 95 NUMBEP OE MDDES IN FOUNDAT ION***** 120 NUMBER CF ©REEXISTING EL SMENTS*\#** 0 WUMER TF PRFEXISTING NCDES******* 0 NUMBER OF DIFF. MATERIALS********* 5 NU.ABFP CF CONSTRUCTION LAYERS***** 8 NUMGER OF LCAC CASES************** 0
final results are not punched dut

MATERIAL DRCDERTY DATA
ATMOSPHEPIC PRESSURE = 2.1160

| MAT | UNIT WT | K | monul us KUR | $N$ | 0 | POISSON RATIC | F | c | PHI | FAIL.RATIC | KO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.1200 | 97.0 | 290.9 | -1.1733 | 0.0 | 0.5000 | c. 0 | $0 . t 460$ | 0.0 | 0.9550 | 1.0000 |
| 2 | 0.1210 | 57.9 | 173.6 | 0.2724 | 0.0 | 0.5000 | 0.0 | 0.3220 | 7.0700 | 0.9240 | 1.0000 |
| 3 | 0.1250 | 445.5 | 1336.5 | -0.1728 | 0.0 | C. 5005 | 9.3 | 1.4210 | 0.0 | 1.0210 | 1.0000 |
| 4 | 2. 1260 | 187.2 | 561.6 | 0.2445 | 0.0 | 0.5000 | 0.0 | 1.4300 | 11.5800 | 0.9527 | 1.0000 |
| 5 | 0.1190 | 102.2 | 306.6 | 0.2650 | 0.0 | 0.5350 | 2.0 | 3.3400 | 15.0000 | 0.6011 | 0.0 |

NOTAL POINT IA:PUT OATA

| NODE <br> NUMPER | NODAL POINT $X-O R n$ | $\begin{aligned} & \text { COOROINATES } \\ & Y \rightarrow O R D \end{aligned}$ | $\underset{X X}{\text { B. } C_{X}} \mathrm{COOE}_{Y}^{\mathrm{CO}}$ |
| :---: | :---: | :---: | :---: |
| 1 | J. 0 | 878.000 | 11 |
| 2 | 13.003 | 878.050 | 11 |
| 3 | 20.003 | 878.0.92 | 1 |
| 4 | 30.003 | 878.050 | 11 |
| 5 | 40.000 | 878.000 | 11 |
| 6 | 50.000 | 878.000 | 11 |
| 7 | 60.000 | 878.300 | 11 |
| 8 | 70.000 | 878.000 | 11 |
| 9 | 78.005 | 378.000 | 11 |
| 10 | 98.000 | 878.000 | 1 |
| 11 | 98.000 | 878.000 | 1 |
| 12 | 158.005 | 878.000 | 1 |
| 13 | 118.300 | 878.200 | 1 |
| 14 | 128.000 | 878.000 | 11 |
| 15 | 138.009 | 878.000 | 11 |
| 16 | 148.005 | 878.000 | 11 |
| 17 | 158.000 | 878.000 | 11 |
| 18 | 168.000 | 878.300 | 11 |
| 19 | 175.003 | 878.000 | 11 |
| 20 | 132.000 | 879.000 | 1 |
| 21 | C. 0 | 884.000 | 0 |
| 22 | 10.000 | 884.200 | c 0 |
| 23 | 20.005 | 884.000 | 0 - |
| 24 | 30.003 | 884.000 | c 0 |
| 25 | 40.000 | 884.000 | 00 |
| 26 | 50.000 | 984.000 | 00 |
| 27 | 65.005 | 884.000 | 0 \% |
| 28 | 70.000 | 884.000 | $c \quad c$ |
| 29 | 78.000 | 884.300 | c 0 |
| 30 | 88.003 | 884.030 | 00 |
| 31 | 98.000 | 884.0.50 | 00 |
| 32 | 108.005 | 884.000 | c 0 |
| 33 | 118.050 | 884.039 | $=0$ |
| 34 | 128.000 | 884.050 | c 0 |
| 35 | 138.000 | 884.000 | 00 |
| 36 | 148.035 | 884.000 | 00 |
| 37 | 158.000 | 884.000 | 00 |
| 38 | 168.000 | 3R4.030 | c 0 |
| 39 | 175.0.) | 884.030 | c 0 |
| 40 | 182.000 | 384.C50 | 10 |
| 41 | $0 . C$ | 889.000 | 10 |
| 42 | 10.cos | 389.0.30 | 00 |
| 43 | 20.005 | 889.500 | 00 |
| 44 | 30.003 | 889.090 | 00 |
| 45 | 40.025 | 899.000 | 0 0 |
| 46 | $5 \mathrm{C.cos}$ | 889.000 | 00 |
| 47 | 60.030 | 889.009 | c 0 |
| 48 | 72.303 | 899. 209 | $c \quad 0$ |
| 49 | 78.003 | RR9.350 | 0 O |
| 50 | 88.000 | 389.000 | c 0 |
| 51 | 98.035 | 854.350 | 20 |
| 52 | 106.000 | 889.000 | c $\quad 9$ |
| 53 | 118.00) | 889.650 | 00 |
| 54 | 128.009 | 889.350 | - 0 |
| 55 | 138.005 | 889.000 | 0 0 |




| 176 | 182.000 | 939.000 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 177 | 158.090 | 944.000 | 0 | 0 |
| 178 | 168.000 | 944.000 | 0 | 0 |
| 179 | 175.000 | 944.000 | 0 | 0 |
| 180 | 182.000 | 944.000 | 1 | 0 |

four nodfs smild flement gata

| $\begin{aligned} & \text { ELET } \\ & \text { VO. } \end{aligned}$ | COnnfctec |  |  | ES | matl | EL FMENT CFNTER | COOROINATES |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | J | K | $L$ | NO. | X -OPD | $Y \rightarrow$ RD |
| 1 | 1 | 2 | 22 | 21 | 1 | 5.000 | 881.000 |
| 2 | 2 | 3 | 23 | 22 | 1 | 15.000 | 881.000 |
| 3 | 3 | 4 | 24 | 23 | 1 | 25.00C | 881.000 |
| 4 | 4 | 5 | 25 | 24 | 1 | 35.00C | 881.000 |
| 5 | 5 | 6 | 26 | 25 | 1 | 45.00C | 881.000 |
| 6 | 6 | 7 | 27 | 26 | 1 | 55.000 | 881.000 |
| 7 | 7 | 8 | 28 | 27 | 1 | 65.000 | 881.200 |
| 8 | 8 | 9 | 29 | 28 | 1 | 74.000 | 881.000 |
| 7 | 0 | 10 | 30 | 29 | 1 | 83.00C | 881.000 |
| 13 | 10 | 11 | 31 | 30 | 1 | 93.000 | 881.000 |
| 11 | 11 | 12 | 32 | 31 | 1 | 103.000 | 881.000 |
| 12 | 12 | 13 | 33 | 32 | 1 | 113.000 | 881.000 |
| 13 | 12 | 14 | 34 | 33 | 1 | 123.000 | 881.000 |
| 14 | 14 | 15 | 35 | 34 | 1 | 133.000 | 881.000 |
| 15 | 15 | 16 | 36 | 35 | 1 | 143.00 C | 881.000 |
| 16 | 16 | 17 | 37 | 36 | 1 | 153.000 | 881.003 |
| 17 | 17 | 18 | 38 | 37 | 1 | 163.200 | 881.000 |
| 19 | 18 | 19 | 39 | 38 | 1 | 171.500 | 881.000 |
| 19 | 19 | 2 C | 42 | 39 | 1 | 178.500 | 881.000 |
| 23 | 21 | 22 | 42 | 41 | 1 | 5.000 | 886.500 |
| 21 | 22 | 23 | 43 | 42 | 1 | 15.00 C | 886.500 |
| 22 | 23 | 24 | 44 | 43 | 1 | 25.000 | 886.500 |
| 23 | 24 | 25 | 45 | 44 | 1 | 35.900 | 886.500 |
| 24 | 25 | 26 | 46 | 45 | 1 | 45.000 | 886.500 |
| 25 | 26 | 27 | 47 | 46 | 1 | 55.000 | 886.505 |
| 26 | 27 | 28 | 48 | 47 | 1 | 65.000 | 886.505 |
| 27 | 28 | 29 | 49 | 48 | 1 | 74.000 | 886.500 |
| 28 | 29 | 30 | 59 | 49 | 1 | 83.005 | 886.500 |
| 29 | 30 | 31 | 51 | 50 | 1 | 93.000 | 886.505 |
| 30 | 31 | 32 | 52 | 51 | 1 | 103.000 | 886.500 |
| 31 | 32 | 33 | 53 | 52 | 1 | 113.20C | 88t. 500 |
| 32 | 33 | 34 | 54 | 53 | 1 | 123.000 | 986.5CD |
| 33 | 34 | 35 | 55 | 54 | 1 | 133.000 | $886.50 n$ |
| 34 | 35 | 36 | 56 | 55 | 1 | 143.000 | 886.500 |
| 35 | 36 | 37 | 57 | $5 t$ | 1 | 153.000 | 886.500 |
| 3\% | 37 | 38 | 5H | 57 | 1 | 163.c0C | 886.500 |
| 37 | 38 | 39 | 50 | 58 | 1 | 171.50C | 886.500 |
| 38 | 39 | 40 | 00 | 50 | 1 | 178.500 | 886.502 |
| 39 | 41 | 42 | 62 | 6! | 2 | 5.000 | 991.502 |
| 45 | 42 | 43 | 63 | 62 | 2 | 15.200 | 891.500 |
| 41 | 43 | 44 | 64 | 63 | 2 | 25.000 | 891.500 |
| 42 | 44 | 45 | 65 | 64 | 2 | 35.000 | 891.500 |
| 43 | 45 | 46 | 66 | 65 | 2 | 45.000 | 891.500 |
| 44 | 46 | 47 | 67 | 66 | 2 | 55.000 | 891.500 |
| 45 | 47 | 48 | 68 | 67 | 2 | 65.00 C | 891.500 |
| 45 | 48 | 49 | 09 | 62 | 2 | 74.000 | 891.502 |
| 47 | 49 | 5 C | 79 | 69 | 2 | 83.000 | 891.509 |
| 49 | 50 | 51 | 71 | 73 | 2 | 93.805 | 891.500 |
| 49 | 51 | 52 | 72 | 71 | 2 | 103.000 | 891. 500 |
| 53 | 52 | 53 | 73 | 72 | 2 | 112.00 C | 891.500 |
| 51 | 53 | 54 | 74 | 73 | 2 | 123.000 | 891.509 |
| 52 | 54 | 55 | 75 | 74 | 2 | 133.000 | 891.500 |
| 53 | 55 | 56 | 76 | 75 | 2 | 143.000 | 891.50 C |
| 54 | 56 | 57 | 77 | 76 | 2 | 153.000 | 891.500 |
| 55 | 57 | 58 | 78 | 77 | 2 | 163.00C | 891.500 |



| 116 | 130 | 131 | 141 | 140 | 5 | 178.500 | 911.500 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 117 | 132 | 133 | 142 | 142 | 5 | 105.500 | 916.500 |
| 118 | 133 | 134 | 143 | 142 | 5 | 113.000 | 916.500 |
| 110 | 134 | 135 | 144 | 143 | 5 | 123.000 | 916.500 |
| 120 | 135 | 136 | 145 | 144 | 5 | 133.000 | 916.500 |
| 121 | 136 | 137 | 146 | 145 | 5 | 143.300 | 916.500 |
| 122 | 137 | 138 | 147 | 146 | 5 | 153.00C | 916.500 |
| 123 | 138 | 139 | 148 | 147 | 5 | 163.000 | 916.502 |
| 124 | 139 | 140 | 149 | 148 | 5 | 171.500 | 916.500 |
| 125 | 140 | 141 | 159 | 149 | 5 | 178.500 | 916.500 |
| 126 | 142 | 143 | 151 | 151 | 5 | 115.500 | 921.500 |
| 127 | 143 | 144 | 152 | 151 | 5 | 123.000 | 921.500 |
| 128 | 144 | 145 | 153 | 152 | 5 | 133.000 | 921.500 |
| 129 | 145 | 146 | 154 | 153 | 5 | 143.000 | 921.500 |
| 133 | 146 | 147 | 155 | 154 | 5 | 153.000 | 921.500 |
| 131 | 147 | 148 | 156 | 155 | 5 | 163.000 | 921.500 |
| 13? | 148 | 149 | 157 | 156 | 5 | 171.500 | 921.500 |
| 133 | 149 | 153 | 158 | 157 | 5 | 178.500 | 921.500 |
| 134 | 151 | 152 | 159 | 159 | 5 | 125.500 | 92 t .500 |
| 135 | 152 | 153 | 160 | 159 | 5 | 133.200 | 926.500 |
| 136 | 153 | 254 | 161 | 160 | 5 | 143.000 | 926.500 |
| 137 | 154 | 155 | 162 | 161 | 5 | 153.00 C | 926.500 |
| 138 | 155 | 156 | 163 | 162 | 5 | 163.000 | 926.500 |
| 139 | 156 | 157 | 164 | 163 | 5 | 171.500 | 926.500 |
| $14)$ | 157 | 158 | 165 | 164 | 5 | 178.500 | 926.500 |
| 141 | 159 | 160 | 166 | 166 | 5 | 135.50 C | 931.500 |
| 142 | 160 | 161 | 167 | 166 | 5 | 143.000 | 931.500 |
| 143 | 161 | 162 | 168 | 167 | 5 | 153.00 C | 931.500 |
| 144 | 162 | 163 | 169 | 168 | 5 | 163.00 C | 931.500 |
| 145 | 163 | 164 | 170 | 169 | 5 | 171.500 | 931.500 |
| 146 | 164 | 165 | 171 | 179 | 5 | 178.500 | 931.500 |
| 147 | 166 | 167 | 172 | 172 | 5 | 145.500 | 936.500 |
| 148 | 147 | 168 | 173 | 172 | 5 | 153.000 | 936.500 |
| 149 | 168 | 169 | 174 | 173 | 5 | 163.00 C | 936.50 S |
| 159 | $1 \in 9$ | 170 | 175 | 174 | 5 | 171.500 | 936.500 |
| 151 | 170 | 171 | 176 | 175 | 5 | 178.500 | 936.500 |
| 152 | 172 | 173 | 177 | 177 | 5 | 155.590 | 941.50 C |
| 153 | 173 | 174 | 178 | 177 | 5 | 163.000 | 941.50C |
| 154 | 174 | 175 | 179 | 178 | 5 | 171.500 | 941.500 |
| 155 | 175 | 176 | 189 | 179 | 5 | 178.500 | 941.500 |

## APPENDIX C

OUTPUT FOR THE FINITE ELEMENT COMPUTER PROGRAM

| $p$ | DELTA-X | DELTA-Y | X-DISP | Y-CISP | TOTAL | NP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3.0 | O.C | 0.0 | 0.0 | 0.0 | 1 |
| 2 | 0.0 | 0.0 | 0.0 | $0 . \mathrm{C}$ | 0.0 | 2 |
| 3 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 | 3 |
| 4 | 9.3 | J. 0 | $0 . \mathrm{C}$ | 0.0 | 0.0 | 4 |
| 5 | 0.0 | 0.0 | C. 0 | 0.0 | 0.0 | 5 |
| 6 | 0.3 | 0.0 | 0.0 | 0.0 | 0.0 | 6 |
| 7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 7 |
| 8 | 0.3 | 2.c | 0.0 | 0.0 | 0.0 | 8 |
| 9 | 3.3 | 0.0 | 0.0 | 0.0 | 0.0 | 9 |
| 1 C | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 10 |
| 1 | 2.3 | 0.0 | 0.0 | $0 . \mathrm{C}$ | 0.0 | 11 |
| 12 | 3.3 | 0.0 | 0.0 | 0.0 | 0.0 | 12 |
| 13 | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 | 13 |
| 14 | 0.2 | 0.0 | 0.0 | 0.5 | 0.3 | 14 |
| 15 | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 | 15 |
| 16 | 0.0 | 0.0 | 0.6 | c. 0 | 0.0 | 16 |
| 17 | 0.0 | 0.0 | 0.0 | 0.6 | 3.0 | 17 |
| 18 | 2.3 | 0.0 | 0.0 | O. C | 0.0 | 18 |
| 19 | 2.3 | $0 . \mathrm{C}$ | 0.0 | C. 0 | 0.9 | 19 |
| 23 | c. $J$ | 0.5 | 0.0 | 0.0 | 0.0 | 20 |
| 1 | C. 0 | 0.0302 | 0.0 | 0.0027 | 0.0027 | 21 |
| 2. | -3.0011 | 0.0003 | -0.011c | 0.0029 | 0.0114 | 22 |
| 3 | - J. 3323 | J.C303 | -0.0228 | 0.0030 | 0.0229 | 23 |
| 4 | -0.0038 | 0.0005 | -0.036C | $0 . \operatorname{CC} 39$ | 0.0362 | 24 |
| 5 | -0. 2060 | 0.0307 | -0.0546 | c. 0063 | 0.3549 | 25 |
| 6 | -0.3133 | J.C319 | -0.3887 | -. 1138 | 0.0858 | 26 |
| 7 | -0. 3196 | 0.0034 | -0.1537 | 0.0241 | 0.1556 | 27 |
| A | -0. 3368 | 0.3769 | -0.258C | i. 0356 | $0.26 \mathrm{C5}$ | 28 |
| 9 | -0. 3618 | 0.6103 | -0.3775 | 0.0446 | C. 3856 | 29 |
| , | -0.1112 | 0.0211 | -0.5610 | c. 6553 | 0.5637 | 30 |
| 1 | -0.1723 | J.C18i) | -0.7374 | 0.0375 | 0.7384 | 31 |
| 22 | -0.2206 | 3.0242 | -C.8443 | S.C183 | 0.8445 | 32 |
| 3 | -0.2286 | 0.c010 | -0.8518 | -c.c399 | 0.8528 | 33 |
| 4 | -9.2300 | - 2.3264 | - 2.7848 | -C.C568 | 0.7908 | 34 |
| 5 | -0.2065 | -3.0348 | -0.t523 | -0.1121 | 0.6619 | 35 |
| 6 | -0.1605 | -2.0349 | - 0.4882 | -0.1c76 | 0.5000 | 36 |
| 37 | -9.1085 | - -2.298 | -0.3257 | -c.c941 | -. 3398 | 37 |
| 析 | - 3.3504 | -2.c245 | -0.1742 | -0.0803 | C. 1919 | 38 |
| 9 | -0.0254 | - -. 0183 | -0. 282 c | -0.ce 80 | 0.1065 | 39 |
| 0 | 2.) | -9.0161 | 0.0 | -0.0639 | 0.3639 | 40 |
| 1 | 0.3 | 0.0310 | 0.0 | c. 0098 | 0.0098 | 41 |
| 2 | -.5. 2321 | 0.0010 | -0.0192 | 0.2059 | 0.0216 | 42 |
| 3 | - 3.3244 | 0.0513 | - 3.0295 | 0.0129 | 0.0429 | 43 |
| 4 | -0.2372 | 2.0315 | -0.6627 | f.C130 | 0.0641 | 44 |
| 5 | -3. 3116 | 9.3)30 | - -3.6964 | C. 0221 | こ. 2989 | 45 |
| 5 | - 3.2211 | 2. 5362 | -3.1561 | 0.6432 | 0.1620 | 46 |
| 7 | -2. 3391 | 9.012n | -0.2696 | 0.6771 | 0.2717 | 47 |
| 9 | -2. 3737 | J. 2238 | - -.4184 | -. 1371 | 0.4319 | 48 |
| 9 | -6.1954 | 2.2339 | -.3.5654 | 0.1321 | C.58C7 | 49 |
| ? | -0.1545 | ).0.45 | -0.7452 | C. 1378 | 2.7579 | 50 |
| 1 | -0.1949 | 3. 2443 | -0.871E | C. 6970 | 0.8770 | 51 |
| 2 | -3. 2129 | 0.0287 | -6.9247 | 0.6244 | 0.9250 | 52 |
| 3 | -0.2143 | 0.0323 | -0.9668 | -0. $c \in 93$ | 0.9095 | 53 |
| 4 | -0. 2155 | - -.2266 | - 2.8594 | -0.1531 | 0.8730 | 54 |


| 55 | -0.2147 | -0.0552 | -0.7774 | -0.2098 | 0.8053 | 55 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 56 | -C. 1956 | -0.2622 | -0.6474 | -0.2186 | 0.6833 | 56 |
| 57 | -0. 1565 | -9.0670 | -0.479s | -0.2163 | 0.5264 | 57 |
| 58 | -0.0986 | -0.3633 | -0.2878 | -6.20cl | 0.3595 | 58 |
| 59 | -0.0504 | - 3.3560 | -0.1448 | -0.1842 | 0.2343 | 59 |
| 60 | 0.5 | -0.0519 | 0.0 | -0.1763 | 0.1763 | 60 |
| 61 | 2.9 | 0.0323 | 0.0 | 0.0219 | C. 0219 | 81 |
| 52 | -0.3039 | 2.0525 | -0.0335 | 0.2227 | 0.0405 | 62 |
| 63 | -0.0384 | 0.3029 | -0.0700 | 0.0249 | 0.0743 | 63 |
| 64 | -0. 3144 | 2. 3040 | -0.1132 | 0.0306 | 0.1172 | 64 |
| 55 | - -. 2225 | 0.0366 | -0.1672 | 0.0464 | 0.1735 | 65 |
| 66 | -0.0364 | 0.2139 | -0.2455 | C. 1862 | 0.2602 | 66 |
| 57 | - 7.0604 | 0.0259 | -0.3697 | 3.1446 | 0.3970 | 67 |
| 69 | - 2.2976 | 0.0419 | -0.5450 | 0.1997 | 0.5864 | 68 |
| 69 | -0.1373 | 0.056 C | -0.7090 | 0.2224 | C. 7431 | 69 |
| 70 | -0.1738 | J. 5644 | -0.8434 | ग. 1953 | 0.8657 | 70 |
| 71 | -2.1911 | 2.0535 | -0.902C | 2.1224 | 0.9103 | 71 |
| 72 | - 2.1980 | 7.0306 | - 0.9073 | 0.0169 | 0.9074 | 72 |
| 73 | -0.1993 | 3.0.527 | -0.8886 | -0.0927 | 0.8934 | 73 |
| 74 | -0.2901 | -0.0262 | -0.8475 | -C. 1905 |  | 74 |
| 75 | -0.2305 | -0.0562 | -0.7826 | -c. 2679 | 0.8686 0.8272 | 75 |
| 76 | -0.1939 | -0.0777 | -0.6747 | -0.3076 | 0.7416 | 76 |
| 77 | -0.1618 | -0.0929 | -0.5154 | -0.3234 | 0.6084 | 77 |
| 78 | -0.1081 | -0.1505 | -C.3194 | -0.3225 | 0.4539 | 78 |
| 79 | -0. 2579 | -0.3979 | - 5.1648 | -0.3121 | 0.3529 | 79 |
| 92 | 0.3 | -0.0968 | 0.0 | -0.30E1 | 0.3081 | 80 |
| 81 | 0.3 | 0.0743 | 0.0 | c. C 386 | 9. 3386 | 81 |
| 32 | -0.2348 | 2. 0047 | - 0.0377 | 0.0402 | 0.0551 | 82 |
| 83 | -0. 3107 | 0.0357 | -0.c799 | 0.0452 | 0.0918 | 3 |
| 84 | -0. 3185 | 3.0379 | -6. 1320 | 0.0560 | 0.1434 | 84 |
| 85 | -9. 3315 | 0.0127 | -0.2033 | C. CB 12 | 2.2189 | 95 |
| 86 | -C. 3501 | 0.0236 | -0.3013 | C. 1361 | O. 33 cb | 86 |
| 87 | -0.7811 | n.0415 | -0.4385 | ?. 2209 | C. 4910 | 87 |
| 86 | -0.1194 | 3.0609 | -0.6053 | C. 2865 | 0.6697 | 88 |
| 89 | - -1452 | 0.0769 | -0.7157 | 3.3003 | 0.7762 | 89 |
| $4:$ | -0.1712 | J. 2733 | - 2.8195 | 0.2305 | 0.8513 | 89 90 |
| 91 | -C. 1904 | $0.257 t$ | -0.8521 | 0. 1304 | 0.8513 0.8620 | 91 |
| 92 | - -.1839 | 0.0314 | - 2.8567 | 0.0121 | J. 8567 | 92 |
| 93 | -C. 1849 | 0.0332 | - 2.8415 | -2.1)66 | j. 8482 | 93 |
| 94 | -0.1853 | -5.0259 | -0.8c98 | -C.2162 | 0.8382 | 94 |
| 95 | - 3.1853 | -3.0563 | -0.7481 | -0.3142 | 0.81114 | 95 |
| 36 | -2.1772 | -2.09.22 | - 2.6449 | - -.3859 | 0.8114 .0 .7515 | 95 96 |
| 97 | -2.1480 | -0.1214 | -3.4917 | -C.4301 | 0.6533 | 97 |
| 98 | -¢. 2975 | -3.141t | -0.3c27 | -C. 4477 | 0.6533 3.5435 | 97 |
| 79 | -2. 2514 | -3.1483 | -0.1546 | - 2.4497 | 0.44755 | 98 |
| 123 | 0.2 | -0.1592 | 0.0 | -0.4492 | 0.4459 | 100 |
| 1.1 | 0.2 | J.0.067 | 3.2 | 6.0571 | 0.3571 | 101 |
| 1.32 | -0. 3056 | 2.0373 | -3.0417 | $0 . C 598$ | 0.0729 | 102 |
| 13 | -0. 3123 | 2.0.291 | - 3.0887 | 0.0685 | 0.0729 0.1121 | 102 103 |
| 124 | -2. 3221 | 3.0132 | - 3.1499 | C. 0871 | 0.1734 | 104 |
| 55 | -i. 3371 | 9.020s | -2. 2345 | C. 1250 | 0.1734 0.2657 | 104 105 |
| 90 | -2. 3015 | 3.0364 | -0.3518 | C. 6.1957 | 0.2657 3.4026 | 165 106 |
| 97 | - 3.3929 | 3.3591 | - 3.4871 | ¢. <br> .2922 | 3.4526 2.5680 | 108 107 |
| 98 | -9.1299 | 2.0798 | -0.6262 | J. 2922 2. 3622 | -0.5684 | 107 108 |
| 9 | --. 1526 | 2.0359 | -9.7248 | J. 3491 | -. 8.8445 | 108 |
| 12 | - -. 16.3 | 2.3797 | -0.7851 | J. 2577 | C. 8216 | 12 |
| 11 | - E .1689 | 3.5592 | -0.8232 | 3.1365 | 6.8216 0.8344 | 111 |
| 12 | -0.1692 | 0.0321 | -9.8242 | 0.0657 | .88344 0.8242 | 112 |
| 13 | -3. 1794 | 2.2034 | -3.9492 | -0.1198 | 2. 3180 | 113 |
| 14 | -0.1709 | - 3.0259 | - 0.7795 | -0.2431 | C. 8079 | 113 |


| 115 | -0.1692 | -0.0573 | - -. 7068 | -0.3566 | C. 7516 | 115 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 116 | -0.1566 | -0.1308 | -3.6023 | -0.4555 | 0.7551 | 116 |
| 217 | -0.1285 | -0.1415 | -0.4581 | -0.5192 | 0.6924 | 117 |
| 118 | -0. 3839 | -0.1717 | -0.2809 | -0.5532 | 0.6204 | 118 |
| 119 | -0.3437 | -0.1830 | -0.1433 | -0.5610 | 0.5790 | 119 |
| 120 | 0. 3 | -0.1870 | 0.0 | -0.5638 | 0.5638 | 120 |
| 121 | -0.1544 | 0.0833 | -0.75c9 | 0.2948 | 0.8067 | 121 |
| 122 | -0.1541 | 0.0595 | -c. 7680 | 0.1550 | 0.7835 | 122 |
| 123 | -2.1550 | J.6327 | -0.776t | 0.0189 | 0.7768 | 123 |
| 124 | - 2.1558 | 0.6038 | -0.7577 | -0.1235 | 0.7677 | 124 |
| 125 | -0.1566 | -0.0257 | -0.7199 | -0.2580 | 0.7647 | 125 |
| 126 | -0.1511 | - 3.3615 | -0.6529 | -C. 3920 | 0.7598 | 126 |
| 127 | -0.1372 | -0.1103 | -0.5521 | -0.5086 | 0.7507 | 127 |
| 128 | -0.1116 | - 2.1592 | -0.4198 | -0.5923 | 0.7260 | 128 |
| 129 | -0.3720 | - 3.1964 | -0.2581 | -C.6384 | 0.6886 | 129 |
| 130 | -0. 0377 | -0.2117 | -0.1318 | -0.6534 | 0.6666 | 130 |
| 131 | 0.0 | -0.2166 | 0.0 | -5.6572 | 0.6572 | 131 |
| 132 | - 0.1409 | c. 0594 | -0.6868 | 0.1863 | 0.7116 | 132 |
| 133 | - 3.1402 | 2.0329 | -0.6907 | c. 0410 | 0.6919 | 133 |
| 134 | -2.1410 | 0.0344 | - 0.6852 | -0.1068 | 2.6935 | 134 |
| 135 | -0.1403 | -0.0265 | -0.6473 | -0.2608 | 0.6979 | 135 |
| 136 | -0.1349 | -0.0665 | -0.5865 | -0.4150 | 0.7156 | 136 |
| 137 | -0.1214 | - C. 1196 | -0.4958 | -0.5464 | 0.7378 | 137 |
| 138 | -0. 2977 | -2.1751 | -0.3772 | -C.6463 | 0.7484 | 138 |
| 139 | -0.3627 | -0.2184 | -0.2321 | -c.7071 | 0.7442 | 139 |
| $14 ?$ | -0. 2325 | -3.2364 | -2.1187 | -2.7270 | 0.7366 | 14.5 |
| 141 | 2.) | -0.742t | $0 . \mathrm{C}$ | -0.7341 | 0.7341 | 141 |
| 142 | -0.1254 | 3.3325 | -0.5760 | 0.0801 | 0.5915 | 142 |
| 143 | - 2.1243 | 3. 6347 | - 0.5696 | -0.0732 | 2. 5743 | 143 |
| 144 | -0.1235 | -0.0277 | -2.5506 | -0.2338 | 0.5982 | 144 |
| 145 | - 3.1123 | -0.0708 | -0.498C | -0.4c24 | $0.64 \mathrm{C3}$ | 145 |
| 146 | - 3.1067 | -0.1283 | -0.4231 | -0.5540 | 0.6971 | 145 |
| 147 | -9. 3953 | -0.1897 | -6.3214 | -0.6740 | 0.7467 | 147 |
| 148 | -0.0540 | -0.2377 | -0.1991 | - C . 7469 | 0.7727 | 148 |
| 149 | -0.0278 | -2.2581 | -0.1011 | -0. 7748 | 0.7814 | 149 |
| 153 | 2.0 | -5.2648 | 0.0 | -C. 7827 | 0.7827 | 150 |
| 151 | -0. 1073 | 2. 5343 | -0.4350 | -3. 6199 | 3.4305 | 151 |
| 152 | -i. 1248 | - 2.0288 | -2.4151 | -0.1809 | 0.4528 | 152 |
| 153 | -0.1039 | -3.0743 | -0.3860 | -C. 3528 | 0.5229 | 153 |
| 154 | - 3.3913 | -9.1358 | -0.3255 | -0.5220 | 0.6151 | 154 |
| 155 | -9. $372 t$ | -0.2330 | -0.247C | -0.6552 | 0.7002 | 155 |
| 158 | -0.3448 | -0.2548 | -0.1507 | - 0.7439 | 0.7702 0.7590 | 154 156 |
| 157 | - 3.3229 | - 2.2763 | -3.3771 | -0.7763 | 0.7590 0.7801 | 156 157 |
| 158 | 0.J | -2.2839 | 0.0 | -2. 7882 | 0.7882 | 158 |
| 159 | -0.3928 | -0.0395 | -0.2685 | -0.1060 | 0.7882 0.2868 | 158 159 1 |
| $16 \%$ | -0. 3798 | -3.0766 | -9.2477 | -0.2714 | 0.3674 | 160 |
| 161 | -0.3741 | -0.141A | -0.2152 | -0.4376 | 0.4877 | 161 |
| 162 | -0.0581 | -0.2154 | -0.1579 | - 0.5811 | 3.6522 | 162 |
| 163 | -2. 2345 | -0.2692 | -0.2945 | - 0.6732 | -.6798 | 163 |
| 154 | -0. 2166 | - 2.2915 | - C. 3473 | -0.7115 | 0.7131 | 164 |
| 165 | 2. 3 | -3.2982 | 3.2 | -0. 7225 | 0. 7225 | 165 |
| 165 | -3.3539 | -3. 3783 | - 0.1177 | - | 0. 2014 | 165 |
| 167 | -2.3518 | -2. 1443 | - 2.1012 | -0.3111 | -. 2.3272 | 168 167 |
| 168 | -0.3410 | - 2.2269 | -9.0764 | -0.4381 | 0.3272 | 167 168 |
| 169 | - -j.j20́t | -2.2316 | -0.0453 | -0.5238 | 0.5454 | 168 169 |
| 170 | -7.21 26 | -3.3013 | -0.5197 | -ن. 0.549 | 0.5254 0.5553 | 169 170 |
| 171 | -. 3 | - 3.3093 | 0.0 | -C. 5674 | U.5553 | 171 |
| 172 | -0.024E | -0.1455 | -0.0245 | - 0.1455 | 0.5674 0.1476 | 171 172 |
| 173 | -0.0138 | -0.2373 | -0.2138 | -?. 2373 | 0.2377 | 173 |
| 174 | -0.2373 | -0.2361 | -0.0.573 | -0.2861 | c. 2862 | 174 |


| 175 | -0.0929 | -0.3983 | -0.2029 | -0.3683 | 0.3083 | 175 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 176 | 2.3 | -0.3140 | 0.0 | -0.3140 | 3.3140 | 176 |
| 177 | 0.3 | 0.0 | 0.0 | 0.0 | 0.0 | 177 |
| 178 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 178 |
| 179 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 179 |
| 180 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 180 |

STP $=S S F S$ AND STRESS LEVELS FOR EINAL CONDITION AT FND OF INCOEMENT

| ELE | SIG-X | story | TAU-XY | SIG-1 | SIG-3 | TAU-max | THETA | SIG1/5163 | SLMAX | SLPRES | EtE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3.050 | 2.961 | 0.040 | 3.065 | 2.946 | 0.960 | 69.163 | 1.940 | 0.092 | 0.092 | 1 |
| 2 | 3.048 | 2.962 | 0.112 | 3.125 | 2.885 | 0.120 | 55.457 | 1.083 | 0.186 | 0.186 | 2 |
| 3 | 3.924 | 2.936 | 0.176 | 3.161 | 2.759 | 0.181 | 52.062 | 1.130 | 0.281 | 0.281 | 3 |
| 4 | 3.312 | 2.899 | C. 240 | 3.201 | 2.709 | 0.246 | 51.623 | 1.182 | 0.381 | 0.381 | 4 |
| 5 | 2.967 | 2.789 | 0.315 | 3.206 | 2.551 | 0.327 | 52.882 | 1.257 | 0.507 | 0.507 | 5 |
| 6 | 3.043 | 2.795 | 0.403 | 3.341 | 2.497 | 0.422 | 53.541 | 1.338 | 0.653 | 0.653 | 6 |
| 7 | 3.162 | 2.902 | 2.481 | 3.530 | 2.533 | 0.498 | 52.563 | 1.393 | 0.771 | 0.771 | 7 |
| 8 | 3.398 | 3.177 | 0.531 | 3.830 | 2.745 | 0.542 | 50.872 | 1.395 | 0.839 | 0.839 | 8 |
| 9 | 3.569 | 3.441 | 0.568 | 4.076 | 2.934 | 0.571 | 48.228 | 1.389 | 0.884 | 0.884 | 9 |
| 16 | 3.882 | 3.871 | 2.587 | 4.464 | 3.289 | 0.587 | 45.266 | 1.357 | 0.909 | 0.909 | 10 |
| 11 | 4.186 | 4.283 | 6.590 | 4.826 | 3.643 | 0.592 | 42.656 | 1.325 | 0.916 | 0.916 | 11 |
| 12 | 4.666 | 4.847 | 3. 580 | 5.344 | 4.169 | 3.587 | 40.567 | 1.282 | C. 909 | 0.909 | 12 |
| 13 | 5.254 | 5.506 | 0.562 | 5.956 | 4.804 | 0.576 | 38.683 | 1.240 | 0.891 | 0.891 | 13 |
| 14 | 5.810 | 6.116 | 0.533 | 6.517 | $5.4 C 9$ | 0.554 | 36.995 | 1.205 | 0.858 | 0.858 | 14 |
| 15 | 6.184 | 6.531 | 3.493 | 6.885 | 5.835 | 0.522 | 35.298 | 1.179 | 0.809 | 0.809 | 15 |
| 14 | 6.528 | 6.910 | 0.433 | 7.192 | 6.246 | 0.473 | 33.112 | 1.152 | 0.732 | 0.732 | 16 |
| 17 | 6.755 | 7.174 | C. 343 | 7.367 | 6.563 | 0.402 | 29.264 | 1.122 | 0.622 | 0.622 | 17 |
| 18 | 6.911 | 7.361 | 0.219 | 7.450 | 6.822 | 0.314 | 22.136 | 1.092 | 0.486 | 0.486 | 18 |
| 19 | 6.961 | 7.424 | 0.081 | 7.438 | 6. 947 | 0.246 | 9.660 | 1.071 | 0.380 | 0.380 | 19 |
| 20 | 2.557 | 2.259 | 6.040 | 2.562 | 2.254 | 0.154 | 82.465 | 1.137 | 0.238 | 0.238 | 20 |
| 21 | 2.552 | 2.255 | 0.116 | 2.592 | 2.215 | C. 189 | 71.006 | 1.170 | 0.292 | 0.292 | 21 |
| 22 | 2.562 | 2.253 | C. 182 | 2.646 | 2.168 | c. 239 | 65.141 | 1.220 | 0.370 | 0.370 | 22 |
| 23 | 2.564 | 2.176 | 2.238 | 2.677 | 2.062 | 0.337 | 64.585 | 1.298 | 0.476 | 0.476 | 23 |
| 24 | 2.670 | 2.118 | 0.282 | 2.789 | 1.999 | 0.395 | 67.200 | 1.395 | 0.611 | 0.611 | 24 |
| 25 | 2.788 | 2.1068 | 0.318 | 2.909 | 1.948 | 0.481 | 69.275 | 1.493 | 0.744 | 0.744 | 25 |
| 26 | 3.040 | 2.265 | 0.362 | 3.183 | 2.122 | 0.530 | 68.482 | 1.500 | 0.821 | 0.821 | 26 |
| 27 | 3.182 | 2.441 | 0.407 | 3.362 | 2.261 | 0.551 | 66.133 | 1.487 | 0.852 | 0.852 | 27 |
| 28 | 3.414 | 2.826 | 0.456 | 3.662 | 2.577 | 0.542 | 61.422 | 1.421 | 0.840 | 0.840 | 28 |
| 20 | 3.505 | 3.154 | 0.475 | 3.836 | 2.823 | 0.506 | 55.140 | 1.359 | 0.784 | 0.784 | 29 |
| 32 | 3.762 | 3.729 | 0.499 | 4.155 | 3.336 | 0.409 | 46.137 | 1.245 | 0.634 | 0.634 | 30 |
| 31 | 4.034 | 4.134 | 2.339 | 4.427 | 3.741 | 0.343 | 40.818 | 1.183 | 0.578 | 0.531 | 31 |
| 32 | 4.422 | 4.891 | 0.289 | 5.029 | 4.284 | 0.373 | 25.482 | 1.174 | 0.605 | 0.577 | 32 |
| 33 | 4.791 | 5.418 | 0.293 | 5.534 | 4.676 | 0.429 | 21.555 | 1.184 | 0.664 | 0.664 | 33 |
| 34 | 5.225 | 5.915 | 2.291 | 6.022 | 5.118 | 0.452 | 20.776 | 1.177 | 0.699 | 0.699 | 34 |
| 35 | 5.528 | 6.254 | 0.273 | 6.345 | 5.437 | 0.454 | 18.453 | 1.167 | 0.703 | 0.703 | 35 |
| 36 | 5.823 | 6.583 | 0.219 | 6.642 | 5.764 | 0.439 | 14.993 | 1.152 | 0.679 | 0.679 | 36 |
| 37 | 5.988 | 6.770 | 0.141 | 6.795 | 5. 983 | 0.416 | 9.888 | 1.139 | 0.644 | C. 644 | 37 |
| 39 | 6.979 | 6.879 | 0.050 | 6.873 | 6.076 | 0.398 | 3.605 | 1.131 | 0.617 | 0.617 | 38 |
| 39 | 1.911 | 1.614 | 0.04 C | 1.916 | 1.659 | 0.153 | 82.538 | 1.191 | 0.260 | 0.260 | 39 |
| 43 | 1.920 | 1.524 | 2. 115 | 1.959 | 1.534 | 0.187 | 71.343 | 1.237 | 0.319 | 0.319 | 40 |
| 41 | 1.914 | 1.608 | 0.181 | 1.958 | 1.524 | 0.237 | 65.060 | 1.311 | 0.410 | 0.410 | 41 |
| 42 | 1.932 | 1.584 | 3.224 | 2.041 | 1.475 | 0.283 | 63.962 | 1.385 | 0.496 | 0.496 | 42 |
| 43 | 1.943 | 1.479 | 0.229 | 2.338 | 1. 394 | 0.327 | 67.688 | 1.472 | 0.585 | 0.585 | 43 |
| 44 | 2.121 | 1.494 | 0.219 | 2.190 | 1.425 | 0.383 | 72.530 | 1.537 | 0.678 | 0.678 | 44 |
| 45 | 2.329 | 1.586 | 0.232 | 2.396 | 1.520 | 0.438 | 73.987 | 1.576 | 0.758 | 0.758 | 45 |
| 46 | 2.658 | 1.885 | 0.290 | 2.754 | 1.789 | 0.483 | 71.556 | 1.539 | 0.784 | 0.784 | 46 |
| 47 | 2.773 | 2.135 | 0.364 | 2.938 | 1.971 | 0.484 | 65.570 | 1.491 | 0.755 | 0.755 | 47 |
| 48 | 3.063 | 2.618 | 0.374 | 3.273 | 2.465 | 2.434 | 63.266 | 1.361 | 0.619 | 0.619 | 48 |
| 49 | 3.277 | 3.153 | 3.271 | 3.492 | 2.537 | 0.278 | 51.432 | 1.189 | 0.357 | 0.357 | 49 |
| 50 | 3.502 | 3.587 | 0.201 | 3.795 | 3.394 | 2.201 | 46.040 | 1.118 | 0.326 | 0.239 | 50 |
| 51 | 3.805 | 4.256 | 0.129 | 4.291 | 3.771 | 3.263 | 14.974 | 1.138 | 0.397 | 0.291 | 51 |
| 52 | 4.369 | 4.983 | 6.153 | 4.911 | 4. 441 | 0.435 | 10.274 | 1.215 | 0.472 | 0.467 | 52 |
| 53 | 4.252 | 5.257 | 0.147 | 5.272 | 4.181 | 2.545 | 7.799 | 1.261 | 0.573 | 0.573 | 53 |
| 54 | 4.440 | 5.693 | $0.14 t$ | 5.715 | 4.424 | 0.643 | 6.579 | 1.291 | 0.653 | 0.653 | 54 |
| 55 | 4.639 | 5.986 | 0.113 | 5.996 | 4.660 | 0.698 | 4.649 | 1.303 | 0.691 | 0.691 | 55 |
| 56 | 4.767 | 6.224 | 2. C64 | 6.227 | 4.764 | 0.731 | 2.530 | 2. 307 | 0.708 | 0.708 | 56 |



| 117 | 0.367 | 0.232 | $0 . C 57$ | 0.388 | 0.211 | 0.688 | 69.827 | 1.834 | 0.032 | 0.020 | 117 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 118 | 9.481 | 0.529 | 0.166 | 0.673 | 0.337 | 0.168 | 40.831 | 1.998 | 0.052 | 0.038 | 118 |
| 119 | 1.010 | 1.541 | 0.300 | 1.676 | 0.874 | 0.401 | 24.257 | 1.917 | 0.087 | 0.086 | 119 |
| 12.0 | 3.826 | 1.899 | 0.359 | 2.008 | 0.717 | 0.645 | 16.889 | 2.800 | 0.140 | 0.140 | 120 |
| 121 | J.94C | 2.578 | 0.322 | 2.639 | 0.879 | 0.885 | 10.743 | 3.003 | 0.189 | 0.189 | 121 |
| 122 | 0.716 | 2.762 | 0.195 | 2.781 | 0.698 | 1.041 | 5.407 | 3.986 | 0.227 | 0.227 | 122 |
| 123 | 2.635 | 3.052 | 0.068 | 3.354 | 0.633 | 1.210 | 1.603 | 4.824 | 0.265 | 0.265 | 123 |
| 124 | 3.504 | 3.101 | 0.213 | 3.101 | 0.504 | 1.299 | 0.281 | c. 154 | 0.287 | 0.287 | 124 |
| 125 | 0.487 | 3.179 | -C.001 | 3.179 | 0.487 | 1.346 | -0.024 | 6.523 | 0.298 | 0.298 | 125 |
| 126 | 2.114 | 2.147 | -0.060 | 0.193 | 0.069 | 0.062 | -37.239 | 2.813 | 0.019 | 0.014 | 126 |
| 127 | 2.339 | 0.625 | 0.160 | 0.697 | 0.267 | 0.215 | 24.137 | 2.610 | 0.050 | 0.048 | 127 |
| 128 | 0.778 | 1.519 | 0.317 | 1.637 | 0.661 | 0.488 | 20.295 | 2.476 | 0.106 | 0.106 | 128 |
| 129 | 0.634 | 1.830 | 2.344 | 1.921 | 0.542 | 0.690 | 14.941 | 3.546 | 0.152 | 0.152 | 129 |
| 130 | -. 725 | 2.362 | 0.252 | 2.400 | 0.687 | 0.856 | 8.565 | 3.491 | 0.186 | 0.186 | 130 |
| 131 | ). 567 | 2.440 | 0.124 | 2.448 | 0.559 | 0.944 | 3.772 | 4.379 | 0.208 | 0.208 | 131 |
| 132 | 3.550 | 2.588 | 3.048 | 2.589 | 0.549 | 1.020 | 1.335 | 4.719 | 0.225 | 0.225 | 132 |
| 133 | 3.492 | 2.576 | . .014 | 2.576 | 0.492 | 1.042 | 0.384 | 5.240 | 0.230 | 0.230 | 133 |
| 134 | -3.015 | 0.174 | -c. 079 | 0.203 | -0.044 | 0.123 | -20.078 | -4.653 | 0.028 | 0.028 | 134 |
| 135 | 3.324 | 0.650 | 0.198 | 0.743 | 0.231 | 0.256 | 25.237 | 3.221 | 0.058 | 0.058 | 135 |
| 136 | 0.659 | 1.450 | 0.305 | 1.554 | 0.555 | 0.500 | 18.825 | 2.802 | 0.110 | 0.110 | 136 |
| 137 | 0.547 | 1.667 | 0.268 | 1.728 | 0.486 | 0.621 | 12.776 | 3.553 | 0.137 | 0.137 | 137 |
| 138 | 2.651 | 1.998 | 0.148 | 2.014 | 0.635 | 0.690 | 6.191 | 3.174 | 0.151 | 0.151 | 138 |
| 139 | 2.574 | 1.968 | 0.073 | 1.971 | 0.570 | 0.701 | 2.980 | 3.459 | 0.154 | 0.154 | 139 |
| 143 | 3.601 | 2.329 | 0.018 | 2.029 | 0.601 | 0.714 | 0.733 | 3.377 | 0.157 | 0.157 | 140 |
| 141 | 3.014 | 0.178 | 0.012 | 0.179 | 0.013 | 0.083 | 4.130 | 14.102 | 0.019 | 0.019 | 141 |
| 142 | 3.352 | 0.662 | 0.197 | 0.757 | 0.257 | c. 250 | 25.879 | 2.949 | 0.056 | 0.056 | 142 |
| 143 | 0.632 | 1.277 | J. 224 | 1.347 | 0.562 | 3.392 | 17.392 | 2.396 | 0.086 | 0.036 | 143 |
| 144 | 3.577 | 1.350 | 0.137 | 1.373 | 0.554 | 0.410 | 9.754 | 2.481 | 0.090 | 0.090 | 144 |
| 145 | 0.725 | 1.496 | 0.057 | 1.500 | 0.721 | 0.390 | 4.191 | 2.081 | 0.085 | 0.085 | 145 |
| 146 | 0.700 | 1.440 | 0.023 | 1.441 | 0.699 | 0.371 | 1.776 | 2.060 | 0.081 | 0.081 | 146 |
| 147 | C. 159 | 0.195 | 0.072 | 0.251 | 0.102 | 0.074 | 38.001 | 2.459 | 0.017 | 0.017 | 147 |
| 148 | 2.381 | 0.583 | 0.140 | 0.654 | 0.310 | 0.172 | 27.085 | 2.111 | 0.039 | 0.039 | 148 |
| 149 | 2.632 | 0.919 | 0.052 | 0.928 | 3.623 | 0.153 | 9.924 | 1.490 | 0.033 | 0.035 | 149 |
| 150 | 3.613 | 0.837 | 0.045 | 0.846 | 0.624 | 0.121 | 10.816 | 1.400 | 0.026 | 0.026 | 150 |
| 151 | 0.677 | 0.896 | 0.011 | 2.896 | 0.677 | 0.110 | 2.858 | 1.324 | 0.324 | 0.024 | 151 |
| 152 | 0.143 | 0.149 | 2.033 | 0.179 | 0.112 | 0.033 | 42.494 | 1.594 | 0.008 | 0.008 | 152 |
| 153 | 0.286 | 0.297 | 0.0 | 0.297 | 0.286 | 0.006 | 0.0 | 1.041 | 0.001 | 0.001 | 153 |
| 154 | $\bigcirc .286$ | 0.297 | 2.0 | 0.297 | J. 286 | 0.306 | 0.3 | 1.041 | 0.001 | 0.001 | 154 |
| 155 | 3.286 | 2.297 | 0.0 | 0.297 | 0.296 | 0.006 | 0.0 | 1.041 | 0.001 | 0.001 | 155 |

solution time

CORN ELEMENT STIFRNESSES********** C. O
FกRM TCTAL STIFFNESS************** 0.0
EQUATICN SOLVING****************** C.O
CALSULATE STDESSES AAN STPAINS**** C.O
SOLUTIUV TIME FER THIS ITERATION** SOC

DETERMIJE CONTECL OATA************ C.C


#### Abstract

APPENDIX D

SUPPORTING DATA FOR THE FINITE ELEMENT COMPUTER PROGRAM


MOTILUS ANO PRISSNH'S RATID VALUES BASED ON AVERAGE STRESSES DUR ING THF INCREMENT STMAINS FOR FINAL CONDITION AT ENO OF INCREMENT

| ELE | ELAS MOC | BULK MCD | SHEAP MOD | POIS | EPS-X | PPS-Y | GAM-XY | EPS-1 | EPS-3 | gammax | ELE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 117.0 | 1563.9 | 39.3 | C. 490 | 0.055 | -0.047 | 0.091 | 0.972 | -0.064 | 0.136 | $!$ |
| 2 | 98.4 | 1651.2 | 33.0 | 0.490 | 0.059 | -0.049 | 0.281 | 0.155 | -9.146 | 0.301 | 2 |
| 3 | 81.5 | 1367.7 | 27.4 | C. 490 | 0.066 | -0.057 | 0.485 | 0.255 | -0.246 | c. 500 | 3 |
| 4 | 64.8 | 1087.0 | 21.7 | 0.490 | 0.093 | -0.085 | 0.743 | 0.386 | -0.378 | 0.764 | 4 |
| 5 | 46.3 | 776.4 | 15.5 | 0.490 | 0.171 | -0.167 | 1.156 | 0.604 | -0.601 | 1.205 | 5 |
| 6 | 26.0 | 436.5 | 8.7 | C.490 | 0.325 | -0.315 | 1.965 | 1.040 | -1.030 | 2.070 | 6 |
| 7 | 12.8 | 215.1 | 4.3 | 0.490 | 0.521 | -0.497 | 3.374 | 1.774 | -1.750 | 3.524 | 7 |
| 8 | 6.9 | 115.t | 2.3 | 0.490 | 0.749 | -0.669 | 5.243 | 2.756 | -2.675 | 5.432 | 8 |
| 9 | 4.0 | 67.9 | 1.4 | 0.49 C | 0.915 | -0.833 | 7.171 | 4.024 | -3.941 | 7.965 | 9 |
| 10 | 2.7 | 45.3 | C. 5 | 0.490 | 0.882 | -0.774 | 10.910 | 5.572 | -5.463 | 11.035 | 10 |
| 11 | 2.2 | 36.7 | 0.7 | 0.490 | 0.534 | -0.465 | 13.277 | 6.692 | -6.623 | 13.315 | 11 |
| 12 | 2.1 | 34.6 | 0.7 | 0.490 | 0.038 | 0.180 | 14.425 | 1.322 | -7.104 | 14.426 | 12 |
| 13 | 2.2 | 37.5 | C. 8 | 0.493 | -0.335 | 1.139 | 13.923 | 7.402 | -6.599 | 14.001 | 13 |
| 14 | 2.9 | 48.2 | 1.0 | 2.490 | -0.662 | 1.741 | 12.053 | 6.684 | -5.406 | 12.290 | 14 |
| 15 | 4.2 | 69.7 | 1.4 | 0.490 | -0.821 | 1.831 | 9.482 | 5.428 | -4.418 | 9.846 | 15 |
| 16 | 6.5 | 109.8 | 2.2 | 3.49C | -0.813 | 1.689 | 6.716 | 4.016 | -3.148 | 7.163 | 16 |
| 17 | 10.9 | 183.1 | 3.7 | 0.490 | -0.757 | 1.453 | 4.098 | 2.676 | -1.980 | 4.656 | 17 |
| 18 | 17.3 | 290.5 | 5.8 | 0.490 | -0.659 | 1.236 | 2.047 | 1.683 | -1.166 | 2.789 | 18 |
| 19 | 23.1 | 387.2 | 7.7 | 0.49 C | -0.585 | 1.099 | 0.654 | 1.160 | -0.647 | 1.807 | 19 |
| 25 | 116.9 | 1960.8 | 39.2 | 0.49 C | 0.151 | -0.141 | 0.280 | 0.157 | -0.147 | 0.303 | 20 |
| 21 | 104.8 | 1758.2 | 35.2 | 0.490 | 0.160 | -0.150 | 0.244 | 0.202 | -0.192 | 0.394 | 21 |
| 22 | 87.4 | 1466.7 | 29.? | 0.490 | 0.182 | -c.171 | 0.423 | 0.280 | -0.2t9 | 0.549 | 22 |
| 23 | 67.0 | 1124.8 | 22.5 | 0.490 | 0.261 | -0.250 | 0.628 | 0.411 | -0.400 | 0.810 | 23 |
| 24 | 41.7 | 70.00 | 14.C | 0.490 | 0.469 | -0.453 | 0.949 | 0.670 | -0.654 | 1.323 | 24 |
| 25 | 21.6 | 362.1 | 7.2 | 0.490 | 3.848 | -0.825 | 1.521 | 1.142 | -1.119 | 2.261 | 25 |
| $2 t$ | 11.3 | 190.2 | 3.8 | 0.490 | 1.311 | -1.245 | 2.465 | 1.808 | -1.743 | 3.551 | 26 |
| 27 | 8.1 | 136.1 | 2.7 | 0.490 | 1.668 | -1.590 | 3.267 | 2.346 | -2.267 | 4.613 | 27 |
| 28 | 8.0 | 134.1 | 2.7 | 0.490 | 1.814 | -1.699 | 3.635 | 2.585 | -2.470 | 5.055 | 28 |
| 29 | 11.4 | 191.7 | 3.8 | C. 490 | 1.514 | -1.420 | 3.477 | 2.322 | -2.228 | 4.549 | 29 |
| 30 | 19.1 | 321.0 | 6.4 | 0.493 | 0.800 | -0.656 | 2.605 | 1.564 | -1.420 | 2.984 | 30 |
| 31 | 329.2 | 5373.2 | 107.5 | 0.490 | -0.052 | 0.234 | 2.113 | 1.157 | -0.975 | 2.132 | 31 |
| 32 | 275.8 | 4027.3 | 92.5 | C.49C | -0.572 | 0.858 | 2.230 | 1.372 | -1.086 | 2.459 | 32 |
| 33 | 11.5 | 193.2 | 3.9 | 0.490 | -1.072 | 1.541 | 2.358 | 1.994 | -1.525 | 3.519 | 33 |
| 34 | 9.3 | 155.7 | 3.1 | 0.490 | -1.471 | 2.087 | 2.864 | 2.592 | -1.975 | 4.567 | 34 |
| 35 | 8.9 | 149.0 | 3.C | 0.490 | -1.650 | 2.332 | 3.055 | 2.850 | -2.168 | 5.019 | 35 |
| 36 | 9.7 | 163.2 | 3.3 | 0.499 | -1.718 | 2.420 | 2.528 | 2.776 | -2.074 | 4.849 | 36 |
| 37 | 11.1 | 186.9 | 3.7 | 0.490 | -1.681 | 2.361 | 1.563 | 2.506 | -1.826 | 4.333 | 37 |
| 38 | 12.2 | 204.8 | 4.1 | C.493 | -1.620 | 2.286 | 0.543 | 2.305 | -1.639 | 3.943 | 38 |
| 39 | 67.5 | 1133.3 | 22.7 | C.490 | 0.264 | -C.249 | 0.138 | 0.273 | -2.258 | 0.531 | 39 |
| 40 | 58.4 | 985.5 | 19.6 | C. 490 | 0.284 | -0.267 | 0.432 | 0.358 | -0.342 | 0.700 | 40 |
| 41 | 45.8 | 769.2 | 15.4 | 0.49 C | 0.332 | -0.315 | 0.770 | 0.512 | -0.494 | 1.006 | 41 |
| 42 | 35.1 | 588.2 | 11.8 | 0.49 C | 0.438 | -3.418 | 1.088 | 0.702 | -0. 882 | 1.385 | 42 |
| 43 | 25.6 | 429.7 | 8.6 | 0.49 C | 0.690 | -0.672 | 1.258 | 0.949 | -0.932 | 1.881 | 43 |
| 44 | 17.4 | 292.3 | 5.8 | C. 490 | 1.144 | -1.105 | 1.524 | 1.378 | -1.339 | 2.716 | 44 |
| 45 | 12.0 | 203.5 | 4.C | 0.490 | 1.666 | -1.601 | 1.932 | 1.930 | -1.8t5 | 3.795 | 45 |
| 46 | 10.7 | 179.0 | 3.6 | 0.450 | 1.944 | -1.829 | 2.402 | 2.294 | -2.179 | 4.473 | 46 |
| 47 | 13.4 | 225.: | 4.5 | C.490 | 1.571 | -1.478 | 2.525 | 2.026 | -1.933 | 3.959 | 47 |
| 48 | 26.1 | 437.1 | 8.7 | 0.490 | 0.925 | -C. 828 | 1.855 | 1.324 | -1.228 | 2.552 | 48 |
| 45 | 63.1 | 1008.4 | $2 \mathrm{C}$. | 2.49C | 0.292 | -0.179 | 1.021 | 2.618 | -5.506 | 1.124 | 49 |
| 55 | 418.8 | $7026 . ?$ | $14 C .5$ | 0.490 | -0.183 | 0.308 | 0.659 | 0.474 | -0.348 | 0.822 | 50 |
| 51 | 427.7 | 7175.7 | 143.5 | 0.450 | -2.442 | 2.606 | 0.606 | 0.688 | -0.523 | 1.211 | 51 |
| 52 | 435.2 | 7301.6 | 146.C | 0.493 | -0.735 | 0.954 | 0.603 | 1.006 | -2.787 | 1.793 | 52 |
| 53 | 33.2 | 557.2 | 11.1 | 0.490 | -1.189 | 1.471 | 0.567 | 1.501 | -1.219 | 2.720 | 53 |
| 54 | 26.3 | 440.6 | 8.8 | 0.490 | -1.634 | 1.962 | 0.694 | 1.995 | - 2.668 | 3.662 | 54 |
| 55 | 23.2 | 398.8 | 7.8 | 0.490 | -1.941 | 2.295 | 2.584 | 2.315 | -1.961 | 4.276 | 55 |


| 116 | 105.2 | 1764.7 | 35.3 | 0.490 | -1.764 | 1.840 | -0.017 | 1.840 | -1.764 | 3.604 | 116 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 117 | 356.5 | 5980.9 | 119.6 | 0.490 | 0.115 | -0.105 | 0.193 | 0.152 | -0.141 | C. 293 | 117 |
| 118 | 397.7 | $6672 . \varepsilon$ | 133.5 | 0.490 | -0.018 | 0.030 | 0.495 | 0.255 | -0.243 | 0.497 | 118 |
| 119 | 152.t | 2563.0 | 51.2 | 0.490 | -0.241 | 0.281 | 0.589 | 0.414 | -0.374 | 0.788 | 119 |
| 123 | 136.8 | 2295.4 | 45.9 | 0.490 | -0.522 | 0.566 | 0.737 | 0.679 | -0.635 | 1.314 | 120 |
| 121 | 138.9 | 2331.1 | 46.6 | 0.490 | -0.785 | 0.844 | 0.658 | 0.908 | -0.849 | 1.756 | 121 |
| 122 | 126.6 | 2123.6 | 42.5 | 0.490 | -1.048 | 1.109 | 0.452 | 1.132 | -1.072 | 2.204 | 122 |
| 123 | 119.4 | 2003.6 | 40.1 | 0.490 | -1.290 | 1.356 | 0.190 | 1.360 | -1.293 | 2.653 | 123 |
| 124 | 111.2 | 1865.1 | 37.3 | 0.490 | -1.449 | 1.515 | 0.060 | 1.515 | -1.449 | 2.964 | 124 |
| 125 | 109.3 | 1833.8 | 36.7 | 0.490 | -1.517 | 1.585 | 0.008 | 1.585 | -1.517 | 3.102 | 125 |
| 126 | 334.8 | 5617.8 | 112.4 | 0.490 | 0.020 | -0.016 | 0.008 | 0.020 | -0.017 | 0.037 | 126 |
| 127 | 384.1 | 6445.2 | 128.9 | 0.490 | -0.123 | 0.133 | 0.437 | 0.258 | -0.248 | 0.507 | 127 |
| 128 | 141.1 | 2366.9 | 47.3 | 0.490 | -0.358 | 0.394 | 0.646 | 0.513 | -0.478 | 0.991 | 128 |
| 129 | 129.1 | 2165.8 | 43.3 | 0.490 | -0.616 | 0.656 | 0.753 | 0.759 | -0.719 | 1.478 | 129 |
| 130 | 132.8 | 2228.9 | 44.6 | 0.490 | -0.835 | 0.888 | 0.551 | 0.931 | -0.878 | 1.809 | 130 |
| 131 | 123.8 | 2076.9 | 41.5 | C. 490 | -1.014 | 1.067 | C. 299 | 1.078 | -1.025 | 2.103 | 131 |
| 132 | 121.0 | 2031.0 | $4 \mathrm{C.6}$ | 0.490 | -1.129 | 1.186 | 0.122 | 1.188 | -1.130 | 2.318 | 132 |
| 133 | 117.2 | 1966.7 | 39.3 | 0.490 | -1.180 | 1.237 | 0.038 | 1.237 | -1.180 | 2.417 | 133 |
| 134 | 258.8 | 4341.7 | 86.8 | 0.490 | -0.049 | 0.051 | -0.052 | 0.057 | -0.056 | 0.113 | 134 |
| 135 | 116.1 | 1948.0 | 39.0 | 0.490 | -0.185 | 0.194 | 0.474 | 0.308 | -0.299 | 0.607 | 135 |
| 136 | 136.5 | 2289.6 | 45.8 | 0.490 | -0.398 | 0.431 | 0.648 | 0.542 | -0.510 | 1.052 | 136 |
| 137 | 129.6 | 2174.0 | 43.5 | 0.490 | -0.596 | 0.632 | 0.604 | 0.702 | -0.666 | 1.368 | 137 |
| 138 | 135.9 | 2279.9 | 45.6 | 0.490 | -0.702 | 0.747 | 0.323 | 0.765 | -0.720 | 1.484 | 138 |
| 139 | 131.4 | 2205.0 | 44.1 | 0.490 | -0.747 | 0.791 | 0.164 | 0.795 | -0.752 | 1.547 | 139 |
| 140 | 132.0 | 2215.2 | 44.3 | 0.450 | -0.766 | 0.812 | 0.041 | 0.812 | -0.767 | 1.579 | 140 |
| 141 | 284.5 | 4773.1 | 95.5 | C. 490 | -0.064 | 0.064 | 0.030 | 0.066 | -0.066 | 0.132 | 141 |
| 142 | 120.1 | 2314.4 | 40.3 | 0.490 | -0.174 | 0.184 | 0.475 | 0.302 | -0.292 | 0.595 | 142 |
| 143 | 141.8 138.8 | 2379.5 2329.3 | 47.6 | 0.490 | -0.324 | 0.352 | 0.473 | 0.427 | -0.398 | 0.825 | 143 |
| 144 | 138.8 | 2329.3 | 46.6 | 0.490 | -0.397 | 0.426 | 0.295 | 0.452 | -0.423 | 0.875 | 144 |
| 145 146 | 146. 2 | 2452.3 | 49.0 | 0.490 | -0.380 | C. 415 | 0.116 | 0.419 | -0.385 | 0.804 | 145 |
| 146 | 146.2 | 2452.7 | 49.1 | 0.490 | -0.365 | 0.398 | 0.047 | 0.399 | -0.366 | 0.765 | 146 |
| 148 | 126.9 | 1653.2 2128.9 | 33.1 42.6 | 0.490 0.490 | -0.022 -0.107 | 0.024 | 0.118 0.328 | 0.064 | -0.062 | 0.126 | 147 |
| 149 | 141.5 | 2373.8 | 47.5 | 0.490 | -0.135 | 0.155 | 0.328 0.109 | 0.203 0.165 | -0.194 | 0.396 0.310 | 148 |
| 159 | 141.8 | 2378.5 | 47.6 | 0.490 | -0.103 | 0.121 | 0.094 | 0.130 | -0.112 | 0.242 | 150 |
| 151 | 144.4 | 2422.8 | 48.5 | 0.490 | -0.096 | 0.117 | 0.023 | 0.117 | -0.097 | 0.214 | 151 |
| 152 | 82.3 317 | 1381.0 | 27.6 | 0.490 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 152 |
| 153 | 317.6 | 5329.3 | 106.6 | 0.490 | 2.0 | 0.0 | 0.9 | 0.0 | 0.0 | 0.0 | 153 |
| 154 | 317.6 | 5329.3 | 106.6 | 0.490 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 154 |
| 155 | 317.6 | 5329.3 | 106.6 | 0.490 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 155 |

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## AN ABSTRACT OF A MASTERS THESIS

submitted in partial fulfillment of the

> requirements for the degree

MASTER OF SCIENCE

Department of Civil Engineering

KANSAS STATE UNIVERSITY Manhattan, Kansas

1979

## ABSTRACT

Accurate prediction of the deformation or soil movement which occurs in the foundation of embankments is necessary because of the effect this deformation may have on drainage structures utility lines, etc. The effect of desiccation on the deformation of the foundation solis and its effect on the overall stability of embankments must be considered. A literature review of desiccation yielded information regarding the process of desiccation. However, very little information on changes in soil strength or the stress-strain characteristics resulting from desiccation was found.

Instrumentation was installed to monitor the stability and foundation deformation during construction of an embankment by the Kansas Department of Transportation. The actual foundation deformation was compared with predictions made by two finite element computer analyses. The first analysis did not consider the effects of desiccation and predicted deformations were far in excess of those actually measured. The second analysis did account for the increased strength near the ground surface which resulted from desiccation. Deformation predictions made during this analysis were much more accurate than those made without considering the effects of desiccation.

Stability analyses using circular arc form of failure were performed. According to these analyses, desiccation resulted in an increase of 25 percent in the computed factor of safety against sliding for the embankment analyzed.

Methods of recognizing the desiccated zone and accounting for its incrased strength in the analysis are presented.

